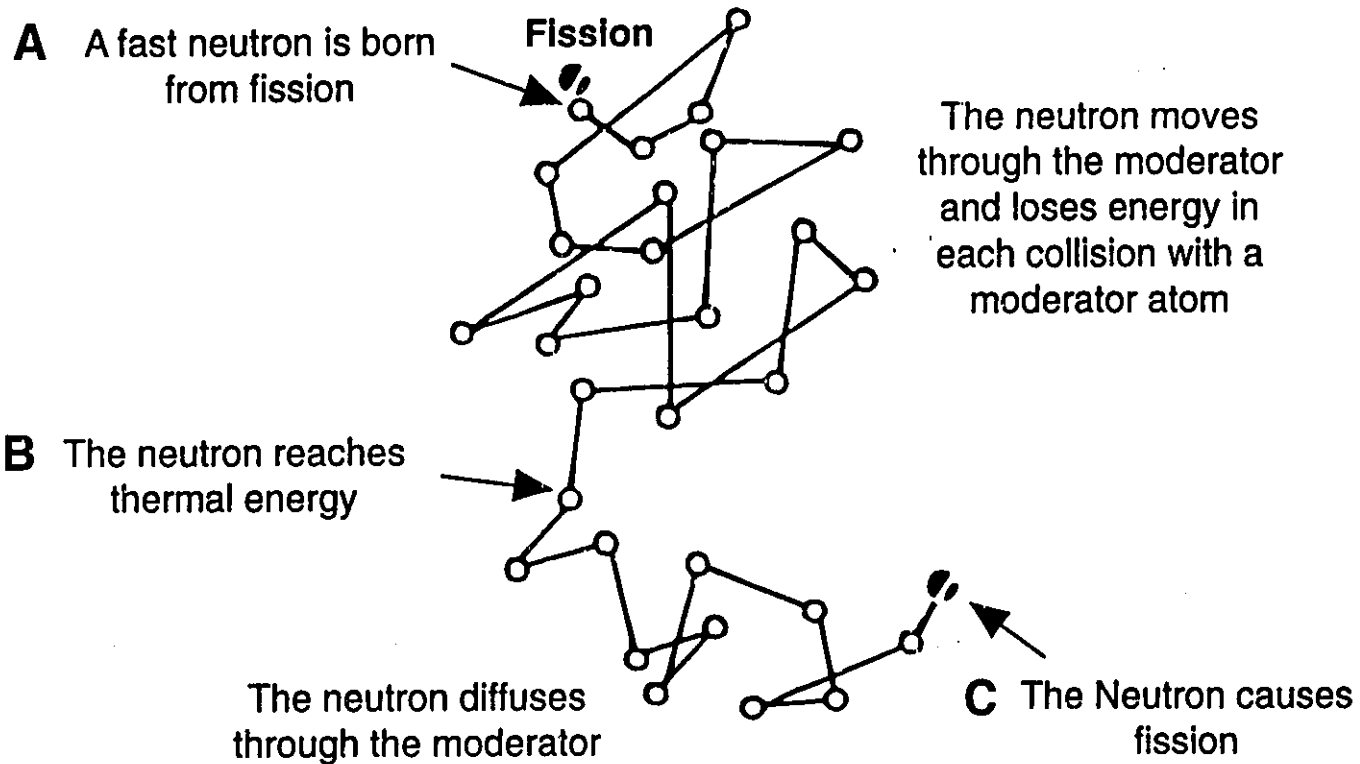
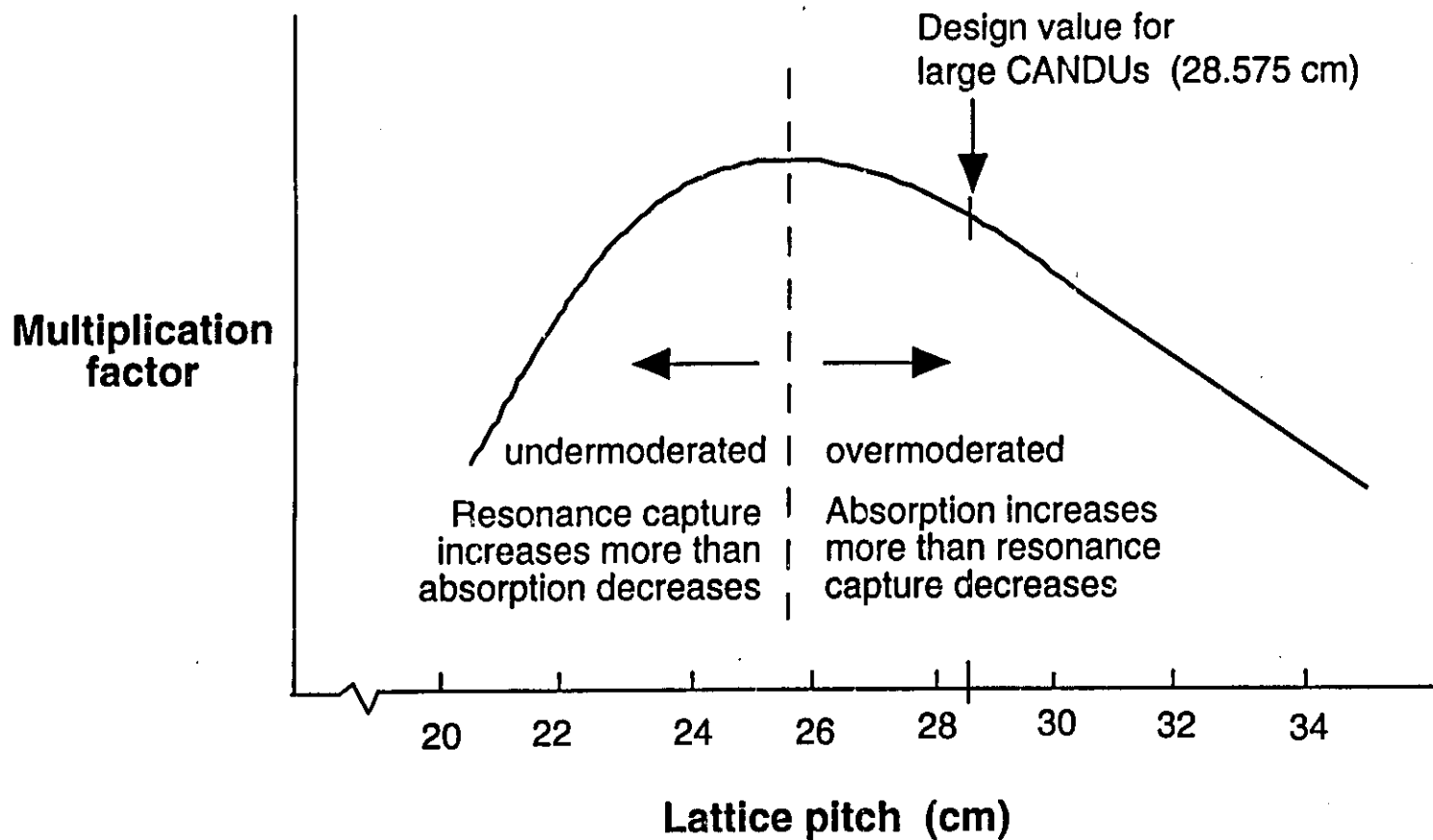


