

Changes in Reactor Power with time



Neutron Life

- * Average distance travelled $< 1\text{m}$
- * Life time 0.001 sec



Power Increase

$$P_{1gen} = P_0 \times k$$

$$P_{2gen} = P_0 \times k \times k = k^2$$

$$P_{ngen} = P_0 k^n$$

If a generation is 0.001 second then after 1 second

$$P_{1000} = P_0 \times k^{1000}$$



Power Increase

If a generation is 0.001 second then after 1 second

$$P_{1000} = P_0 \times k^{1000}$$

For a $\frac{1}{2}$ mk reactivity insertion

$$P_{1000} = P_0 1.0005^{1000} = 1.64 P_0$$

This is not the case!!!!

We have not taken into account the effect of the delayed neutrons.



Reactor Period

For small changes in reactivity it can be shown that

$$P = P_0 e^{t/T}$$

Where $T \approx \frac{l}{\Delta k}$ for small Δk

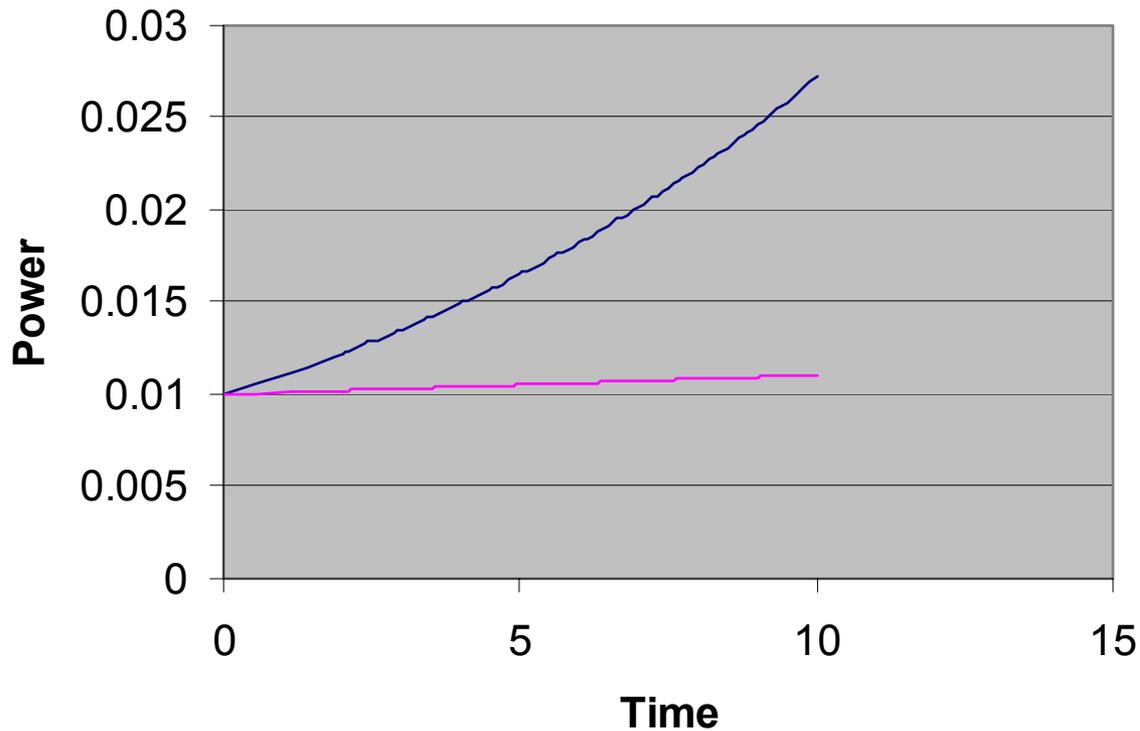


Reactor Period

- ★ The time it takes for reactor power to increase by a factor of e
- ★ Need to be long to control the reactor
- ★ Proportional to average neutron life time
- ★ Inversely proportional to changes in reactivity Δk



Reactor Power Changes



Reactor Periods of 10 and 100 sec



Effect of delayed neutrons

$\approx 0.65\%$ of all neutrons are delayed

Average life time of delayed neutrons is ≈ 13 sec.

This drastically alters the average neutron life time

$$l = .9935 \times 0.001 + .0065 \times 13 = 0.085 \text{ seconds}$$



● Effect of Delayed Neutrons

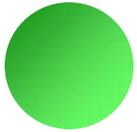
Now our one-half millik change in reactivity after one second

$$T = \frac{l}{\Delta k} = \frac{0.085}{.0005} = 170$$

$$P = P_0 e^{t/T} = P_0 e^{1/170} = 1.006P_0$$

A much more manageable power increase.





Prompt Critical

- ★ Previous approximation for small Δk
- ★ For large Δk the effect of the delayed neutrons is negated
- ★ Reactor power changes with prompt neutrons only
- ★ Rapid power changes





Summary

- ★ Reactor period must be long for control to be possible
- ★ Depends on average life-time of neutrons
- ★ Most neutrons have a life time in the range of 1 msec.
 - These are prompt neutrons.
- ★ Delayed neutrons appear after the fission process.
 - Delayed neutrons increase the average life time of the neutrons



