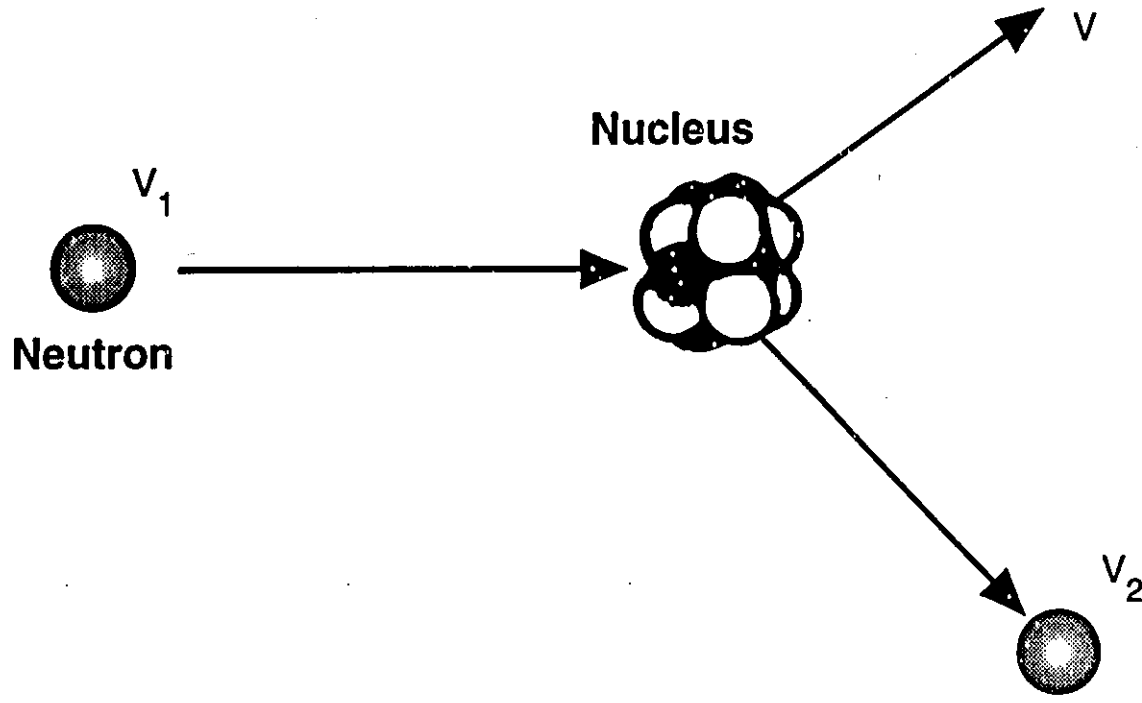
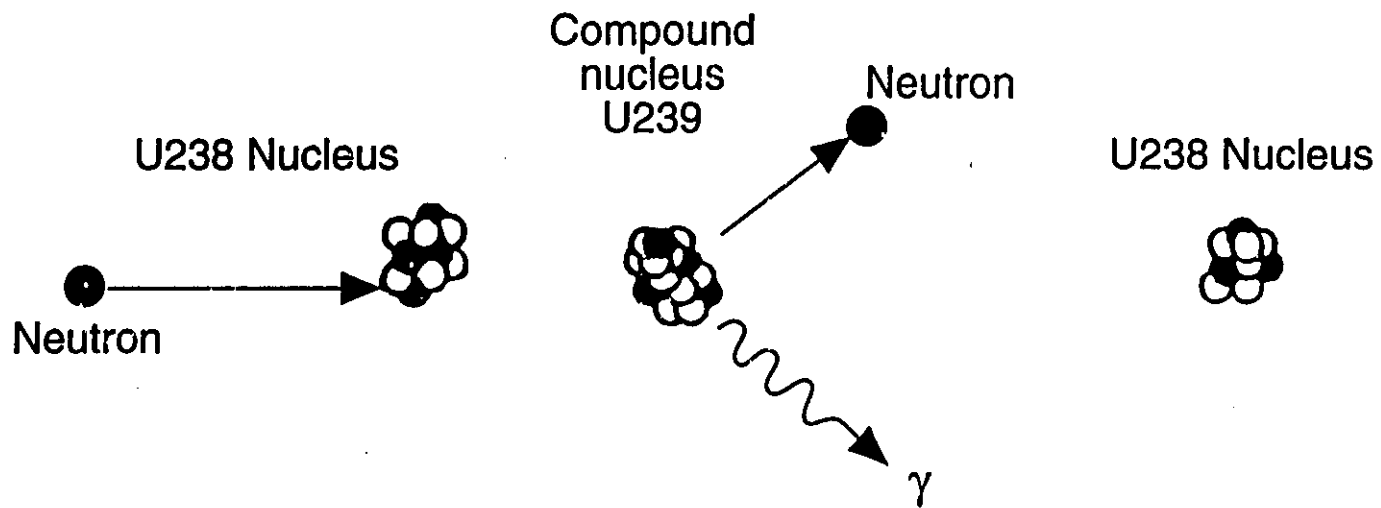


# Elastic Collision



# Inelastic Scattering



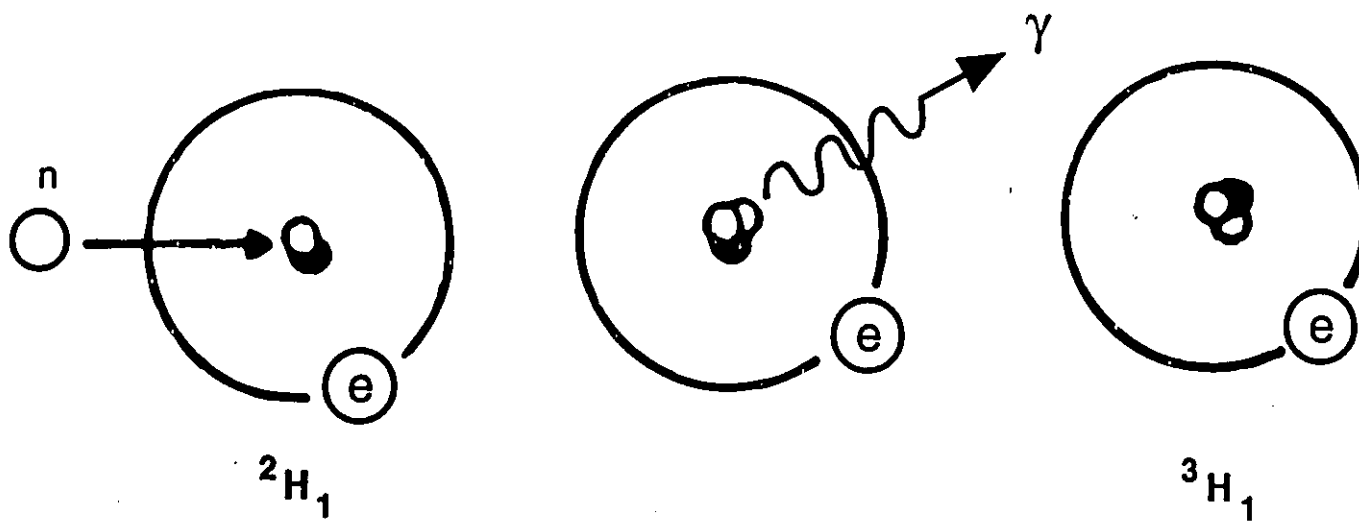
# Transmutation



This reaction may be written as



# Radiative Capture



# Fission Yield of U-235 and Pu-239

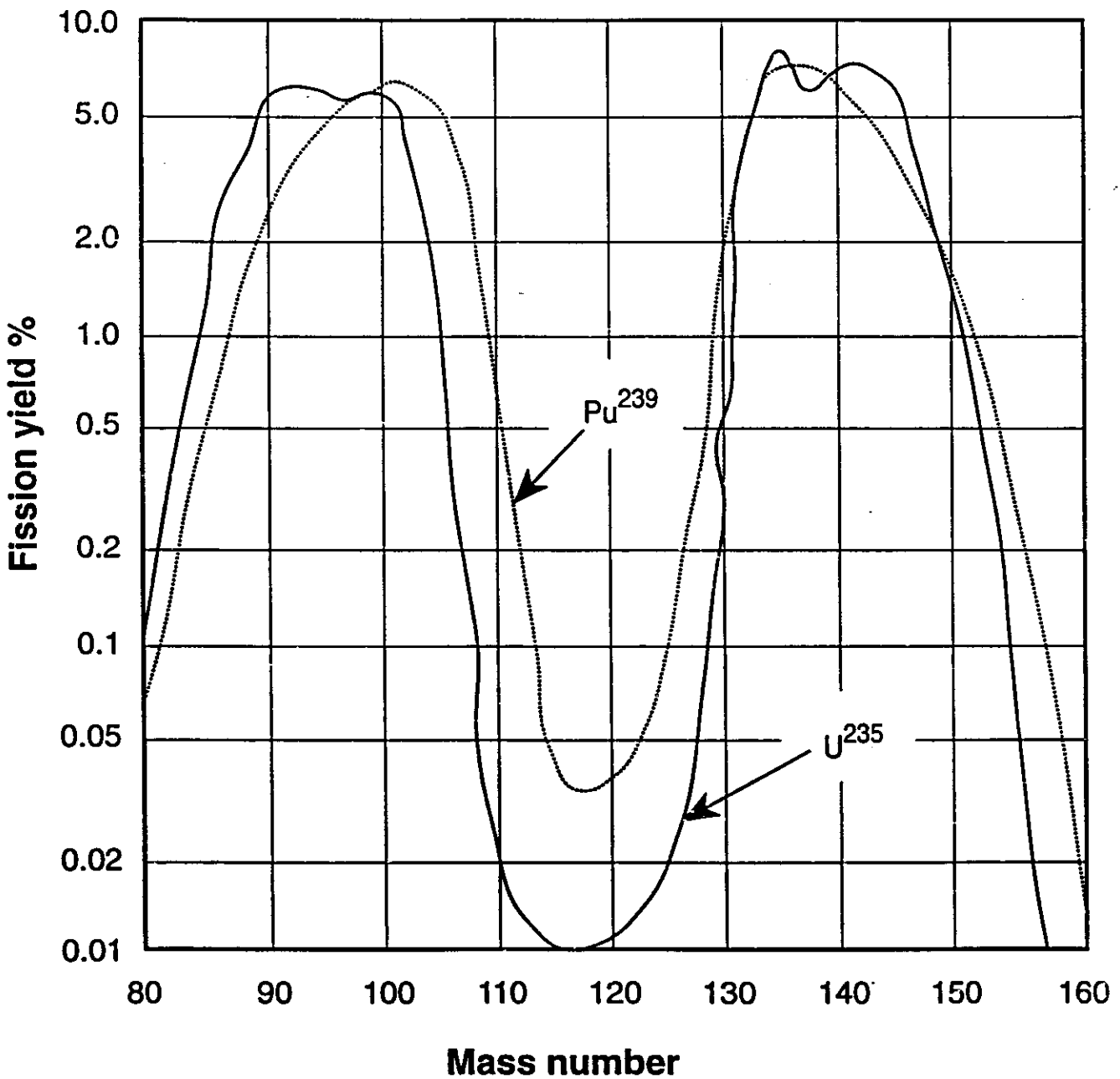
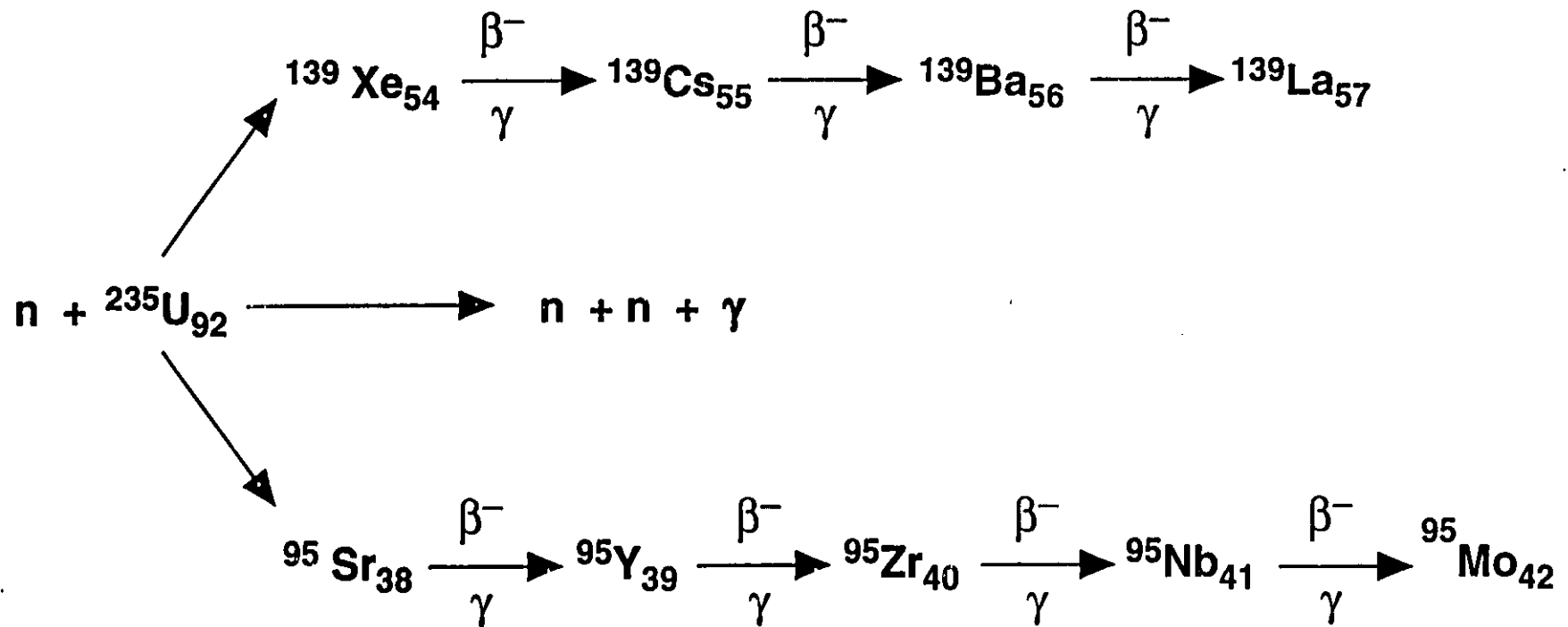
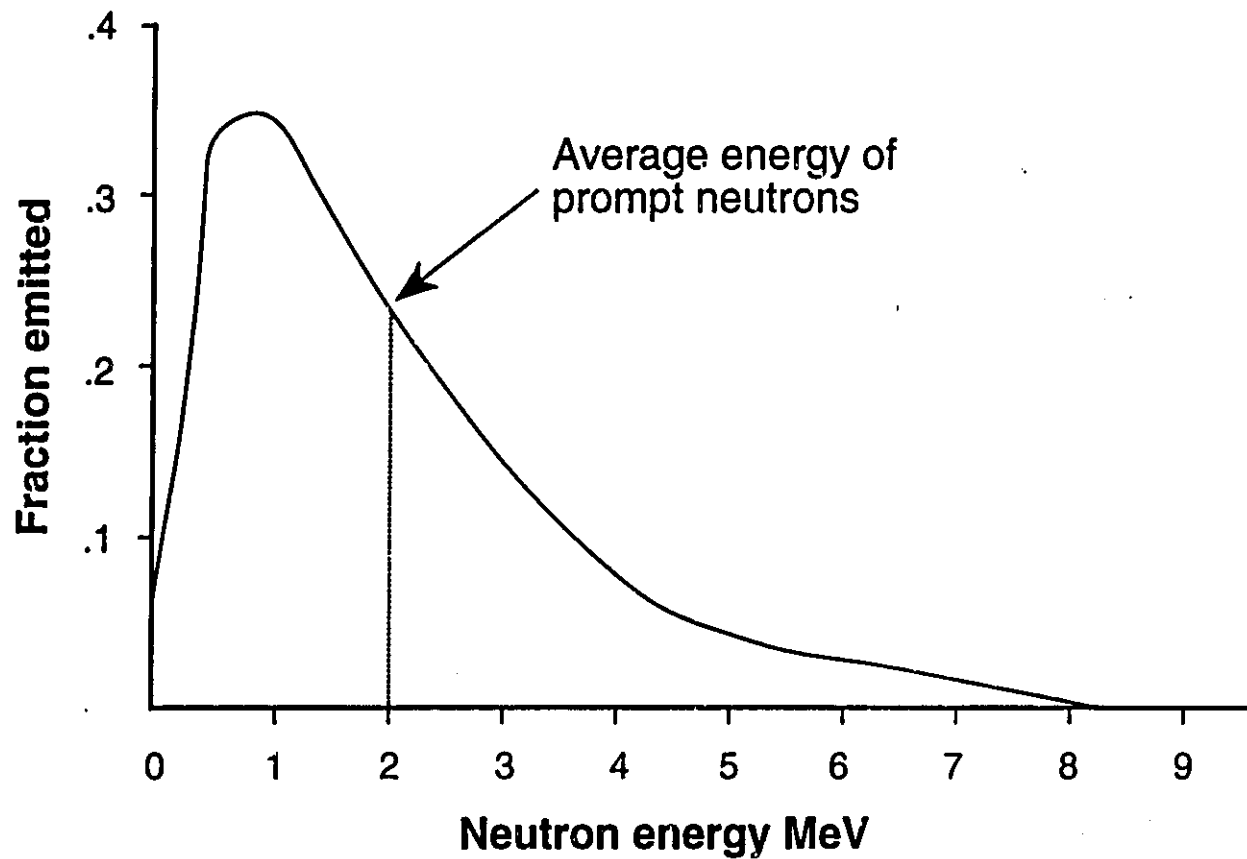