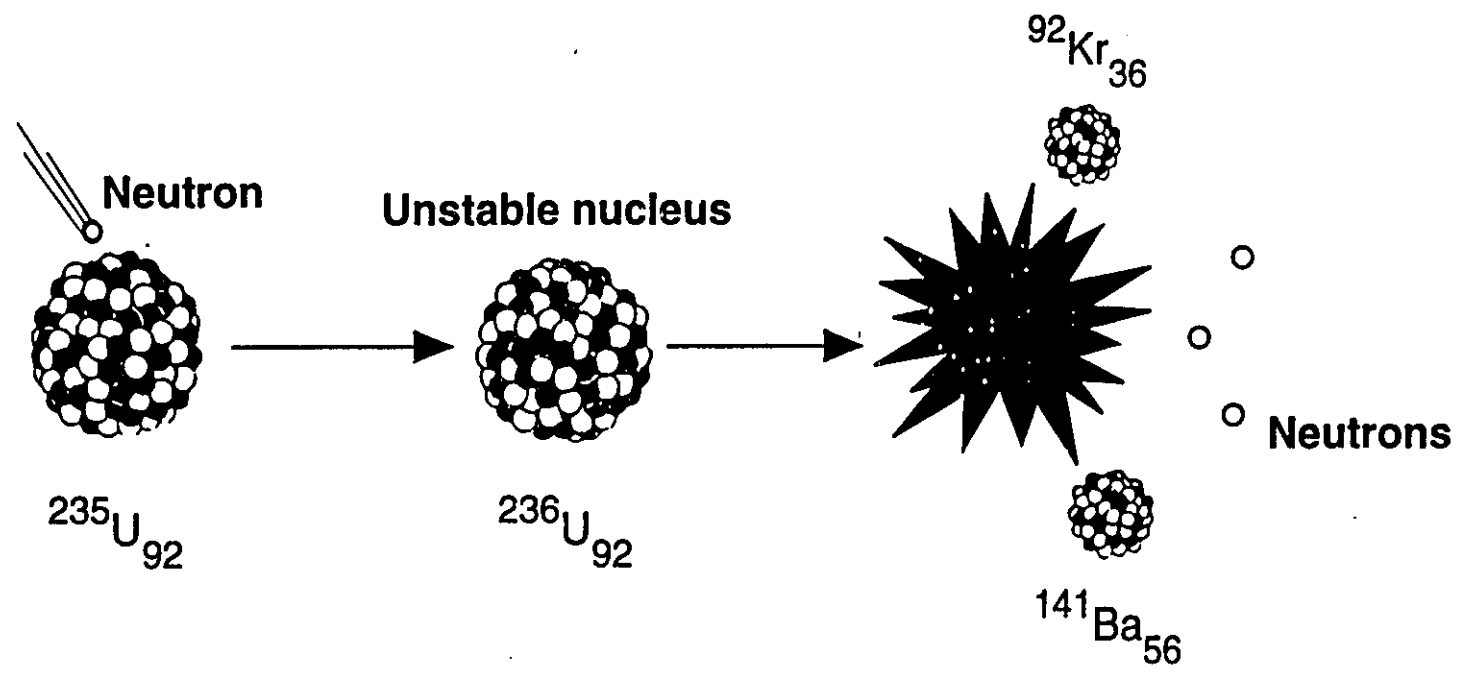
# Path of a Neutron from Birth to Absorption