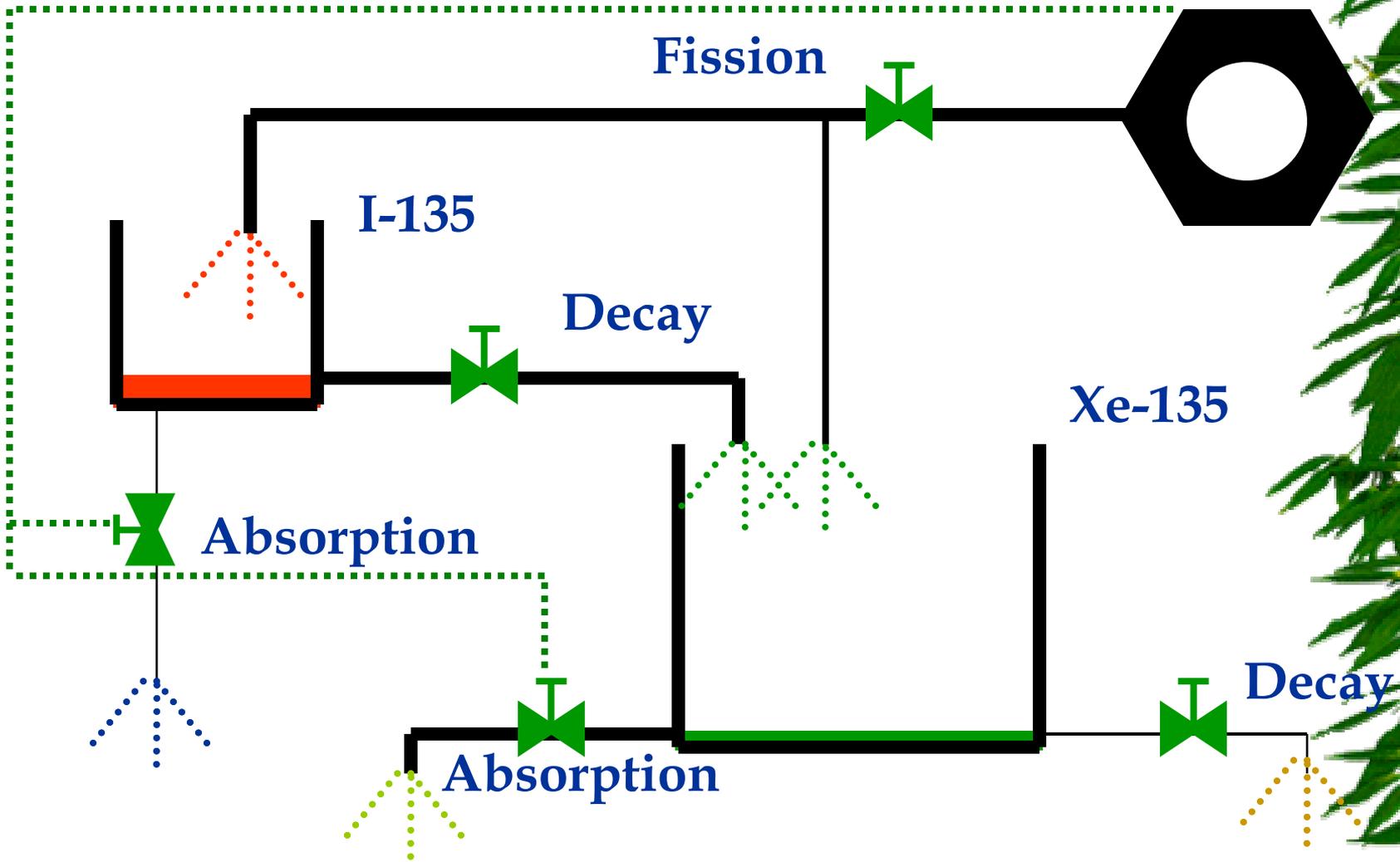
Xenon

Xenon

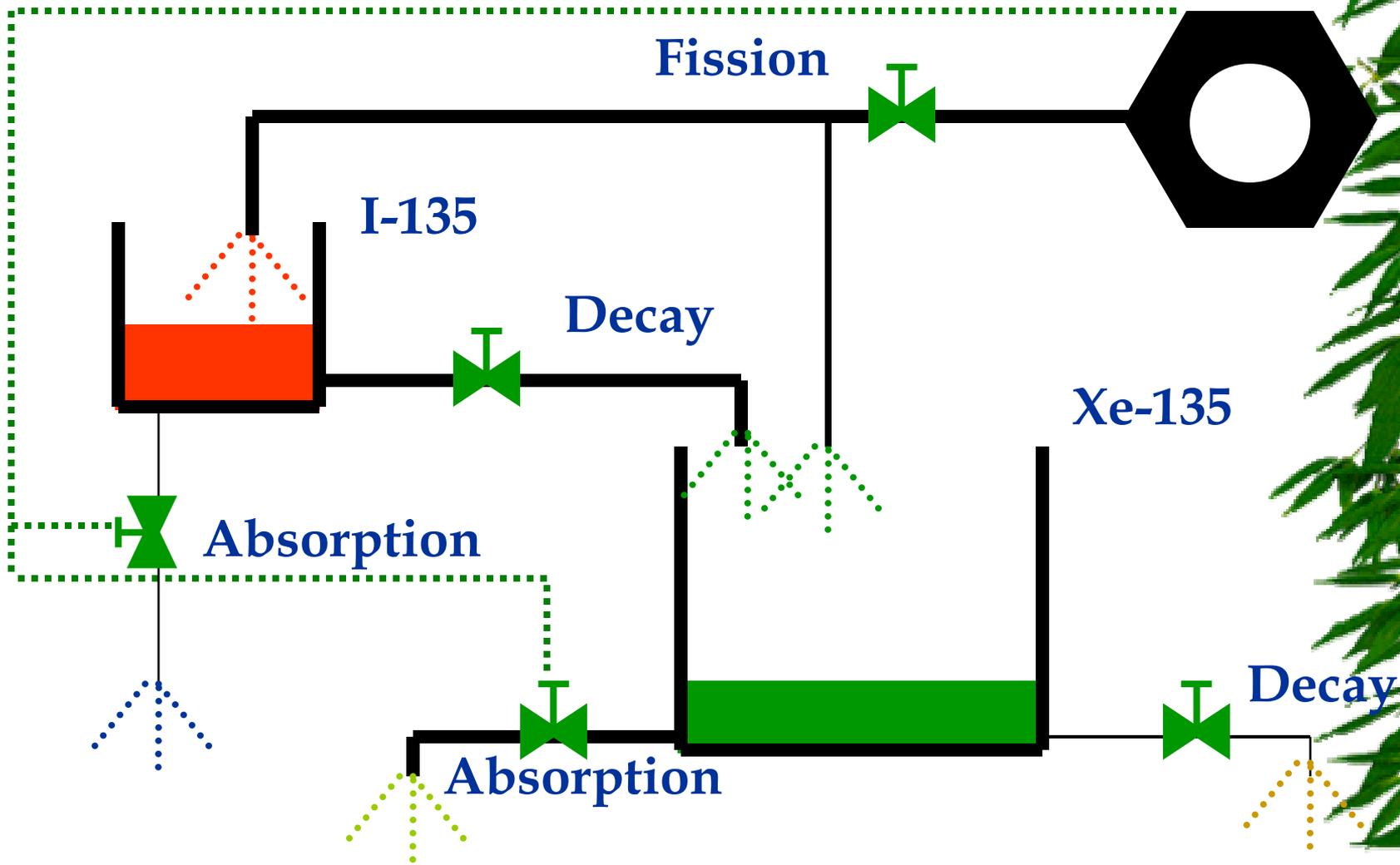
A Fission Product Poison



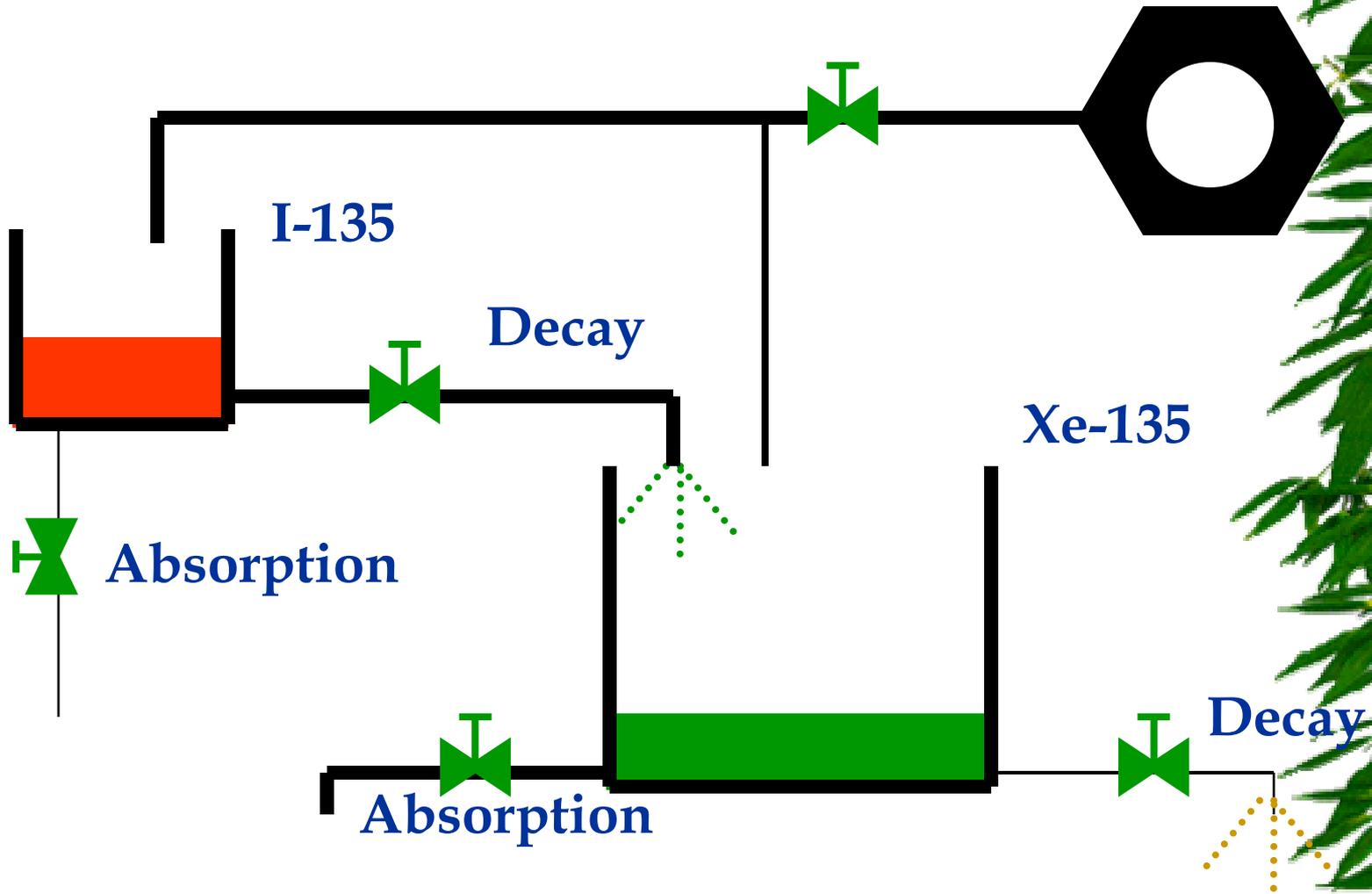