Fig. :

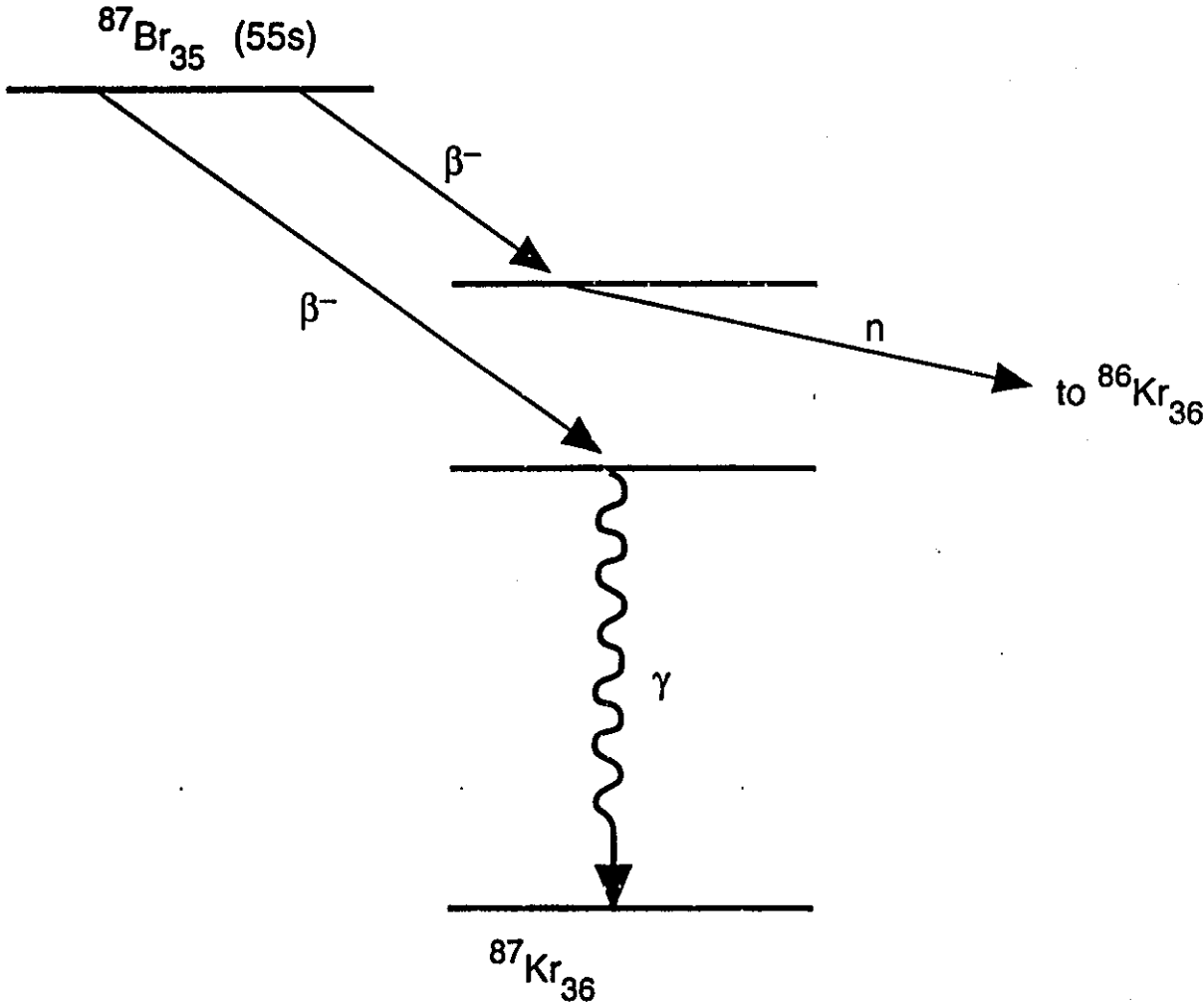
# Fission Product Decay Chain



# Energy Distribution of Prompt Fission Neutrons



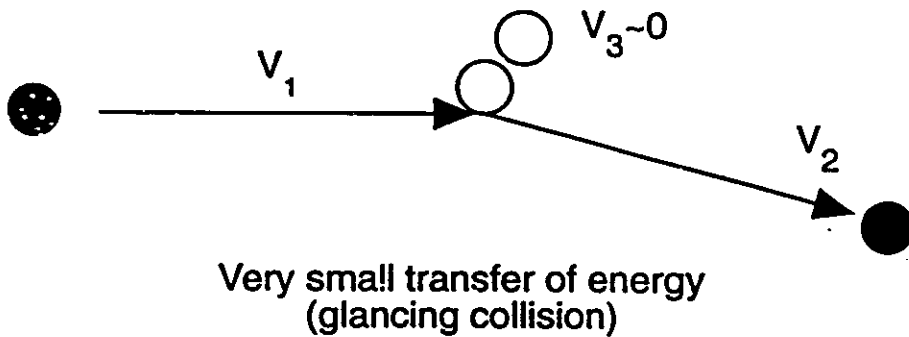
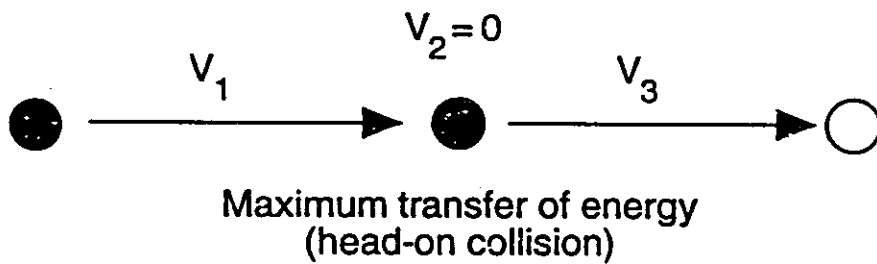
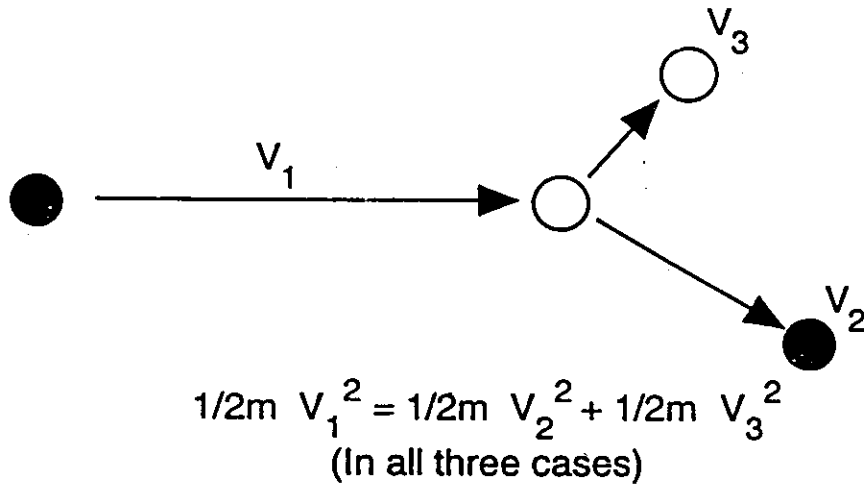
# Production of Delayed Neutron From Br-87 (normal beta-gamma decay mode also shown)