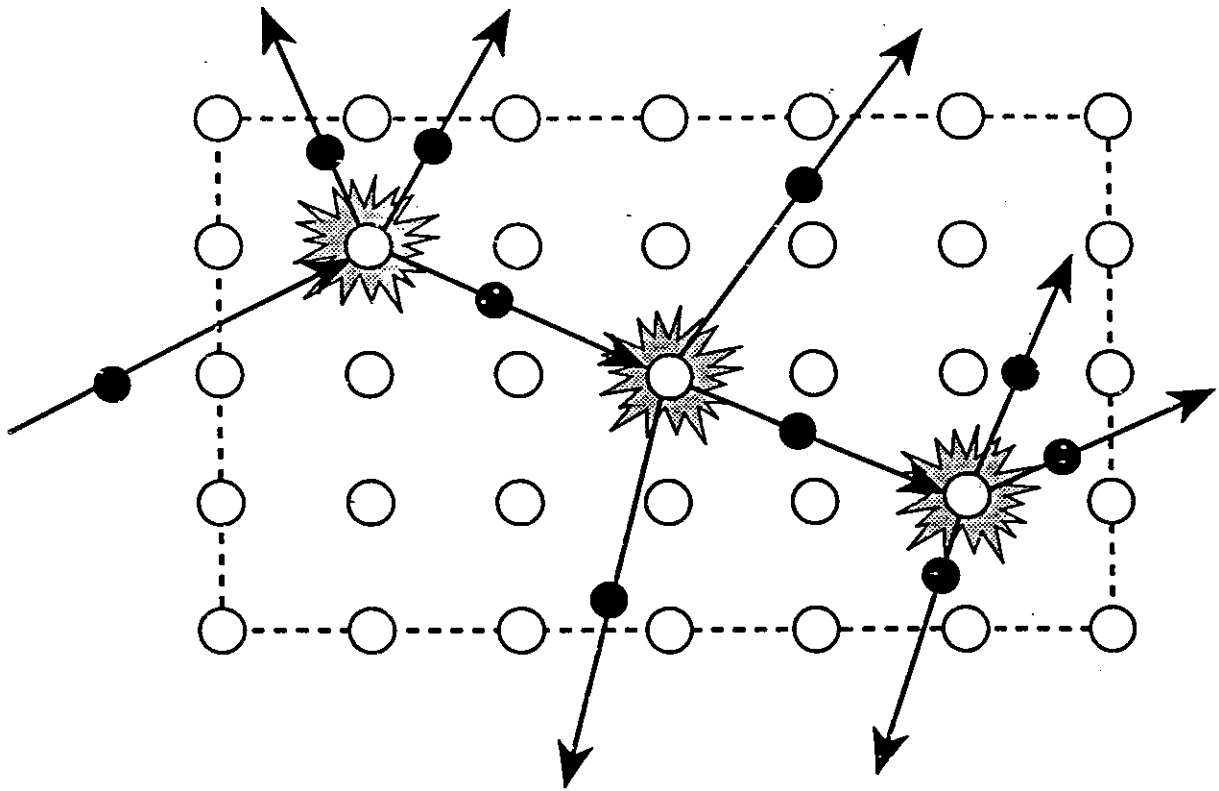
# Variation of k with Pitch of Lattice



# Fission Process



# Fission Chain Reaction



# Log Mean Energy Decrement

## Logarithmic mean energy decrement

$$\begin{aligned}\xi &= \overline{\ln E_0 - \ln E} \\ &= \overline{\ln (E_0 / E)} \\ &= \overline{-\ln (E / E_0)}\end{aligned}$$

Value of  $\xi$  is given by

$$\xi = 1 + \frac{(A-1)^2}{2A} \ln \frac{(A-1)}{(A+1)}$$

Approximate value of  $\xi$  are given by

$$\xi = \frac{2}{A + 2/3}$$

$\xi$  is Greek letter Xi

## Mean Logarithmic Energy Decrements

| Material                    | $\xi$ | Collisions to<br>thermalize |
|-----------------------------|-------|-----------------------------|
| H <sup>1*</sup>             | 1.000 | 18                          |
| H <sub>2</sub> <sup>+</sup> | 0.725 | 25                          |
| He <sup>4*</sup>            | 0.425 | 43                          |
| Be <sup>9</sup>             | 0.206 | 83                          |
| C <sup>12</sup>             | 0.158 | 115                         |
| H <sub>2</sub> O            | 0.927 | 20                          |
| D <sub>2</sub> O            | 0.510 | 36                          |
| BeO                         | 0.174 | 105                         |

## Slowing Down Powers and Moderating Ratios

|                   | $\xi$ | $\Sigma_s(\text{cm}^{-1})(a)$ | $\xi\Sigma_s$      | $\Sigma_a$               | $\xi\Sigma_a/\Sigma_a$ |
|-------------------|-------|-------------------------------|--------------------|--------------------------|------------------------|
| He <sup>(b)</sup> | 0.425 | $2 \times 10^{-6}$            | $9 \times 10^{-6}$ | ? very small             | ? large                |
| Be                | 0.206 | 0.74                          | 0.15               | $1.17 \times 10^{-3}$    | 130                    |
| H <sup>(c)</sup>  | 0.158 | 0.38                          | 0.06               | $0.38 \times 10^{-3}$    | 160                    |
| BeO               | 0.174 | 0.69                          | 0.12               | $0.68 \times 10^{-3}$    | 180                    |
| H <sub>2</sub> O  | 0.927 | 1.47                          | 1.36               | $22 \times 10^{-3}$      | 60                     |
| D <sub>2</sub> O  | 0.510 | 0.35                          | 0.18               | $0.33 \times 10^{-4}(d)$ | 5500(d)                |
| D <sub>2</sub> O  | 0.510 | 0.35                          | 0.18               | $0.88 \times 10^{-4}(e)$ | 2047(e)                |
| D <sub>2</sub> O  | 0.510 | 0.35                          | 0.18               | $2.53 \times 10^{-4}(f)$ | 712(f)                 |