Xenon



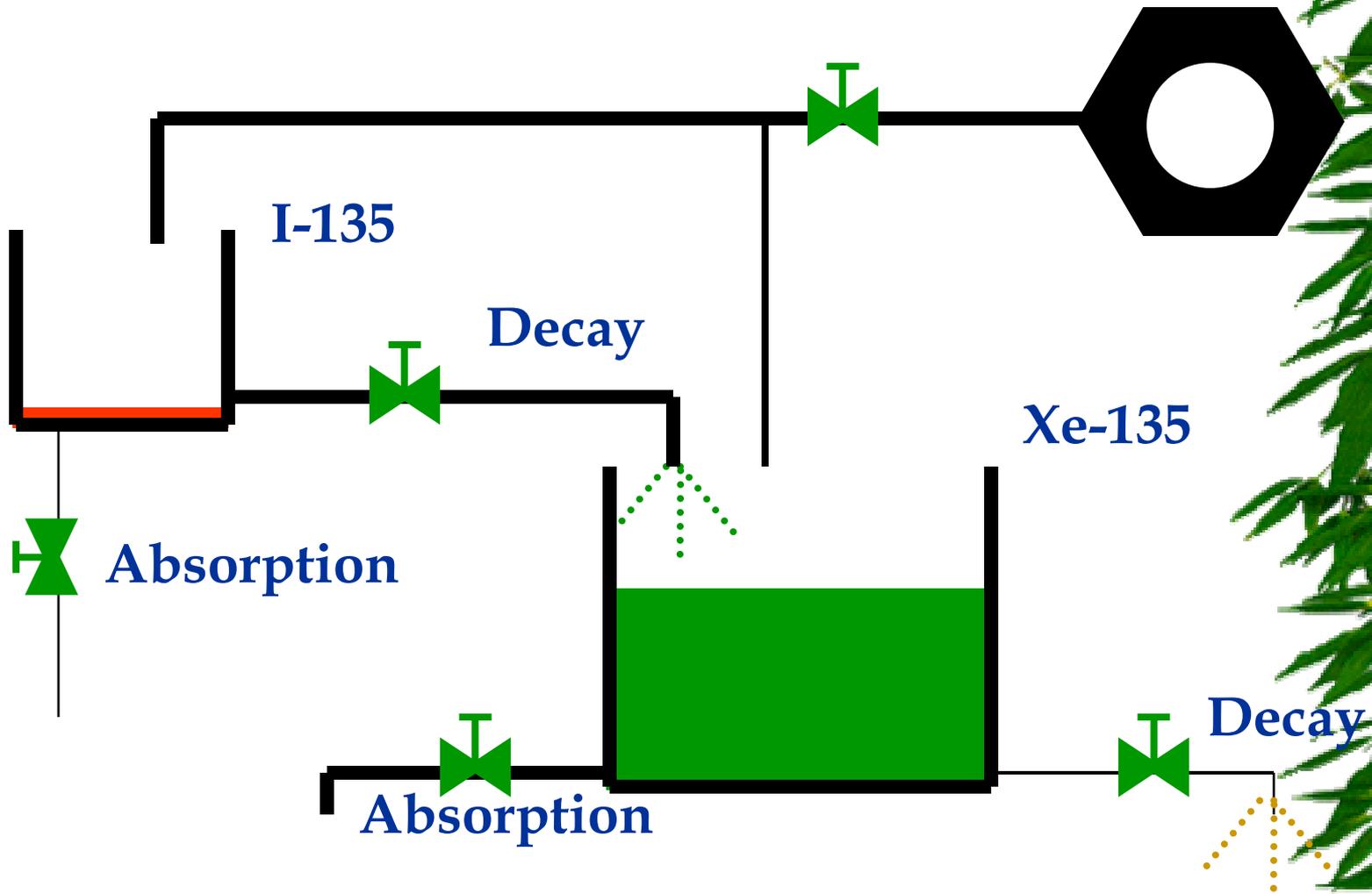
Equilibrium Xenon



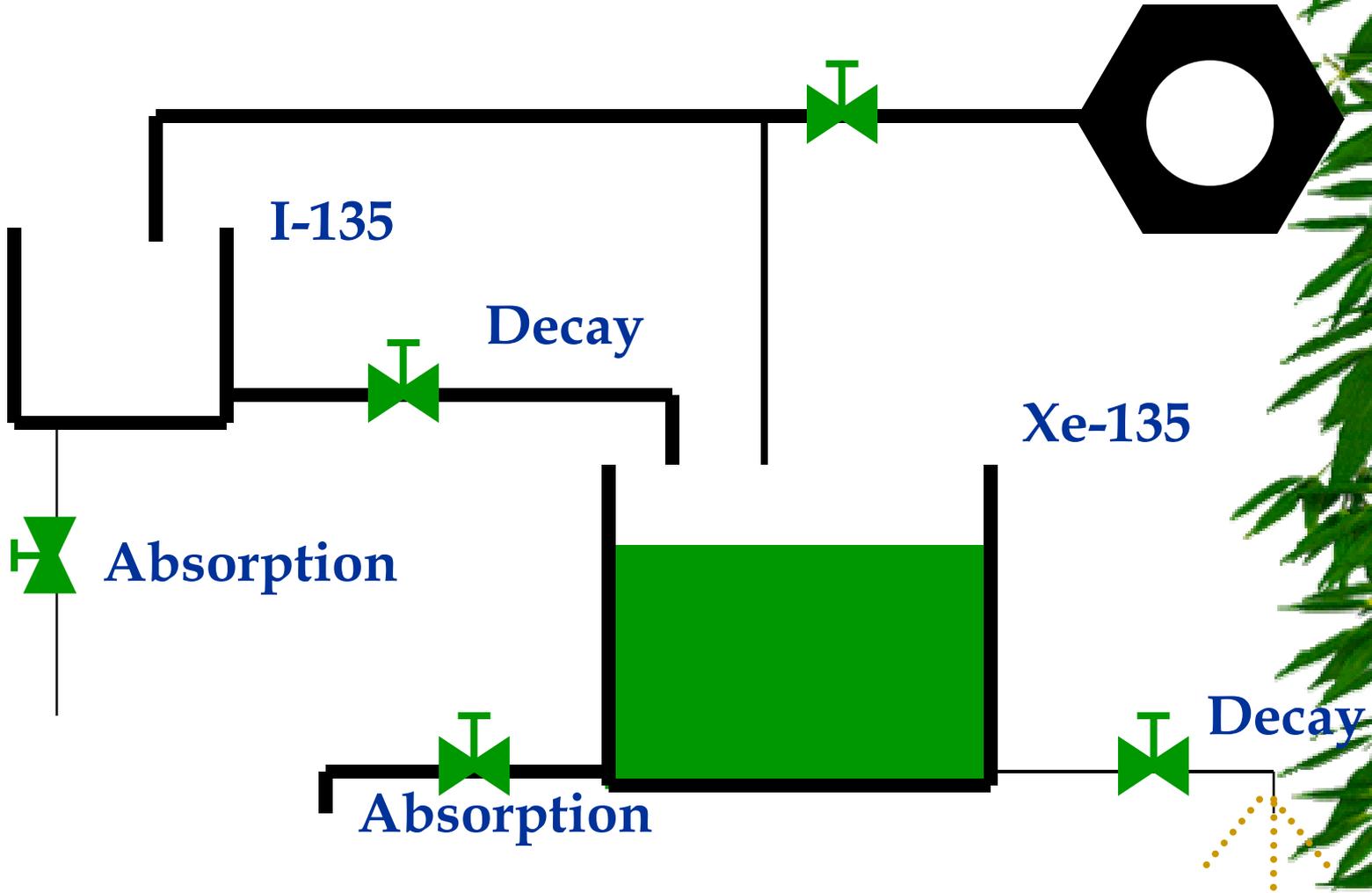
Xenon Immediately on stopping fission