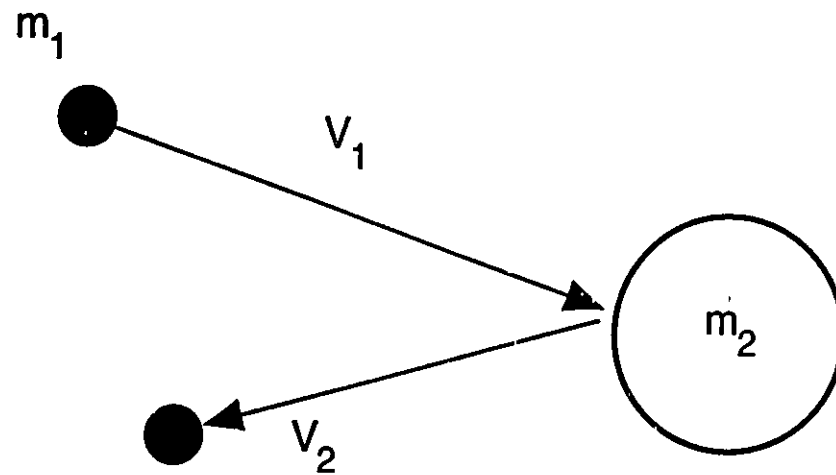
# Elastic Collisions

(for equal masses)



# Elastic Collision

$$(m_2 \gg m_1)$$



If  $m_2 \gg m_1$ ,

$$V_1 \sim V_2$$

and

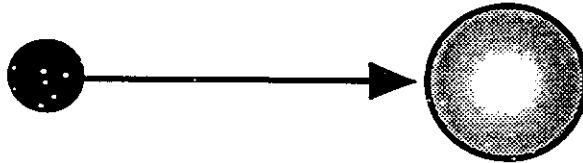
$$V_3 \sim 0$$

## Average Number of Elastic Collisions to Thermalize Fission Neutrons in Various Materials

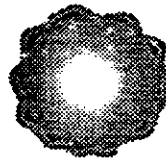
H	18
D (Deuterium)	25
H <sub>2</sub> O (Light water)	20
D <sub>2</sub> O (Heavy water)	36
C-12 (Graphite)	115
U-238	2172

# Inelastic Scattering (internal reaction)

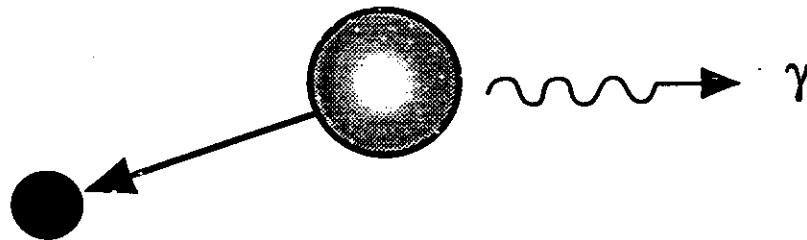
1. Neutron enters stable nucleus



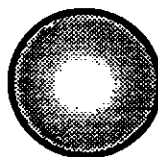
2. Nucleus is excited



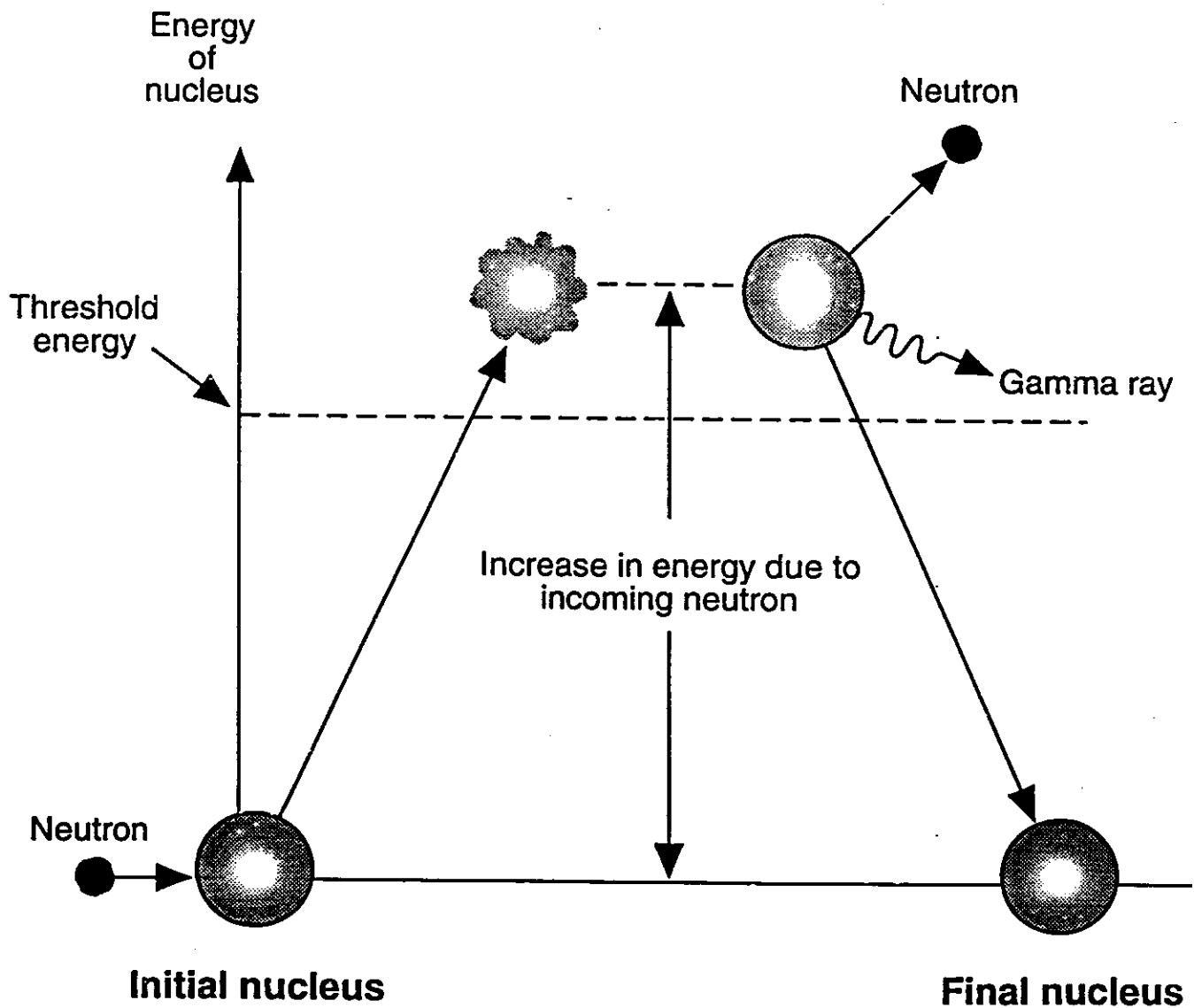
3. Neutron and  $\gamma$  - photon are emitted



4. Nucleus is stable again

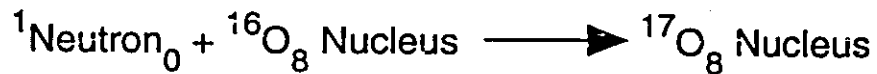
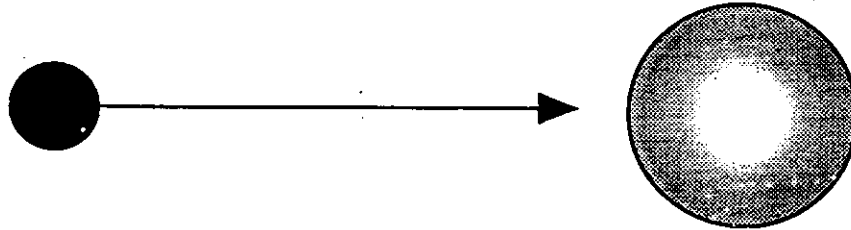


# Inelastic Scattering (above threshold energy)

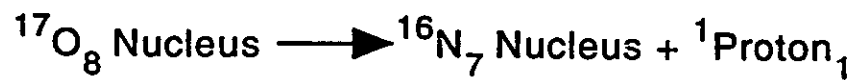
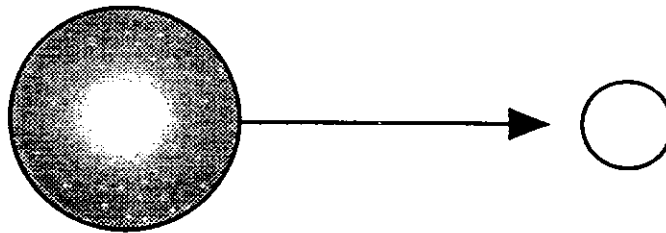


# Nuclear Transmutation

1. Neutron enters stable nucleus



2. Another particle leaves excited nucleus



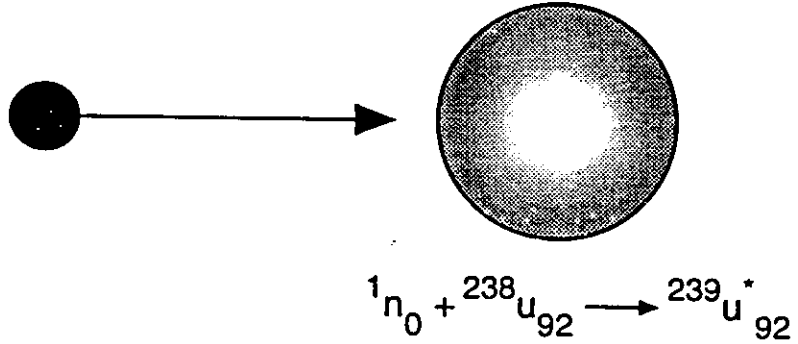
This may be written as



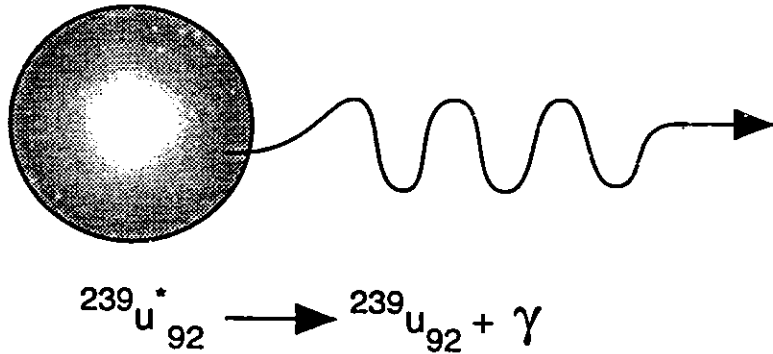
( ${}^{16}_7\text{N}$  nucleus subsequently emits gamma rays)