# Definitions

## Logarithmic mean energy decrement $\xi$

$$N \xi = \text{Ln} \frac{E_i}{E_f}$$

$$N = \text{Number of Collisions}$$

$$E_i = \text{Initial energy (2 MeV)}$$

$$E_f = \text{Final Energy (0.025 eV)}$$

## Macroscopic scattering cross-section $\Sigma_s$

$$\Sigma_s = N\sigma_s$$

$$N = \text{Nuclei per unit volume}$$

$$\sigma = \text{Microscopic cross-section}$$

## Slowing down power

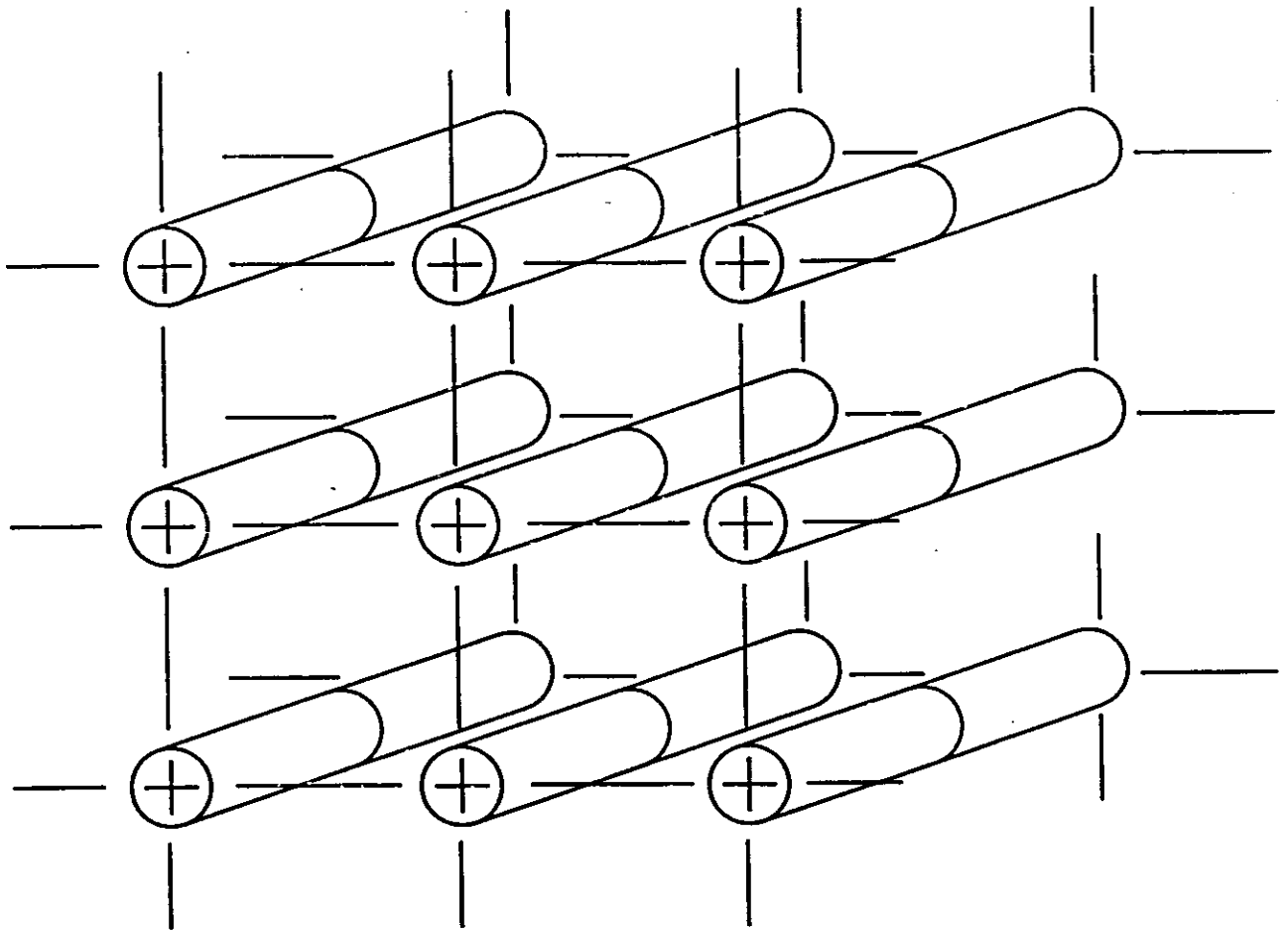
$$= \xi \Sigma_s$$

## Moderating ratio

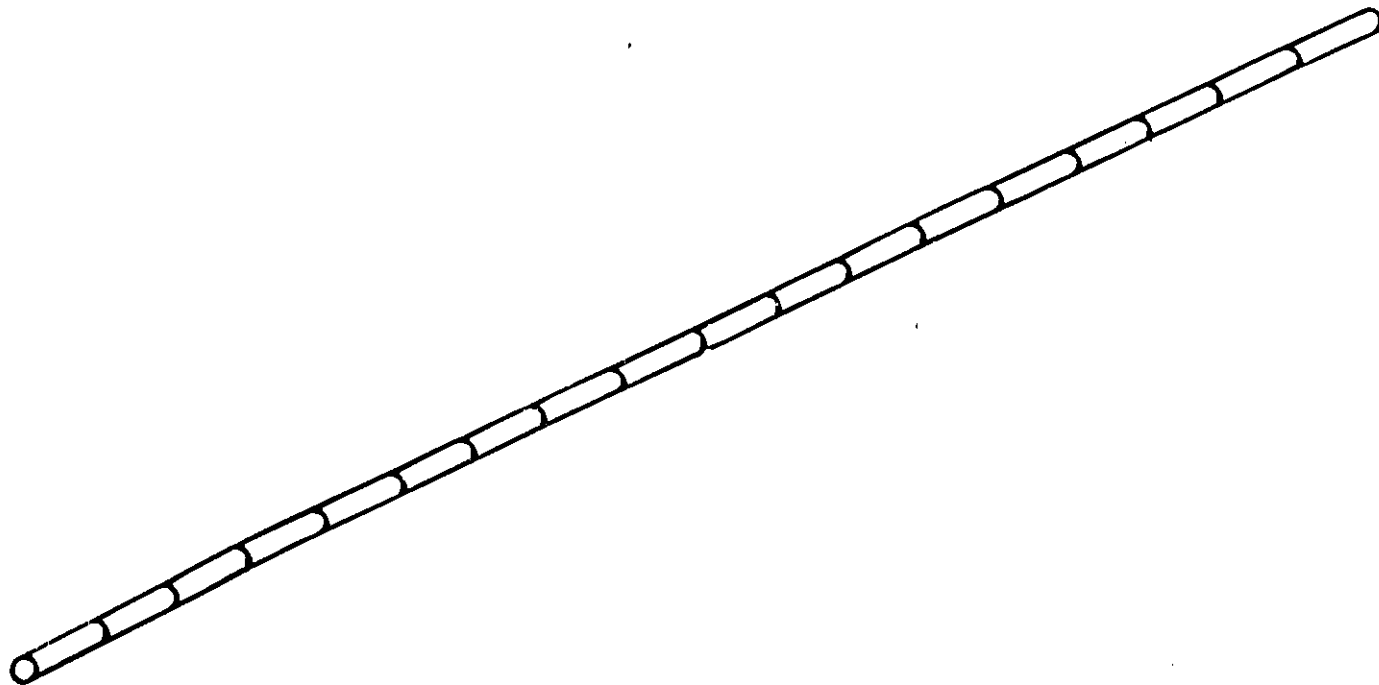
$$= \frac{\xi \Sigma_s}{\Sigma_a}$$



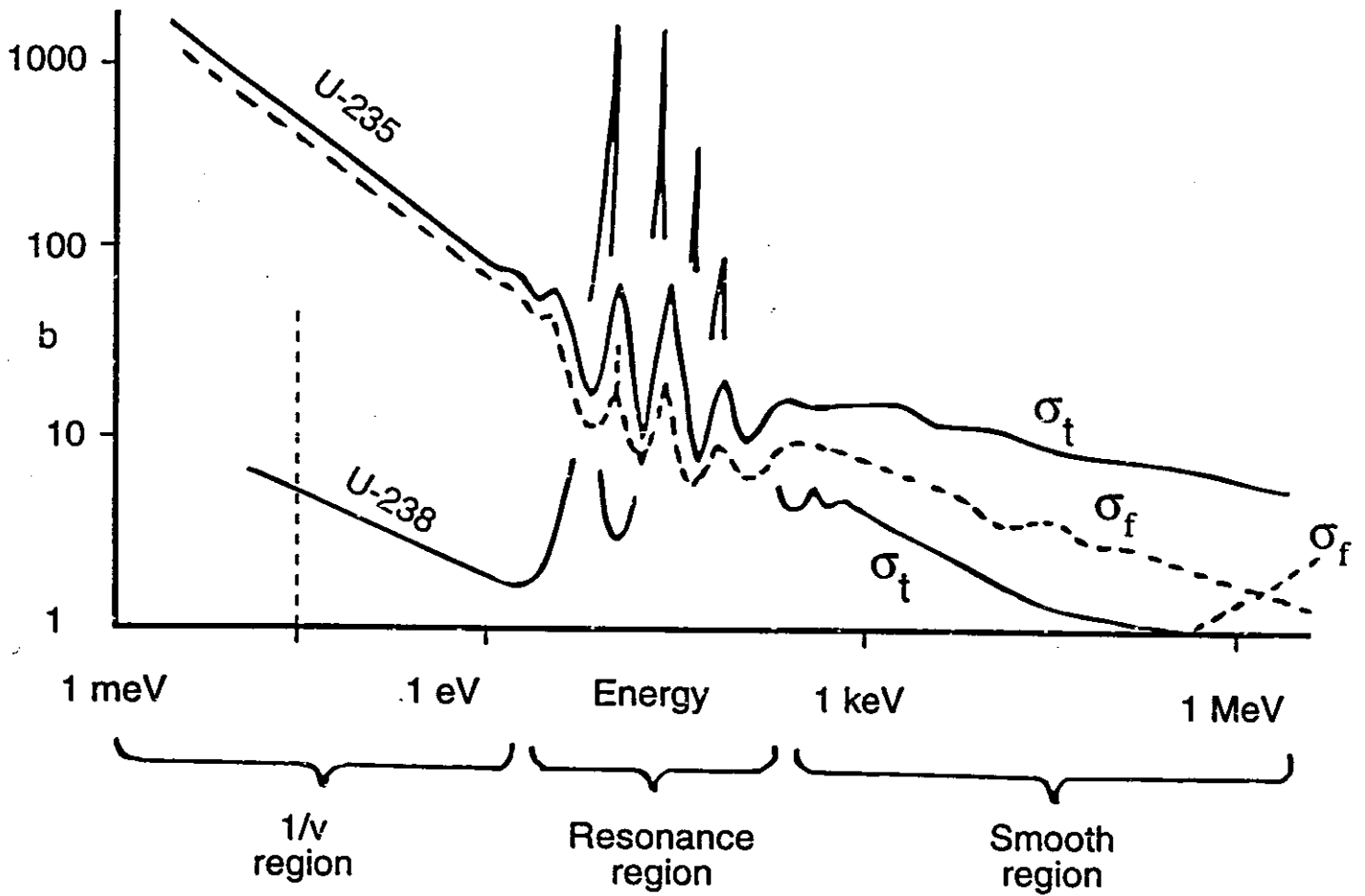
# Critical Assembly of 18 Bundles in D<sub>2</sub>O