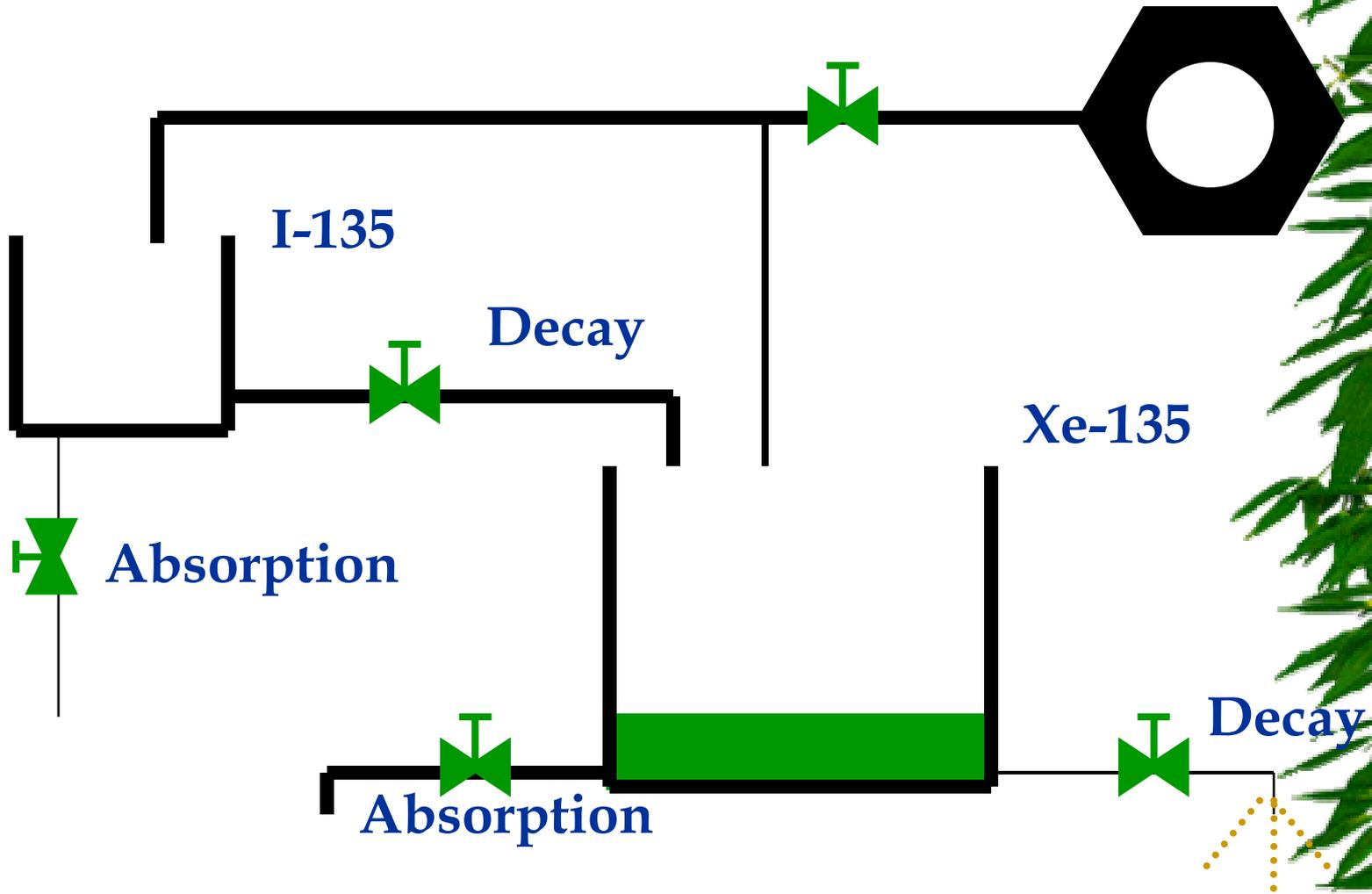
Xenon build up



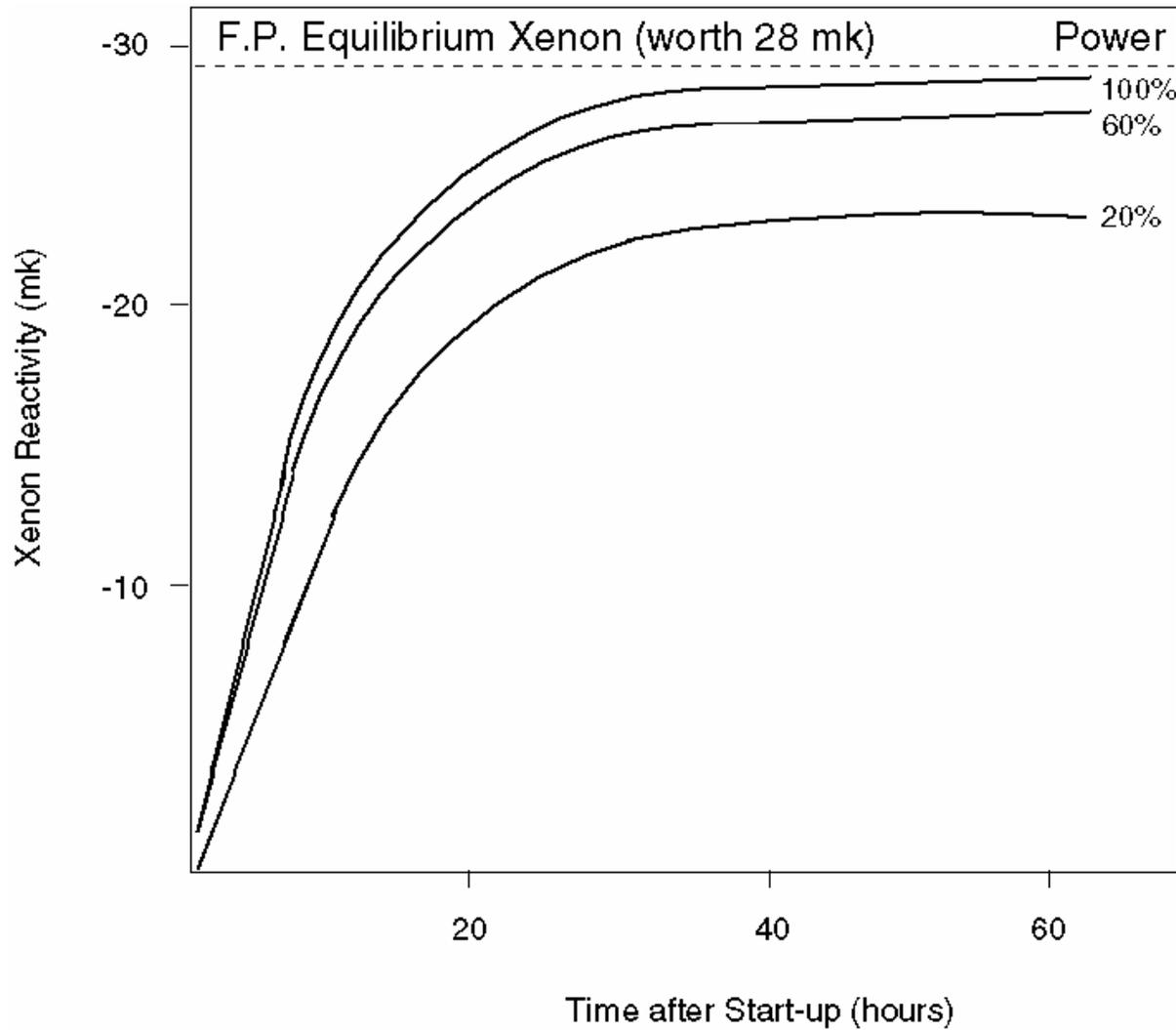
Iodine Disappears



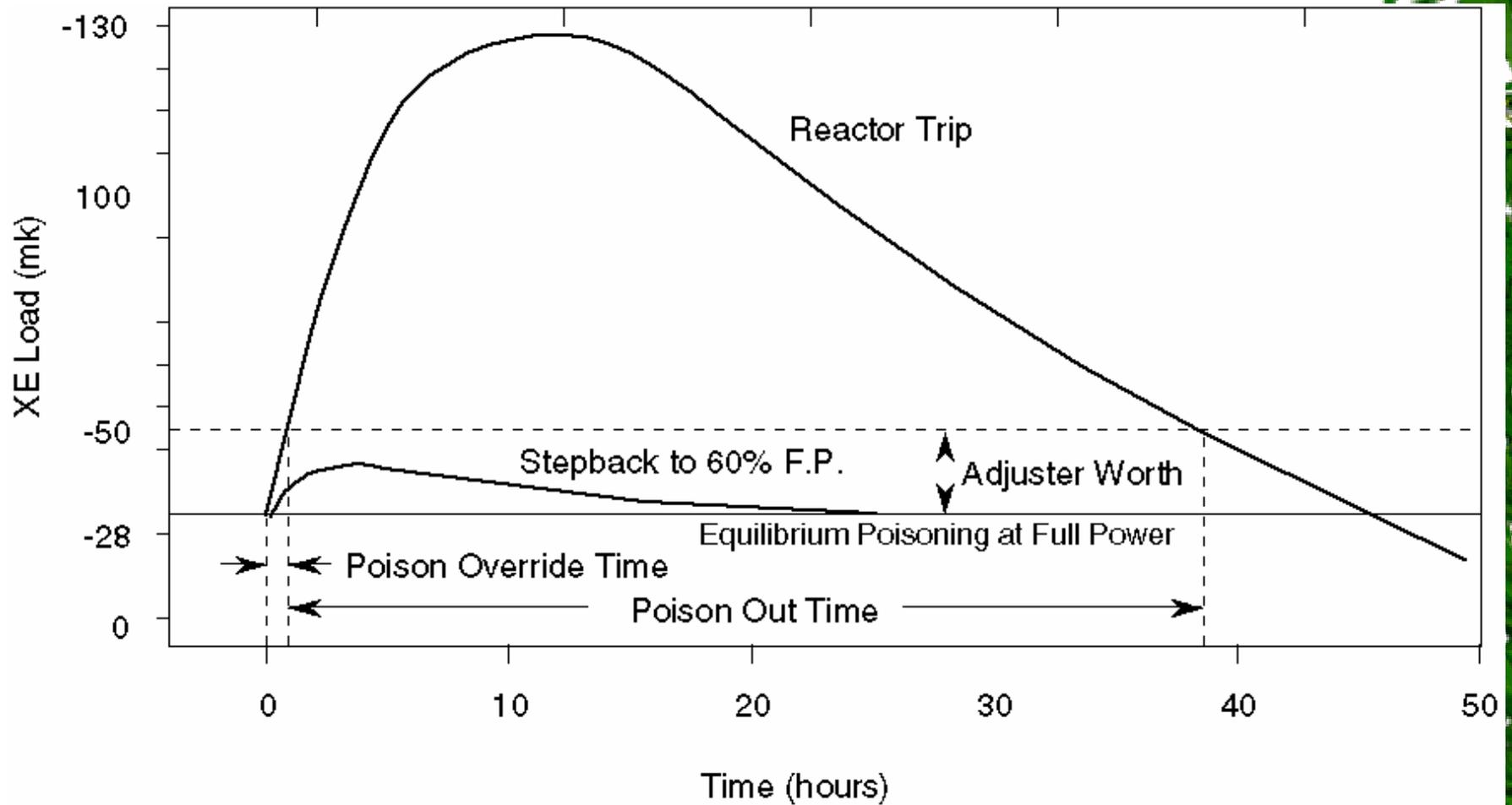