# Radiative Capture

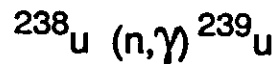
1. Neutron enters stable nucleus



2. Gamma ray leaves excited nucleus

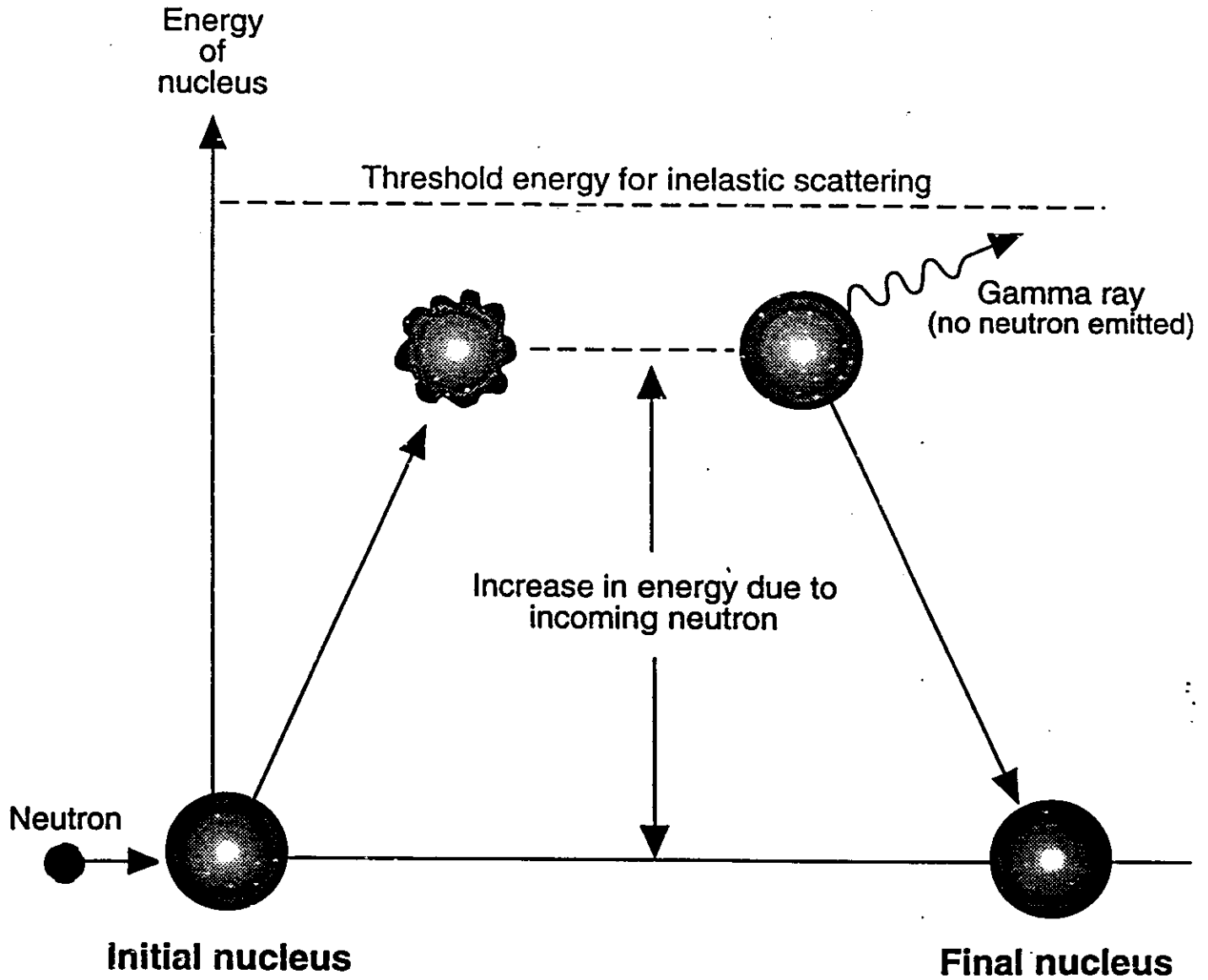


This may be written as



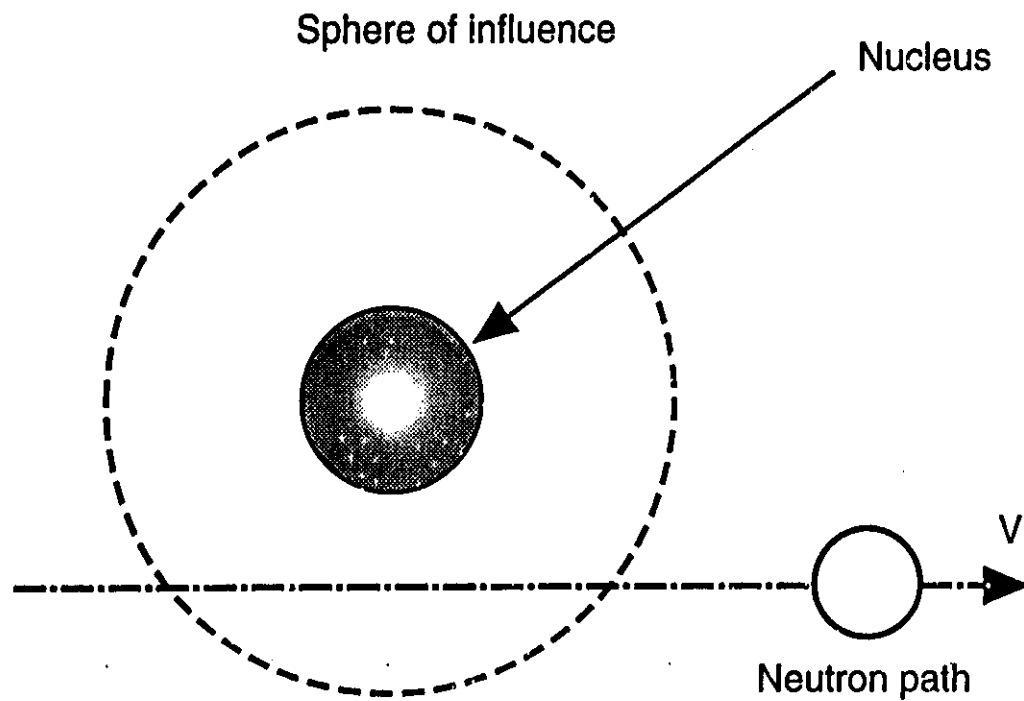
${}^{239}_{92}\text{U}$  subsequently transmutes to  ${}^{239}_{94}\text{Pu}$ . How?

# Radiative Capture (below threshold energy)





# Radiative Capture



Time spent in sphere of influence

$$t \propto \frac{1}{v}$$

If probability of capture  $\propto$  time

$$\sigma_a \propto \frac{1}{v}$$

## Spontaneous Fission and Alpha Decay Rates of Uranium

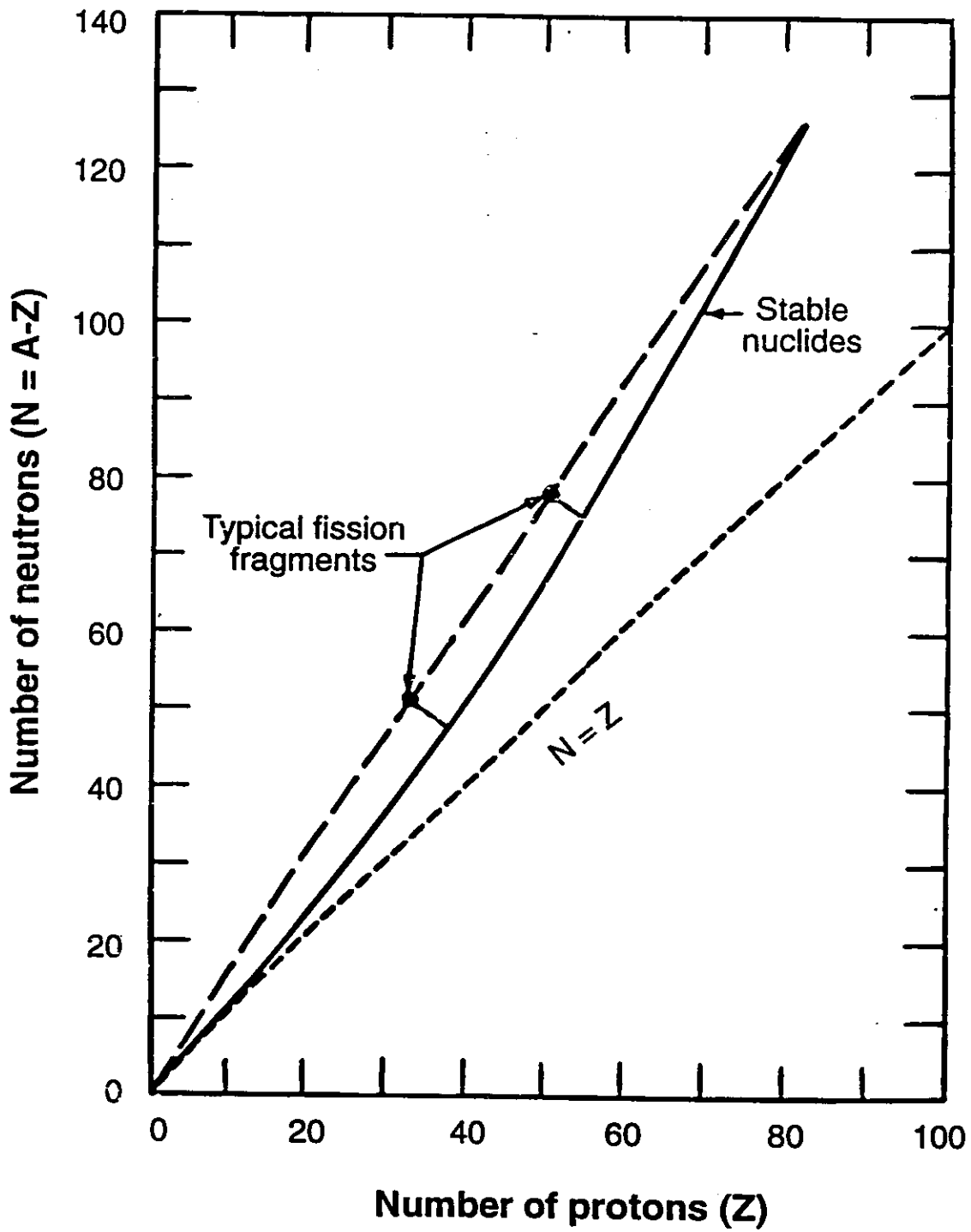
	$t_{1/2} (\alpha)$ (years)	$t_{1/2} (\text{s.f.})$ (years)	$\alpha$ decay rate (atoms /s/kg)	s.f. decay rate (atoms /s/kg)
<b>U-235</b>	$7.1 \times 10^8$	$1.2 \times 10^{17}$	$79 \times 10^6$	0.3
<b>U-238</b>	$4.5 \times 10^9$	$5.5 \times 10^{15}$	$12 \times 10^6$	6.9

## Fissile Materials

Fuel	Neutrons per fission, $\nu$	Neutrons per absorption, $\eta$
Uranium-233	2.51	2.28
Uranium-235	2.43	2.07
Natural uranium	2.43	1.34
Plutonium-239	2.90	2.10
Plutonium-241	3.06	2.24