## Bundles Arranged in Single Line



# Fission Characteristics



## Interactions of importance

$$\left. \begin{array}{l} \sigma_s = \text{Scattering} \\ \sigma_\gamma = \text{Radiative capture} \\ \sigma_f = \text{Fission} \end{array} \right\} \sigma_a = \text{Absorption}$$

$$\text{Capture/fission ratio: } \alpha = \sigma_\gamma / \sigma_f$$

$$\text{Probability of fission: } p = \sigma_f / \sigma_a$$

# Neutron Multiplication Factor

## Neutron multiplication factor

|              |   |   |            |
|--------------|---|---|------------|
| $k_{\infty}$ | = | $\epsilon p \eta f$                                   | (4 Factor) |
| $k$          | = | $\epsilon p \eta f \Lambda_f \Lambda_t$               | (6 Factor) |
| $\epsilon$   | = | Fast fission factor                                   |            |
| $p$          | = | Resonance escape probability                          |            |
| $\eta$       | = | Reproduction factor                                   |            |
|              | = | $\nu \Sigma_f^{\text{FUEL}} / \Sigma_t^{\text{FUEL}}$ |            |
| $\nu$        | = | Neutrons per fission                                  |            |
| $f$          | = | Thermal utilization factor                            |            |
|              | = | $\Sigma_a^{\text{FUEL}} / \Sigma_a^{\text{REACTOR}}$  |            |
| $\Lambda_f$  | = | Fast neutron non-leakage probability                  |            |
| $\Lambda_t$  | = | Slow neutron non-leakage probability                  |            |

## For reactor of finite size

|              |   |  |  |
|--------------|---|--|--|
| $k$          | = | $k_{\infty} \Lambda_f \Lambda_t$       |  |
| $k_{\infty}$ | = | $k$ value for infinitely large reactor |  |

# Sphere

**Volume:**  $\frac{\pi}{6} D^3$

**Surface:**  $\pi D^2$

**Surface/ volume ratio:**  $\pi D^2 / \frac{\pi}{6} D^3$   
 $= 6/D$

if  $D = 1$       Ratio = 6

if  $D = 2$       Ratio = 3

if  $D = 3$       Ratio = 2

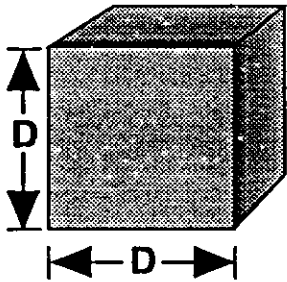
if  $D = 4$       Ratio = 1.5

if  $D = 5$       Ratio = 1.2

if  $D = 6$       Ratio = 1

# Surface-Volume Ratio

## Cube of side D volume 100



$$\text{Surface} = 6D^2$$

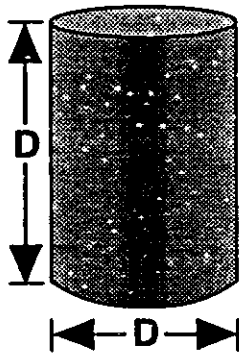
$$\text{Volume} = D^3$$

$$D^3 = 100 \therefore D = 4.64$$

$$S = 6(4.64)^2 = 129$$

$$\text{S:V Ratio} = 129/100 = 1.29$$

## Cylinder of length D, diameter D, volume 100



$$\text{Surface} = 2 \frac{\pi}{4} D^2 + \pi D(D) = \frac{3}{2} D^2$$

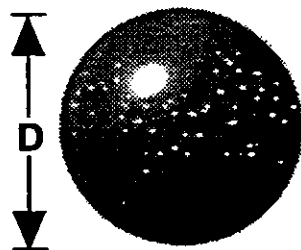
$$\text{Volume} = \frac{\pi}{4} D^2 D = \frac{\pi}{4} D^3$$