Xenon Disappears



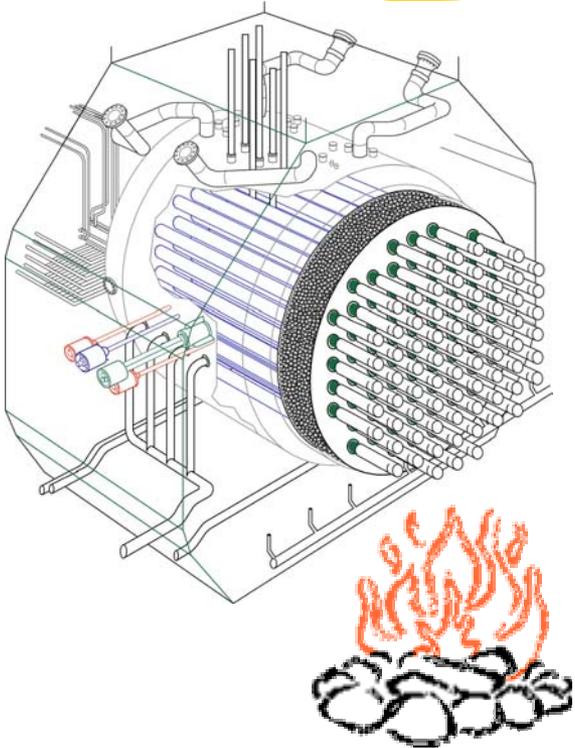
Equilibrium Xenon Concentration



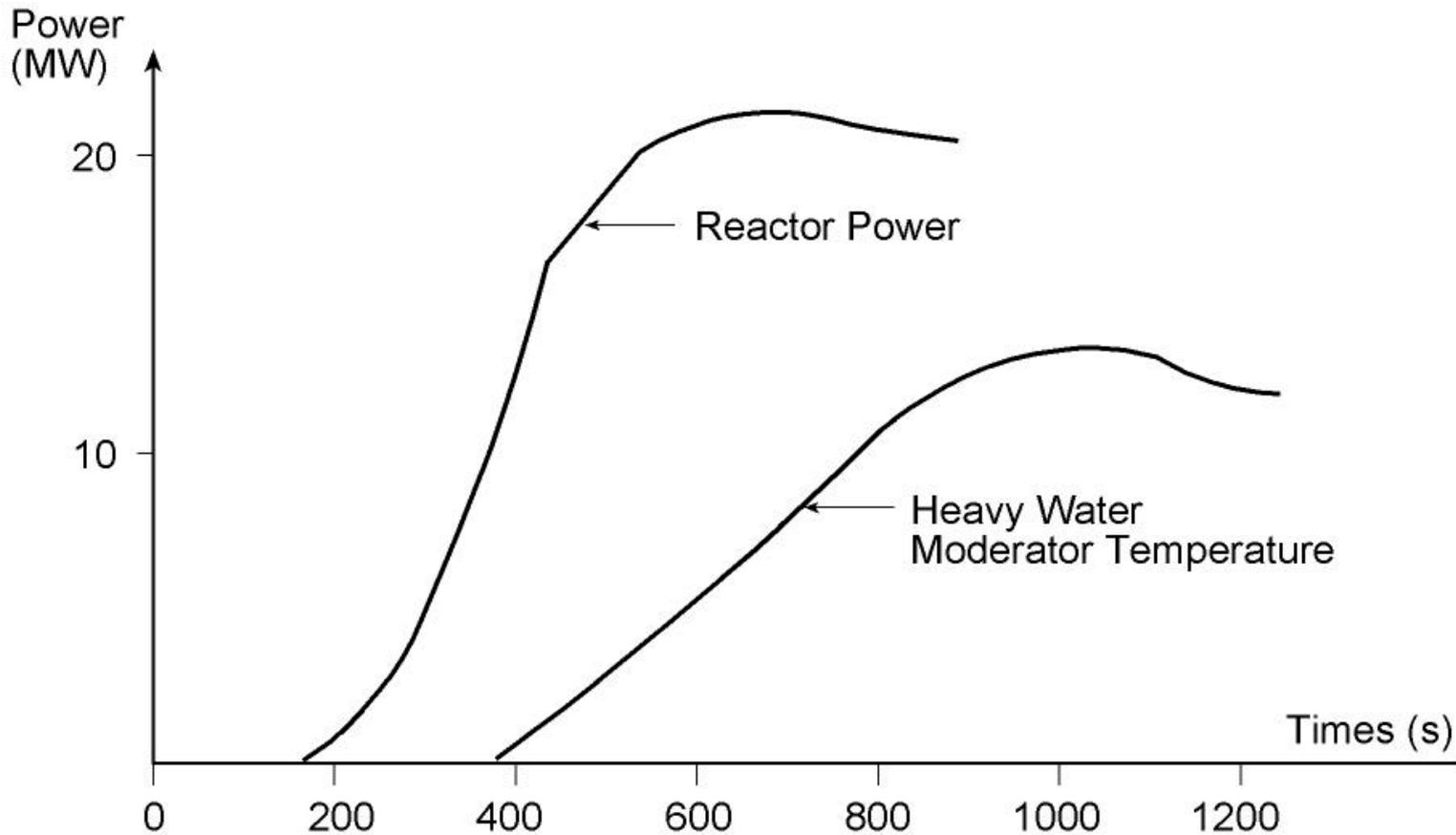
Xenon Transients



Reactivity Temperature Effects



NRX Experiment





Temperature Coefficients

- ★ $\text{mk}/^{\circ}\text{C}$ or $\mu\text{k}/^{\circ}\text{C}$
- ★ Moderator
- ★ Heat Transport System
- ★ Fuel
- ★ Each is independent
- ★ Each happens on its own time scale
- ★ At power fuel predominates