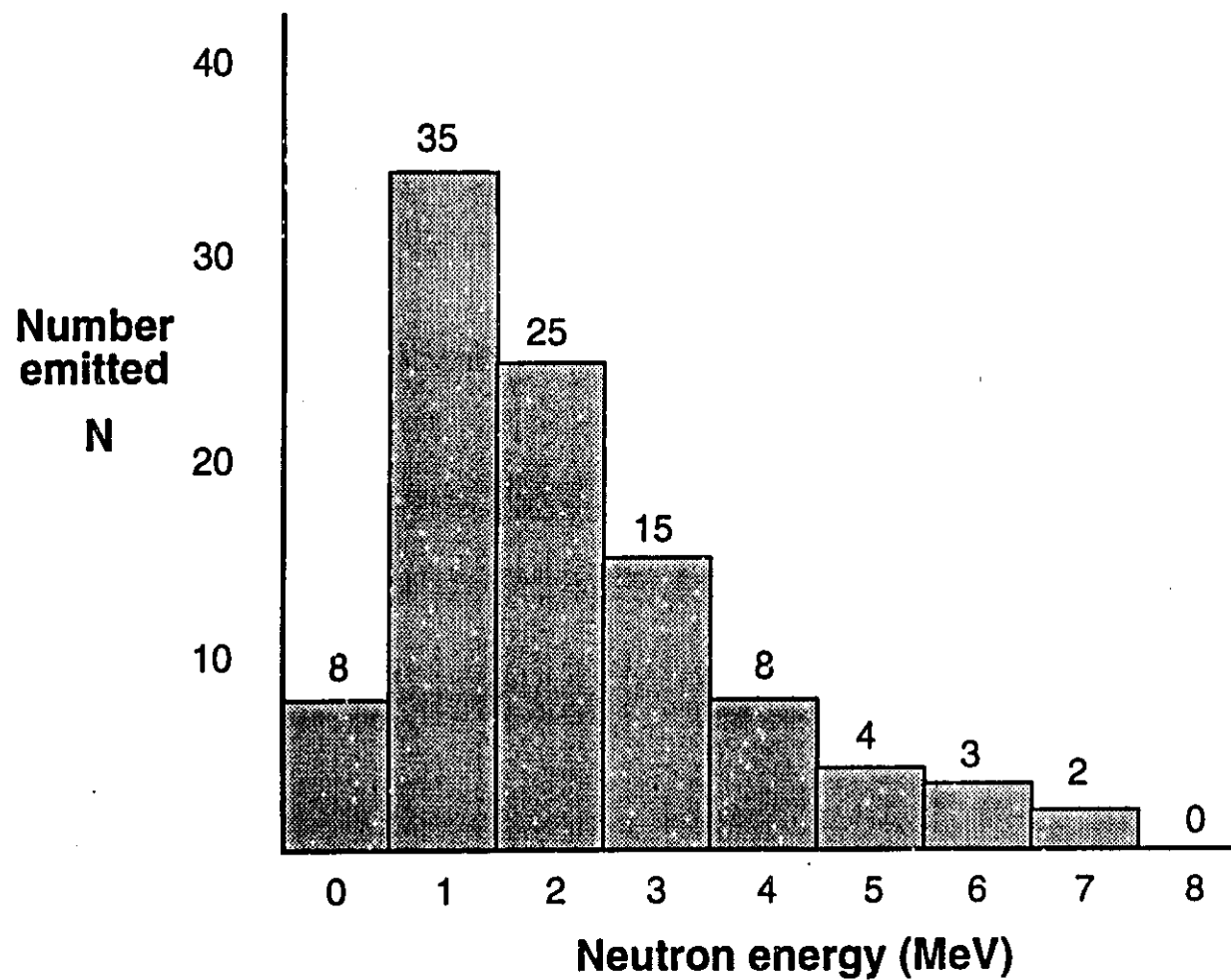


# Reason for Instability of Fission Fragments



# Energy Distribution

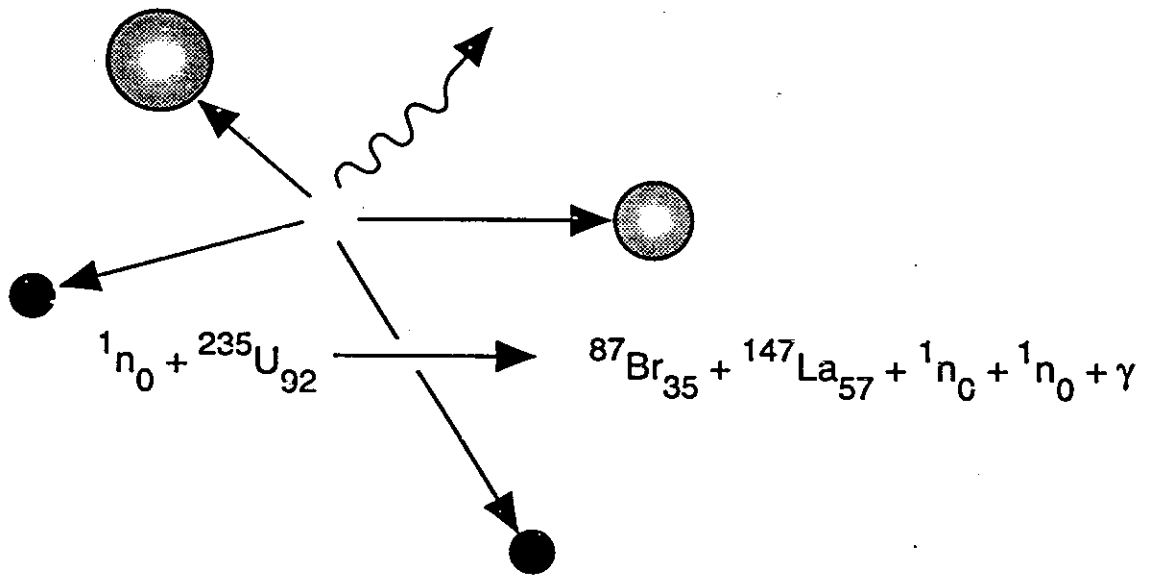
## Sample of 100 Prompt Neutrons



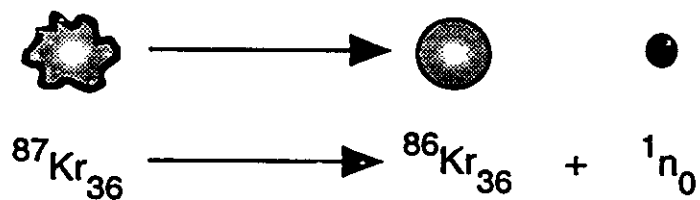
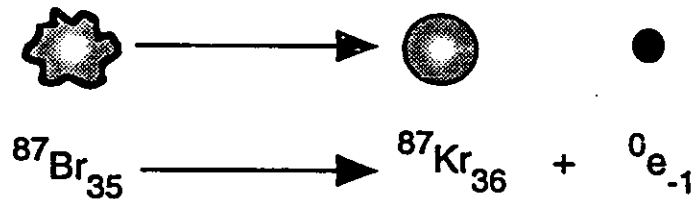
# Delayed Neutrons

Delayed neutrons come from certain nuclei formed by beta decay of fission products

**Fission:**



**Decay:**



## Delayed Neutron Precursor Groups for U-235 Fission

Precursor group	Half-life (seconds)	Relative yield (%)
1	55	4
2	22	21
3	6	19
4	2.2	40
5	0.5	13
6	0.18	3



## Secondary Neutron Emission in Thermal Fission of U-235

Number of neutrons emitted	Number of cases per 1000 fissions
0	27
1	158
2	339
3	302
4	130
5	34

## Value of $\nu$ for Thermal Fissions

Fissile nucleus	$\nu$
U-235	2.43
Pu-239	2.89
Pu-241	2.93

## Approximate Distribution of Fission Energy Release in U-235

Kinetic energy of lighter fission fragment	100 MeV
Kinetic energy of heavier fission fragment	69 MeV
Kinetic energy of secondary neutrons	5 MeV
Energy of prompt $\gamma$ rays	6 MeV
Beta particle energy gradually released from fission products	8 MeV
Gamma ray energy gradually released from fission products	6 MeV
Neutrinos (energy escapes from reactor)	11 MeV
	<b>Total 205 MeV</b>

# Location of Fission Heating

<b>Source</b>	<b>Location of heating</b>
<b>Fission fragments</b>	<b>Fuel pellets (fragments slow down in a distance of about 1<math>\mu</math>m)</b>
<b>Kinetic energy of secondary neutrons</b>	<b>Mostly transferred to moderator by collisions with moderator atoms</b>
<b>Beta particles from fission product decay</b>	<b>Fuel pellets and cladding</b>
<b>Prompt gammas and gammas from fission product decay</b>	<b>Throughout reactor and its shielding (about one third deposited in moderator)</b>

# Fission

## Spontaneous Fission

- Rare but possible

## Induced Fission

- Excited energy level  
must be above critical
- Adding a neutron adds  
energy to the nucleus  
(kinetic & binding energy)

## Fissile Nuclei

- Fission with zero energy neutrons

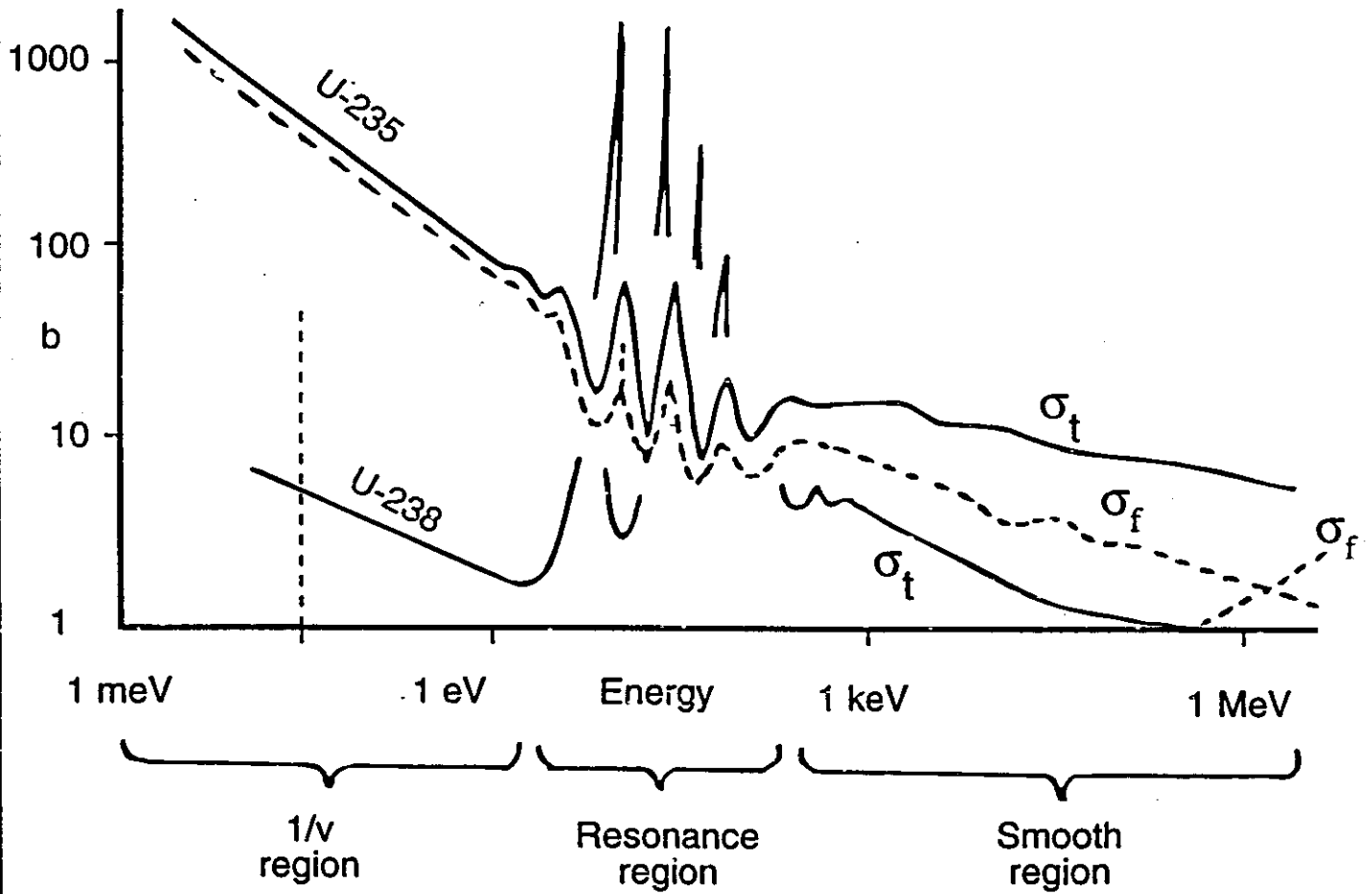
## Fissionable Nuclei

- Fission with energetic (fast) neutrons only

## Fission Process Summary

- \* Critical energy of compound nucleus must be less than binding energy of added neutron
- \* Low energy neutrons interact more readily with U-235 to cause fission than do high energy neutrons. U-238, on the other hand, will only undergo fission with high-energy neutrons.
- \* Neutron/proton ratio curve results in additional neutrons being produced in fission ( $\nu > 1$ )
- \* Neutrons produced in fission have range of energies.  $\bar{E} \approx 2\text{MeV}$ .
- \* Neutrons must be slowed down to lower energies (thermalised or moderated) to start new cycle.

# Fission Characteristics



## Interactions of importance

$$\left. \begin{array}{l} \sigma_s = \text{Scattering} \\ \sigma_\gamma = \text{Radiative capture} \\ \sigma_f = \text{Fission} \end{array} \right\} \sigma_a = \text{Absorption}$$

$$\text{Capture/fission ratio: } \alpha = \sigma_\gamma / \sigma_f$$

$$\text{Probability of fission: } p = \sigma_f / \sigma_a$$

# Avogadro's Number

$$N_A = 6.022 \times 10^{23}$$

Number of atoms or nuclei in a given sample

$$N = \frac{N_A}{A} \times \text{MASS (g)}$$

Example: Atoms in 1kg of U-235

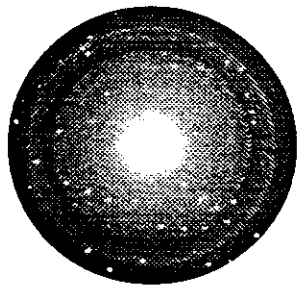
$$\begin{aligned} N &= \frac{6.022 \times 10^{23}}{235} \times 1000 \\ &= 25.62 \times 10^{23} \text{ atoms} \end{aligned}$$

Example: 1kg of U-235 consumed in one day

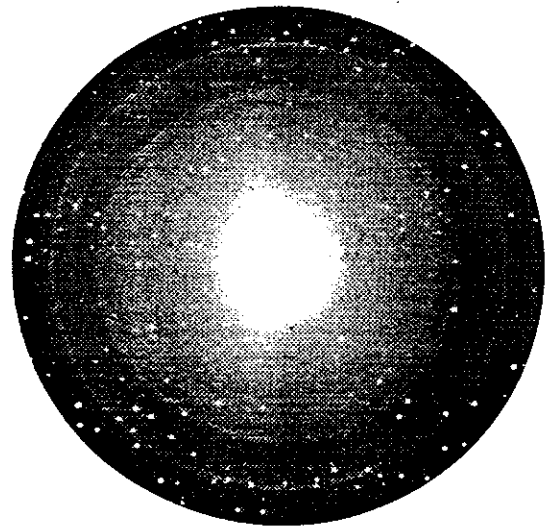
$$\begin{aligned} N &= \frac{6.022 \times 10^{23}}{235} \times 1000 \text{ fission/day} \\ &= 25.62 \times 10^{23} \text{ atoms} / (24 \times 3600) \text{ Fissions/s} \\ &= 0.0002965 \times 10^{23} \times 200 \text{ MeV/s} \\ &= 0.05932 \times 10^{23} \times 1.6022 \times 10^{-13} \text{ J/s} \\ &= 0.09504 \times 10^{10} \text{ W} \\ &= 950 \times 10^6 \text{ W} \\ &= 950 \text{ MW} \end{aligned}$$



# Cross-Sections for U-238



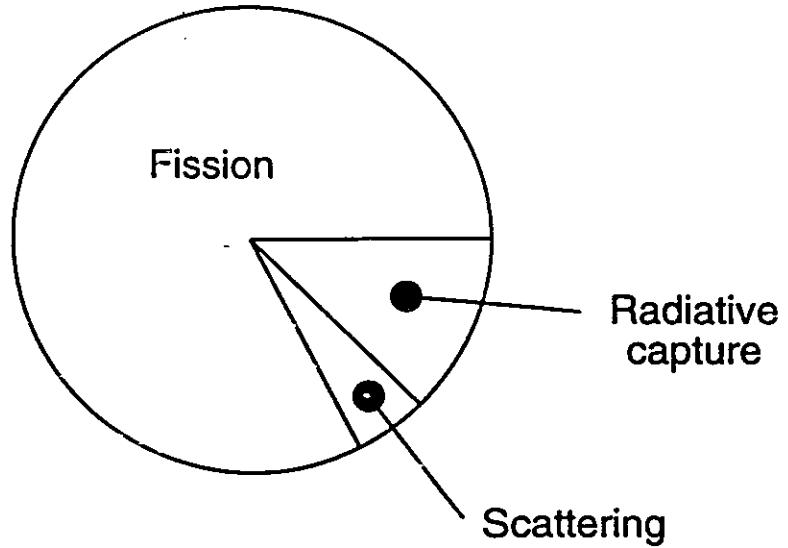
**Radiative capture  
Cross-section of U-238**



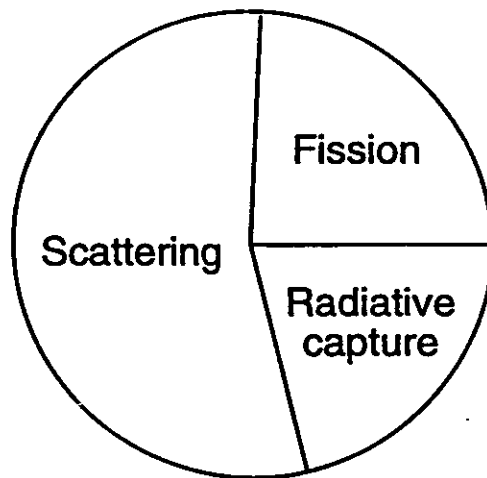
**Elastic scattering  
Cross-section of U-238**

# Pie Diagram for Cross-Sections of U-235 and Nat-U

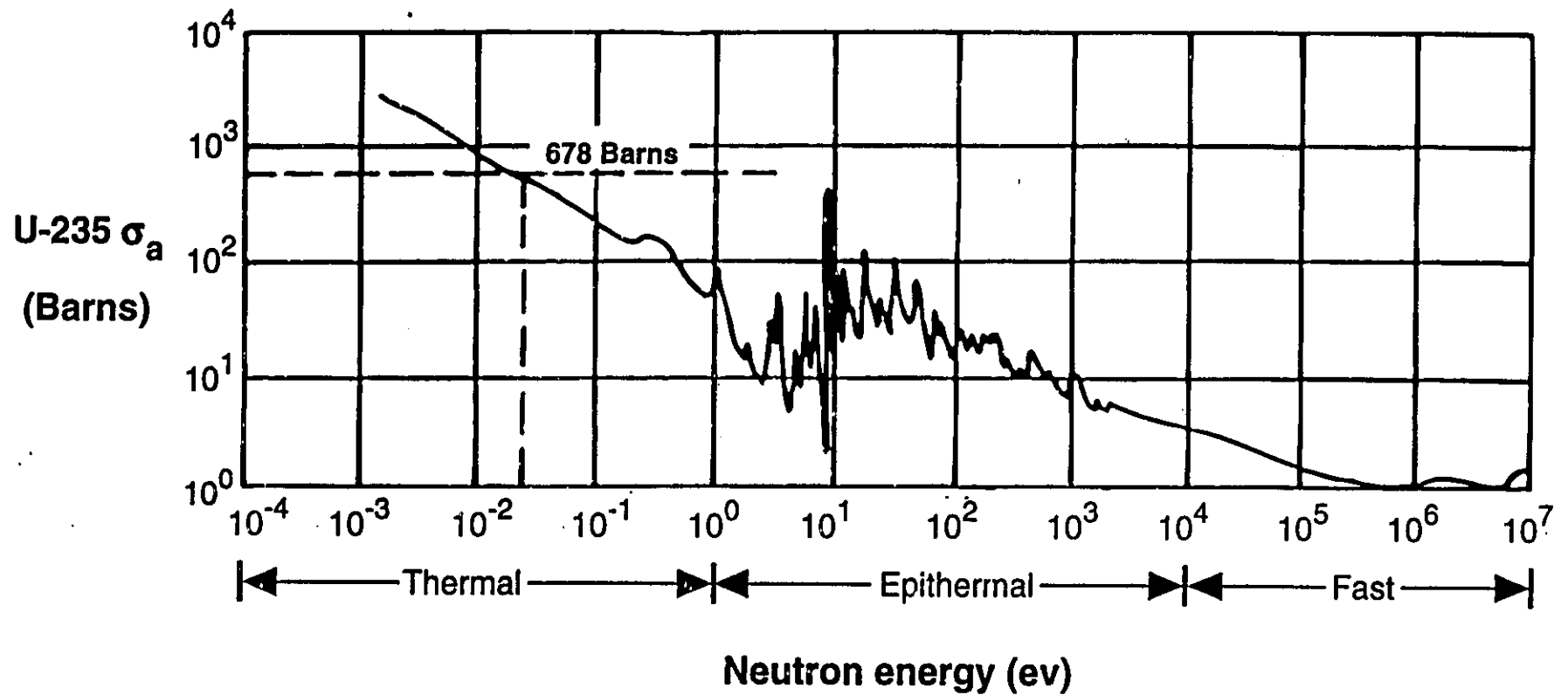
U-235



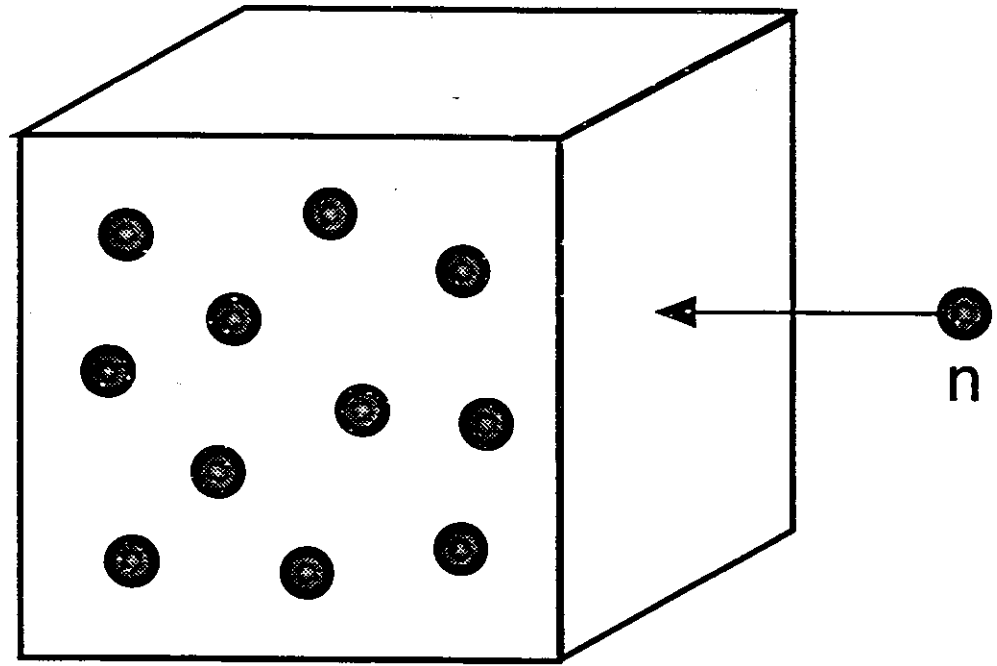
Nat-U



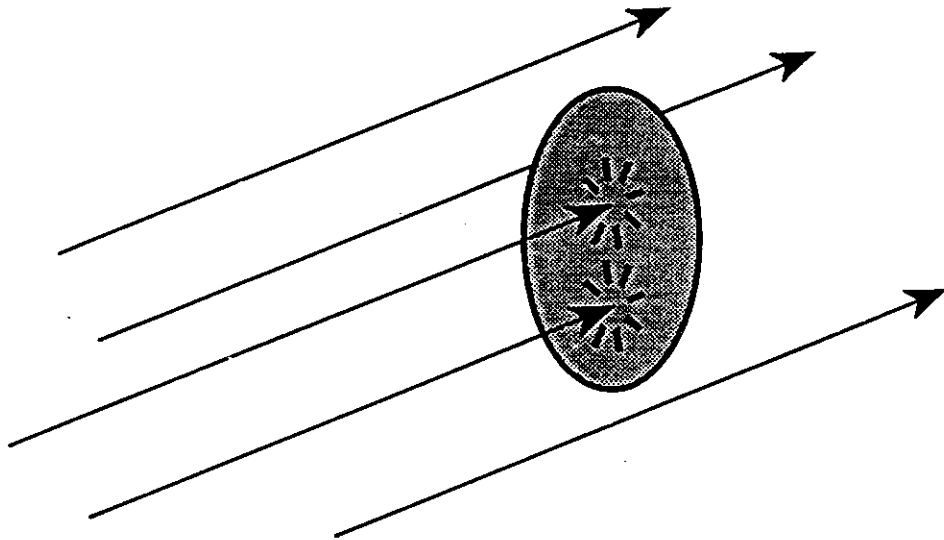
# Variation of Absorption Cross-Section of U-235 with Neutron Energy