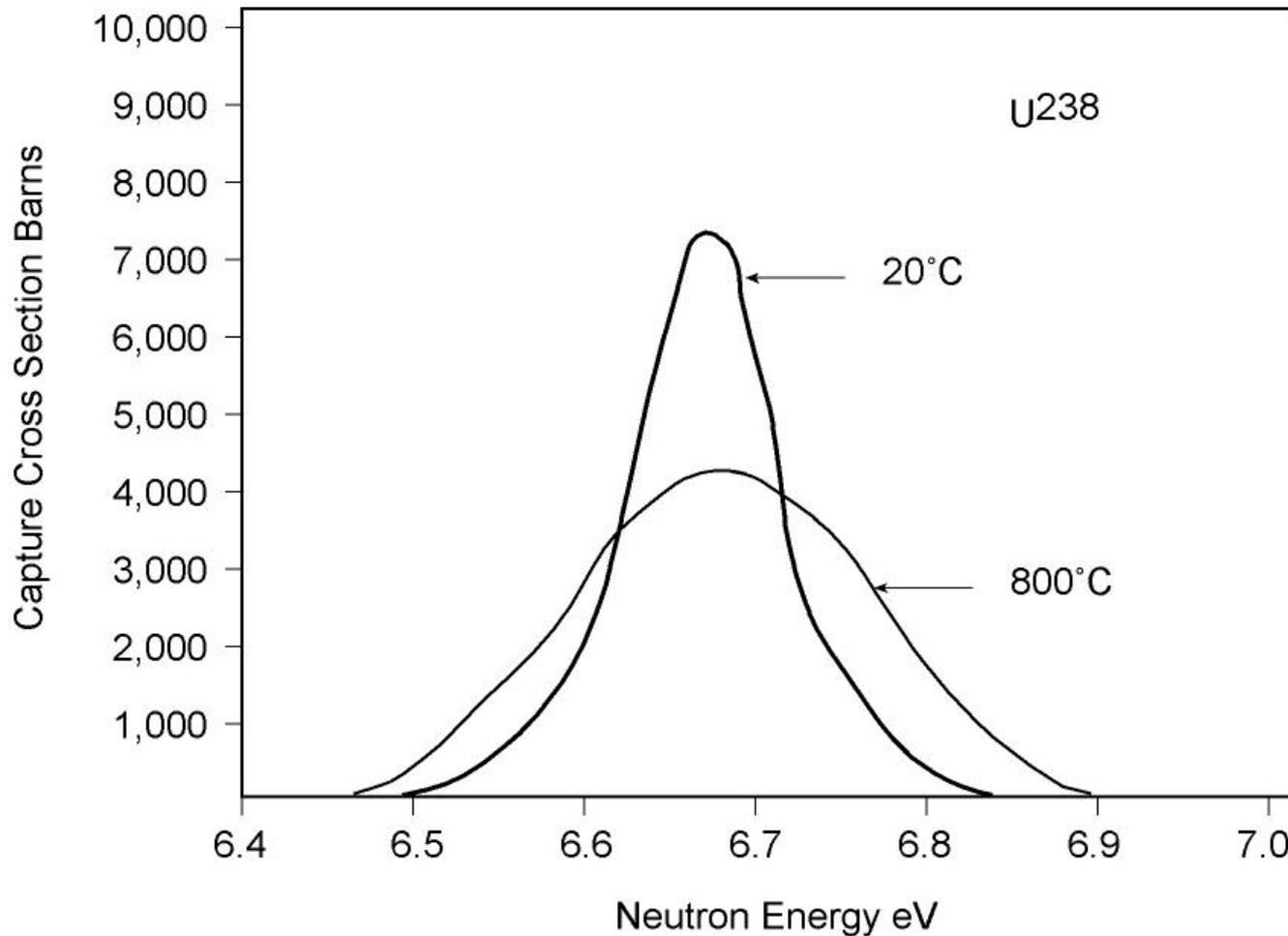


Fuel

- ★ Two effects
 - Increased resonance Capture
 - Changes in relative cross sections
- ★ Coefficient is negative
 - Increase temperature adds negative reactivity



Increased Resonance Capture



Changes in cross sections

Probability of a fission

$$\sigma_f^{fuel}$$

Probability of absorption in fuel

$$\sigma_a^{fuel}$$

Decreases for U-235 (adds negative reactivity)

Increases for Pu-239 (adds positive reactivity)

In equilibrium fuel the Pu-239 predominates

Plut like 'em hot



Combined Effect

- ★ Resonance broadening always predominates
 - Always negative
- ★ More negative with fresh fuel
- ★ Fresh fuel ≈ -0.013 mk/°C
- ★ Equilibrium fuel -0.004 mk/°C



Power Coefficient

- ★ Total reactivity change for zero power hot to full power
 - Zero power hot is a term used to denote the moderator and HTS up to operating temperature but low fission power levels
- ★ $\approx 5 \text{ mk}$



Void Coefficient

- ★ Reactivity change for complete voiding of the HTS
- ★ $\approx +10$ mk for complete voiding
 - This is a bad thing
- ★ HTS cannot void completely instantly
- ★ Reactor trips on high rate of power change and high power protect the reactor