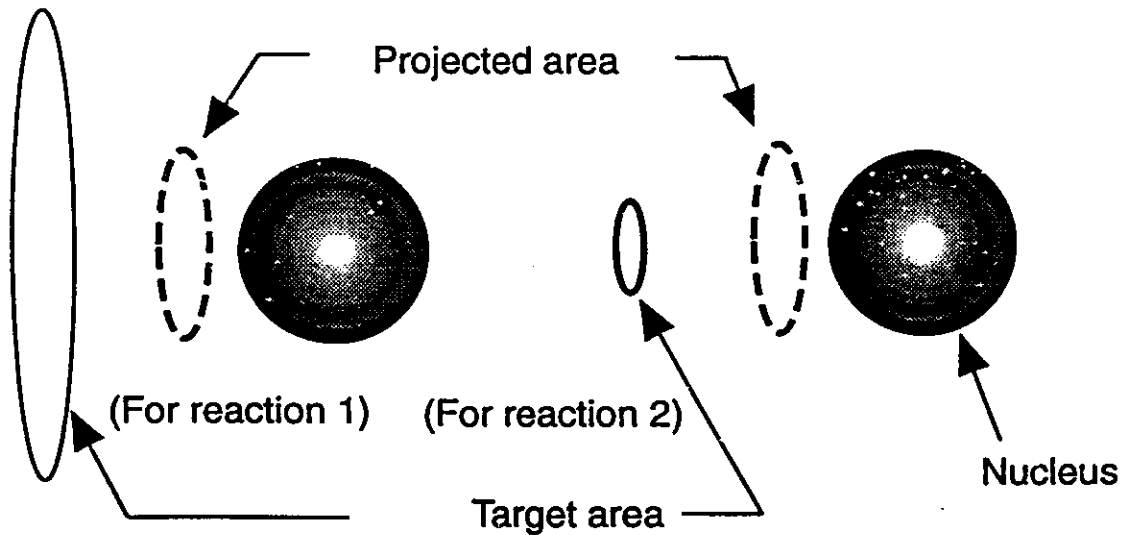
# Concept of Cross-Section



# Target Areas

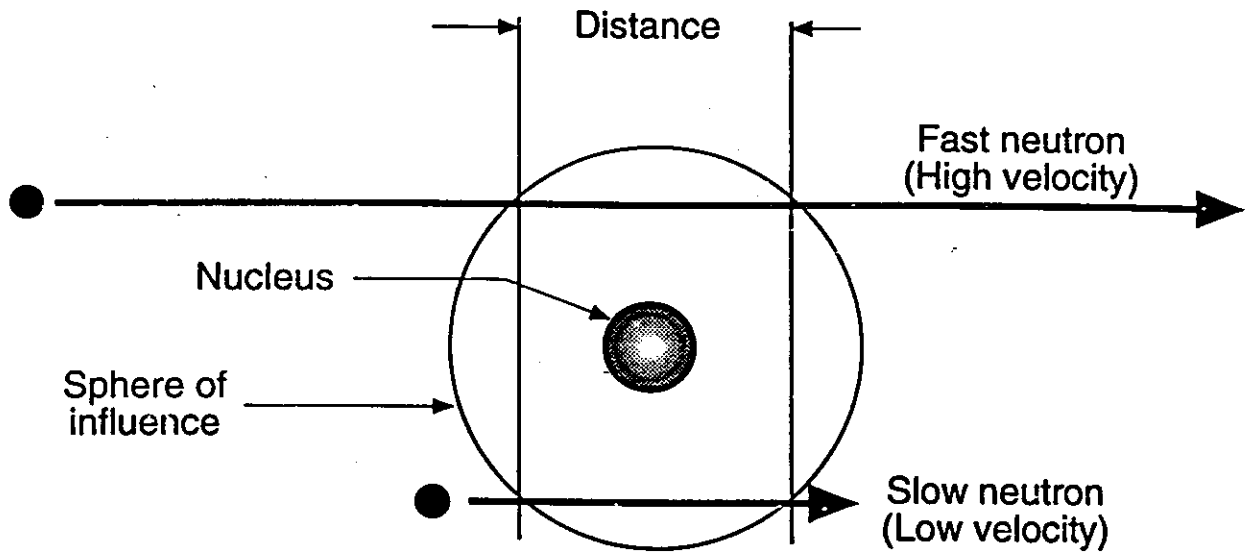


Target area may be smaller or larger than projected (physical) area of nucleus



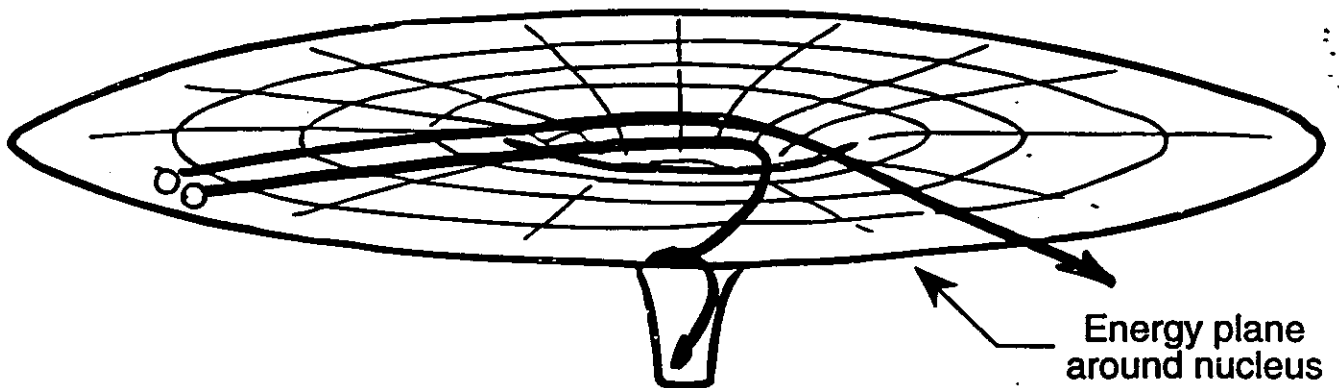
Target areas are different for different nuclear reactions

# Interaction Models



Time to react with nucleus = distance/velocity

## Time Model



Low velocity gives greater chance of capture

## Energy Model

## Comparison of Cross-Sections for Thermal Neutrons

Element	Nucleus radius $r = 1.2 \times 10^{-15} A^{1/3}$ (m)	Nucleus radius (cm)	Nucleus area $A = \pi r^2$ (cm <sup>2</sup> )	Cross section $\sigma_a$ (cm <sup>2</sup> )	Cross section $\sigma_s$ (cm <sup>2</sup> )
H	$0.0012 \times 10^{-12}$	$0.12 \times 10^{-12}$	$0.045 \times 10^{-24}$	$0.332 \times 10^{-24}$	$38 \times 10^{-24}$
B	$0.0026 \times 10^{-12}$	$0.26 \times 10^{-12}$	$0.212 \times 10^{-24}$	$759 \times 10^{-24}$	$3.6 \times 10^{-12}$
C	$0.0027 \times 10^{-12}$	$0.27 \times 10^{-12}$	$0.229 \times 10^{-24}$	$0.0034 \times 10^{-24}$	$4.75 \times 10^{-24}$
O	$0.0030 \times 10^{-12}$	$0.30 \times 10^{-12}$	$0.283 \times 10^{-24}$	$0.00027 \times 10^{-24}$	$3.76 \times 10^{-24}$
Pb	$0.0071 \times 10^{-12}$	$0.71 \times 10^{-12}$	$1.584 \times 10^{-24}$	$0.17 \times 10^{-24}$	$11.4 \times 10^{-24}$
U	$0.0074 \times 10^{-12}$	$0.74 \times 10^{-12}$	$1.720 \times 10^{-24}$	$7.53 \times 10^{-24}$	$8.9 \times 10^{-24}$
U-235	$0.0074 \times 10^{-12}$	$0.74 \times 10^{-12}$	$1.720 \times 10^{-24}$	$99 \times 10^{-24}$ (n, $\gamma$ )  $582 \times 10^{-24}$ (n,f)	

Note that projected area of nucleus is about  $1 \times 10^{-24}$  cm = 1 Barn

# Cross-Section Nomenclature

$\sigma_f$  = Fission cross section

$\sigma_a$  = Absorption cross section

$\sigma_{n,\gamma}$  = Radiative capture cross section

$\sigma_i$  = Inelastic scattering cross section

$\sigma_s$  = Elastic scattering cross section

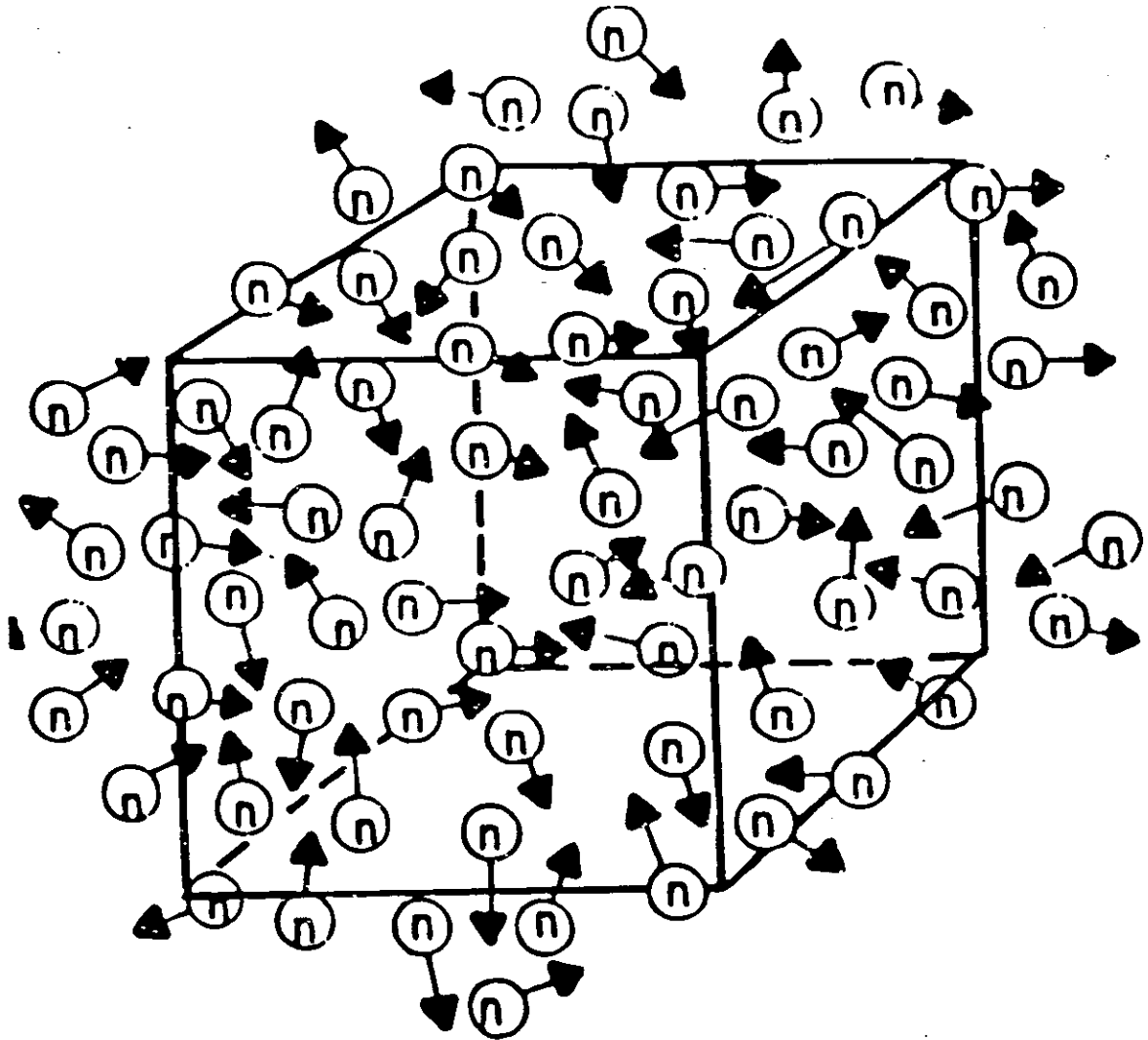


# Thermal Neutron Cross-Sections of Fuel Atoms (in Barns)

*Taken from Atomic Energy Review (IAEA), 1969, Vol 7, No 4, p.3*

	$\sigma_f$	$\sigma_{n,\gamma}$	$\sigma_a$	$\sigma_s$	$\nu$	$\sigma_f/\sigma_a$ (%)
<b>U-233</b>	530.6	47.0	577.6	10.7	2.487	92
<b>U-235</b>	580.2	98.3	678.5	17.6	2.430	86
<b>U-238</b>	0	2.71	2.71	~ 10	0	
<b>Nat. U</b>	4.18	3.40	7.58	~ 10		55
<b>Pu-239</b>	741.6	271.3	1012.9	8.5	2.890	73
<b>Pu-241</b>	1007.3	368.1	1375.4	12.0	2.934	73

# Neutron Reaction Rates



# Neutron Flux

Neutron flux  $\phi$  is defined as the number of neutrons  $n$  multiplied by their velocity  $v$

$$\phi = nv \quad \frac{\text{number}}{\text{cm}^3} \times \frac{\text{cm}}{\text{s}} = \frac{\text{number}}{\text{cm}^2 \text{ s}}$$

Since neutron flux  $\phi$  has units of  $\text{cm}^{-2}\text{s}^{-1}$  it can be considered as the number of neutrons passing through a particular cross sectional area per unit time

# Definitions

## Macroscopic cross-section

(Cross-section density in material)

$$\Sigma = N\sigma$$

$$\left( \frac{1}{\text{cm}} \right) \text{ or } \left( \text{cm}^{-1} \right)$$

$N$  = Nuclei per unit volume

$$\left( \frac{\text{nuclei}}{\text{cm}^3} \right)$$

$\sigma$  = Microscopic cross-section

$$\left( \text{cm}^2 \right)$$

## Neutron flux

(Neutrons passing through given area per second)

$$\phi = nv$$

$$\left( \frac{\text{neutrons}}{\text{cm}^2 \text{ s}} \right)$$

$n$  = Neutrons per unit volume

$$\left( \frac{\text{neutrons}}{\text{cm}^3} \right)$$

$v$  = Neutron velocity

$$\left( \frac{\text{cm}}{\text{s}} \right)$$

## Reaction rate

(Reaction rate of neutrons with material)

$$R = \phi\Sigma$$

$$\left( \frac{\text{reactions}}{\text{cm}^3 \text{ s}} \right)$$

$\phi$  = Neutron flux

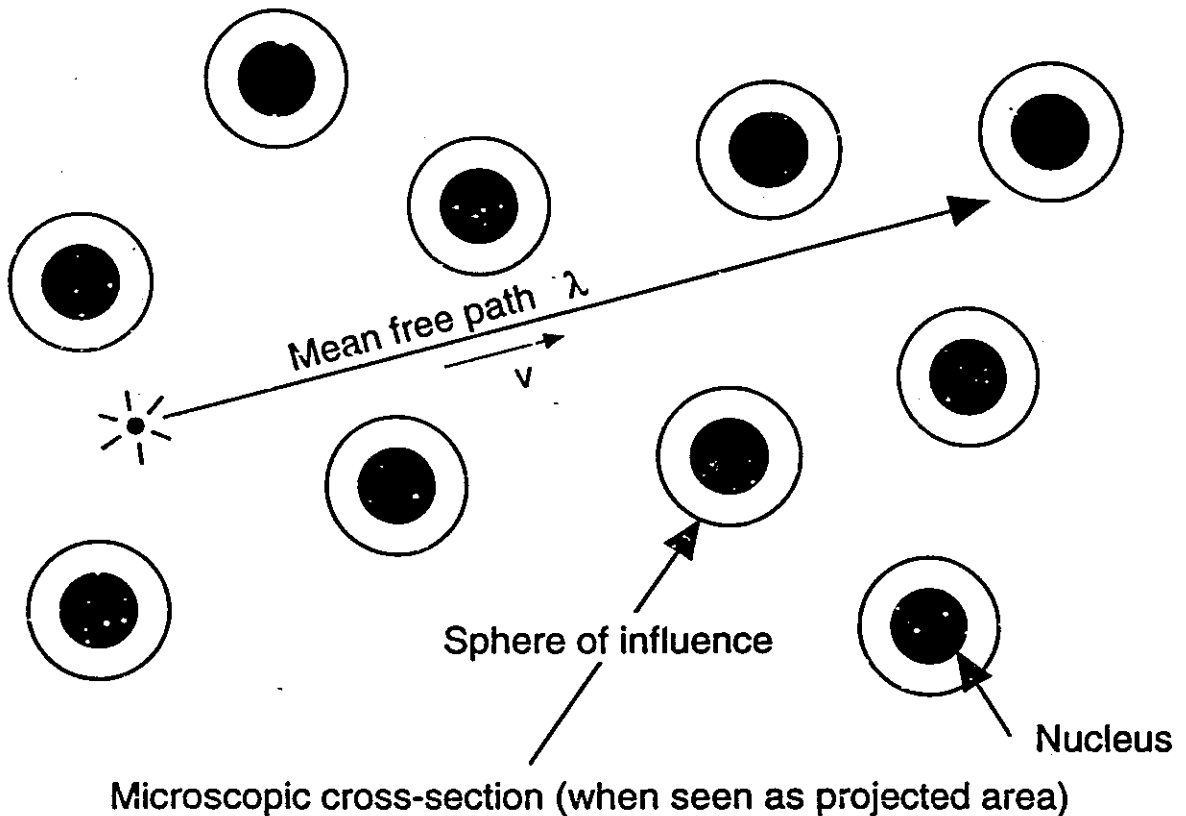
$$\left( \frac{\text{neutrons}}{\text{cm}^2 \text{ s}} \right)$$

$\Sigma$  = Macroscopic cross-section

$$\left( \frac{1}{\text{cm}} \right)$$

# Neutron Mean Free Path

Macroscopic cross-section gives density of microscopic cross-sections of atoms in material



$$R = \Sigma \phi = \Sigma n v \text{ ----- (1)}$$

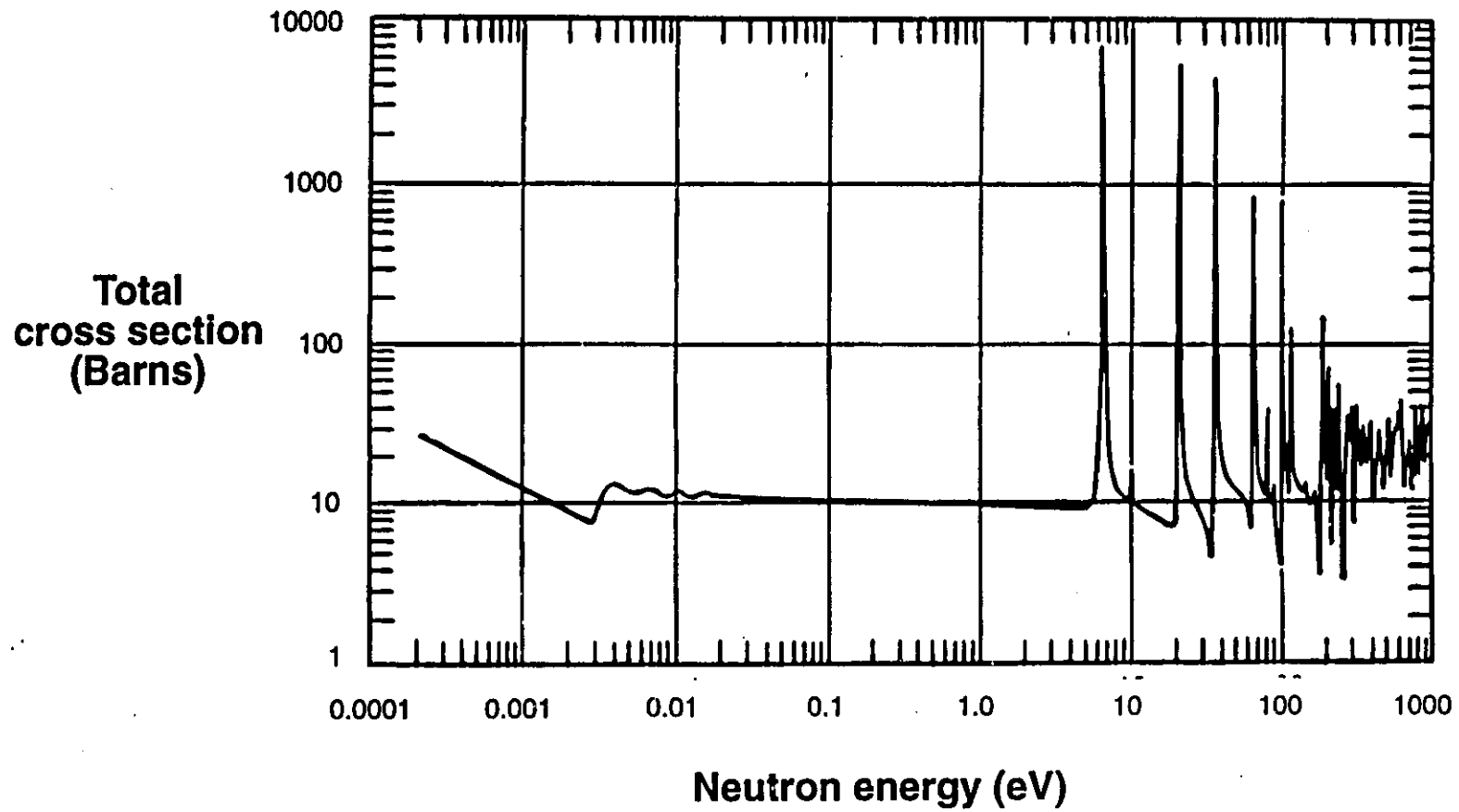
But  $R = \text{Number of neutrons} \times \frac{\text{Distance}}{\text{Second}} \times \frac{1}{\text{Mean distance}}$

$$R = \frac{n v}{\lambda} \text{ ----- (2)}$$

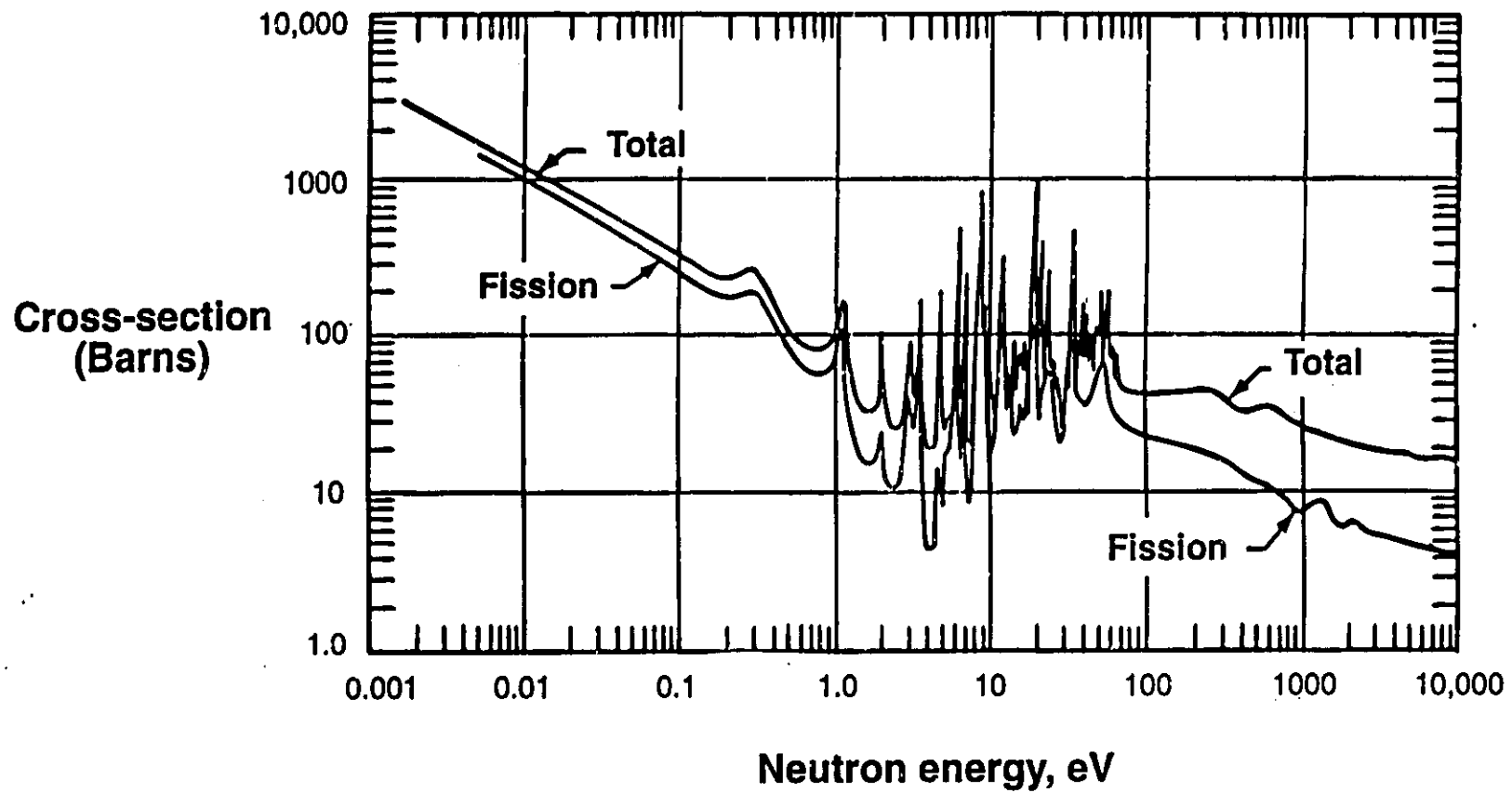
From (1) And (2)

$$\lambda = \frac{1}{\Sigma} \text{ cm}$$

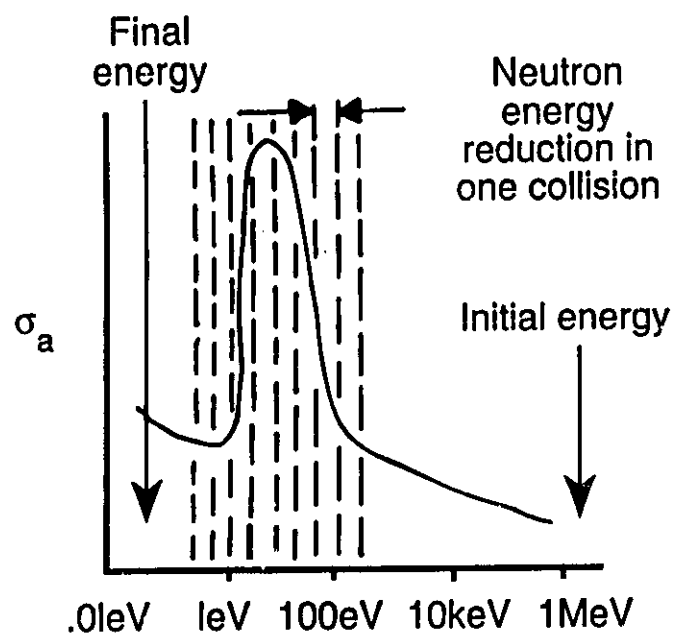
# Total Cross-Section of U-238



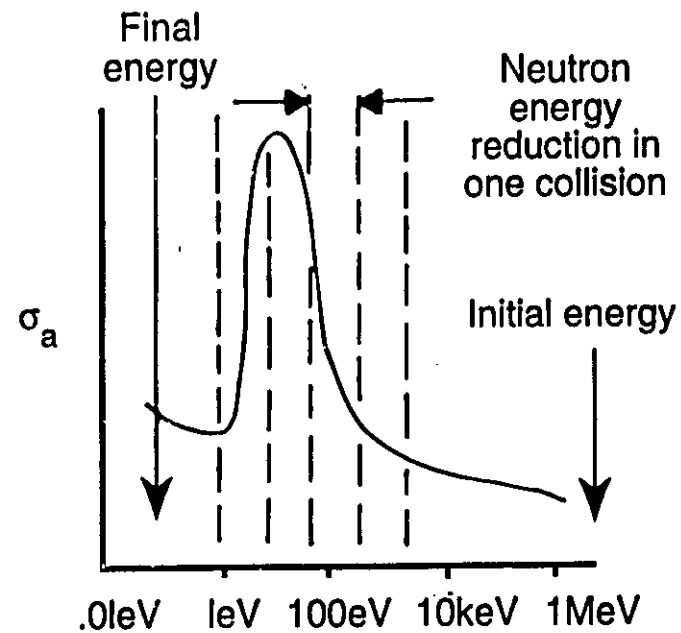
# Cross-Sections of U-235



# The Fraction of the Neutron's Energy that is Lost Per Collision is Small on the Left and Large on the Right



**Moderator 1**



**Moderator 2**



# Change of Multiplication Factor with Moderator Isotopic (PLNGS)