$$D^3 = 100 \left( \frac{\pi}{4} \right) \therefore D = 5.03$$

$$S = \frac{3}{2} \pi (5.03)^2 = 119$$

$$\text{S:V Ratio} = 119/100 = 1.19$$

## Sphere of diameter D, volume 100



$$\text{Surface} = \pi D^2$$

$$\text{Volume} = \frac{\pi}{6} D^3$$

$$D^3 = 100 \left( \frac{6}{\pi} \right) \therefore D = 5.76$$

$$S = \pi (5.76)^2 = 104$$

$$\text{S:V Ratio} = 104/100 = 1.04$$

# Variation of the Thermal Neutron Flux along the Axis of a Cylindrical Reactor

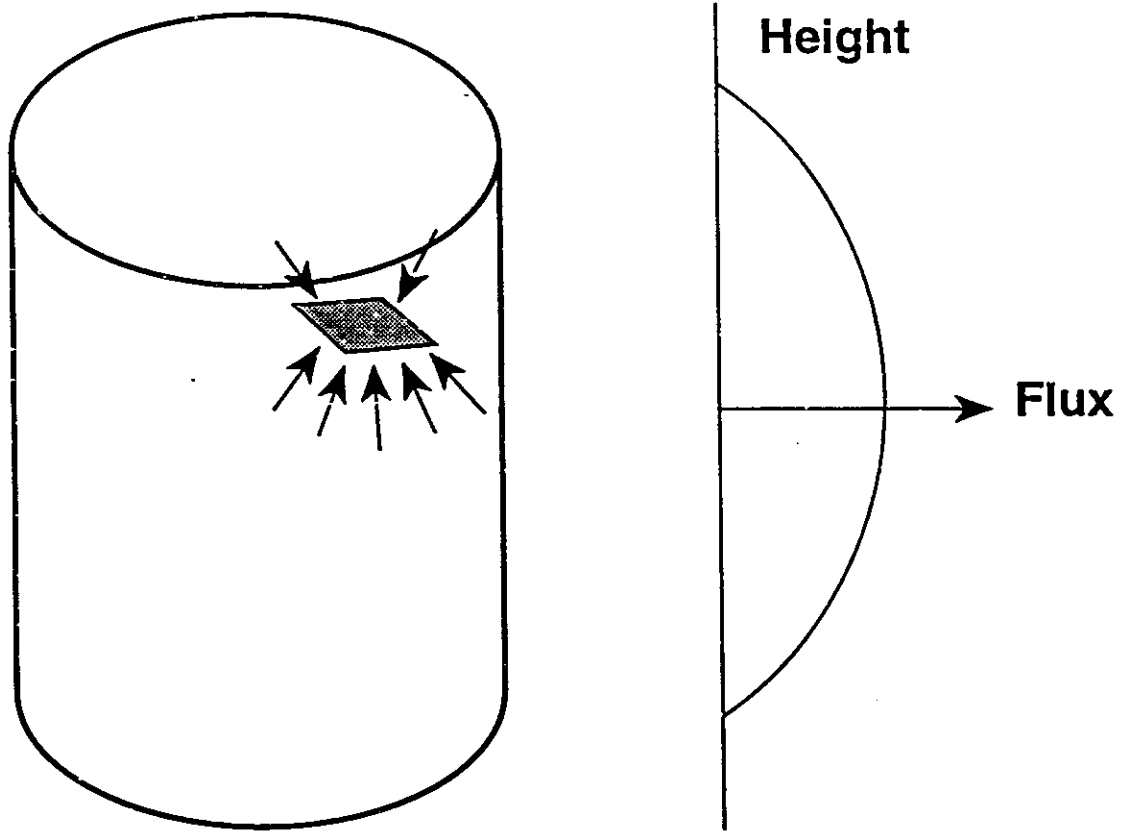


Fig. 6

# Variation of Thermal Neutron Flux in Axial and Radial Directions in a Cylindrical Reactor

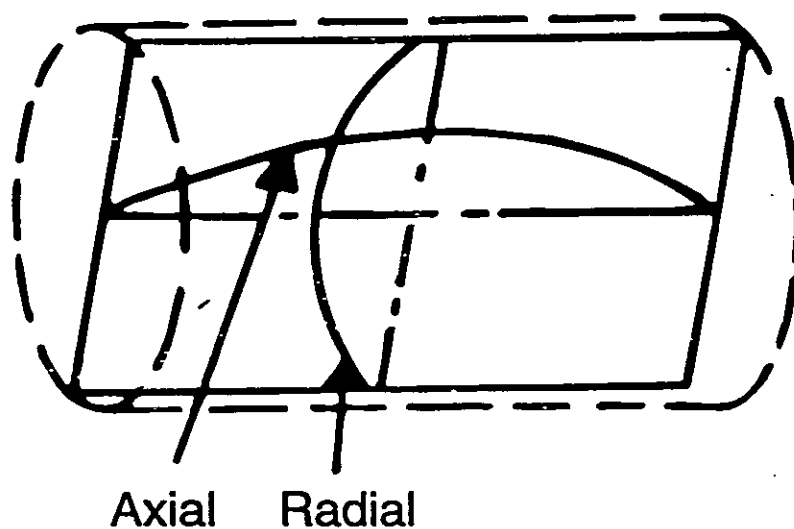
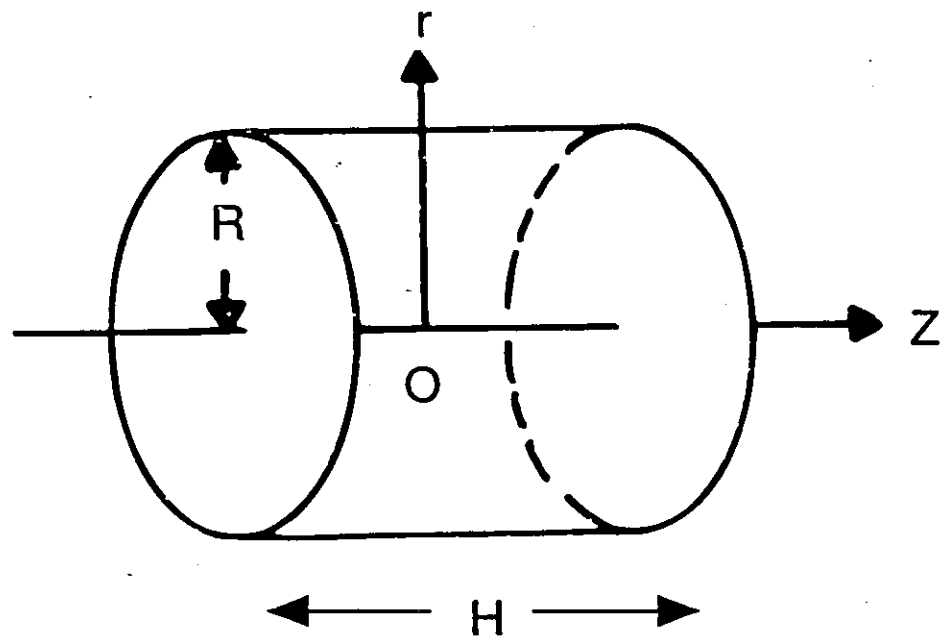
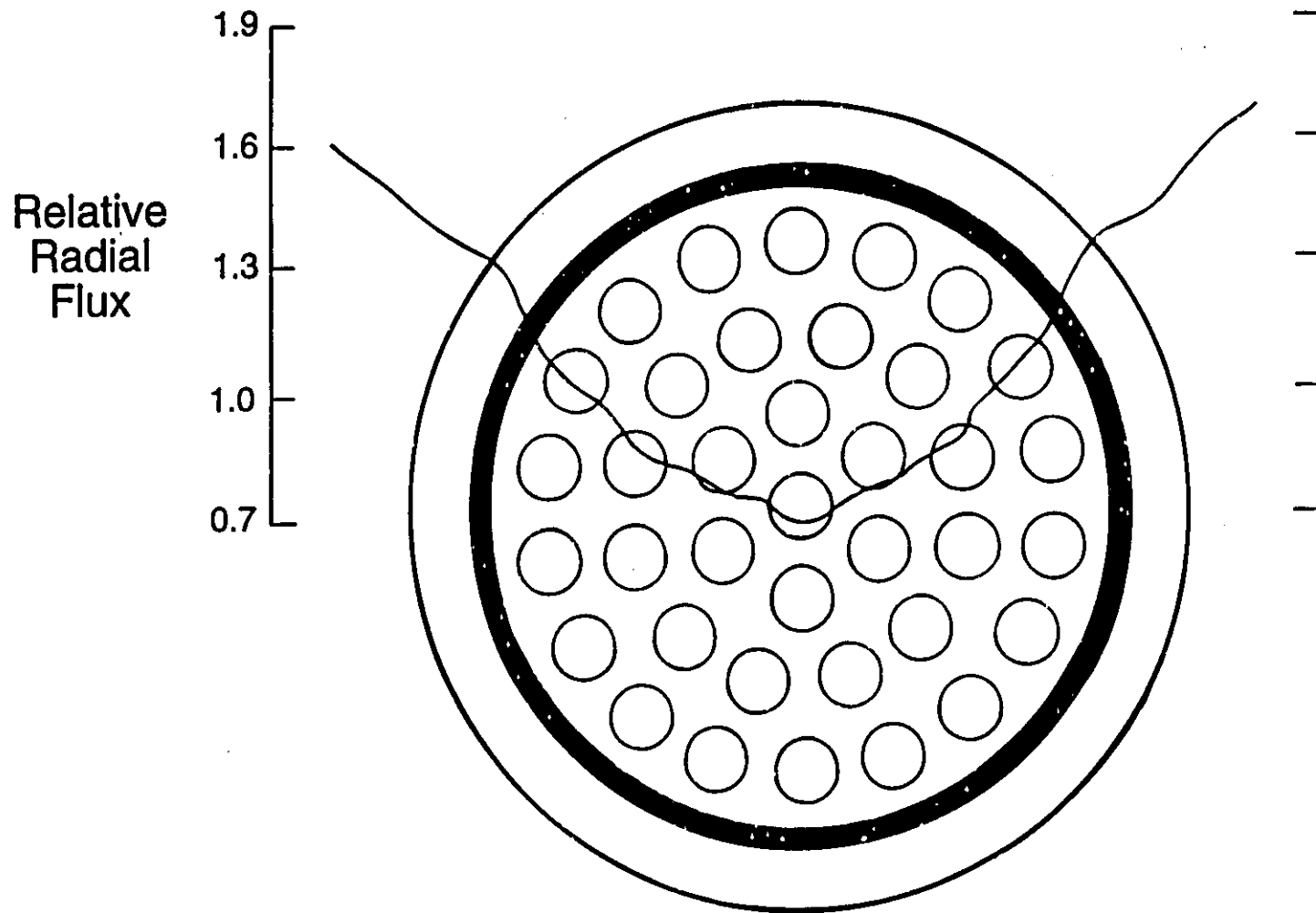


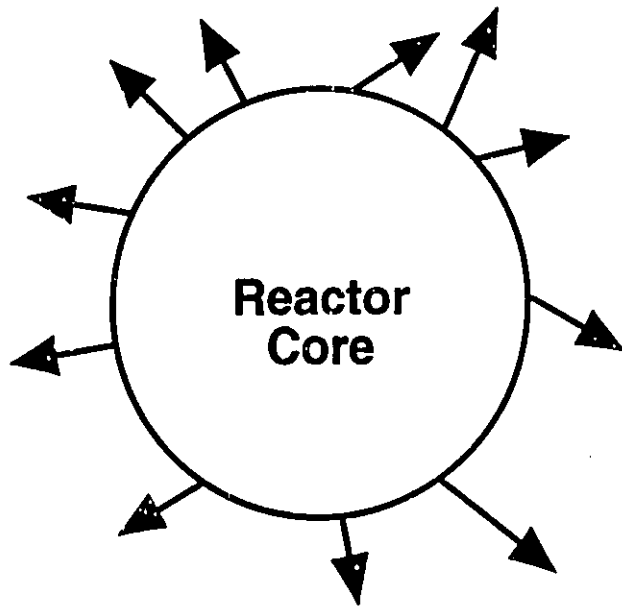
Fig. 6.



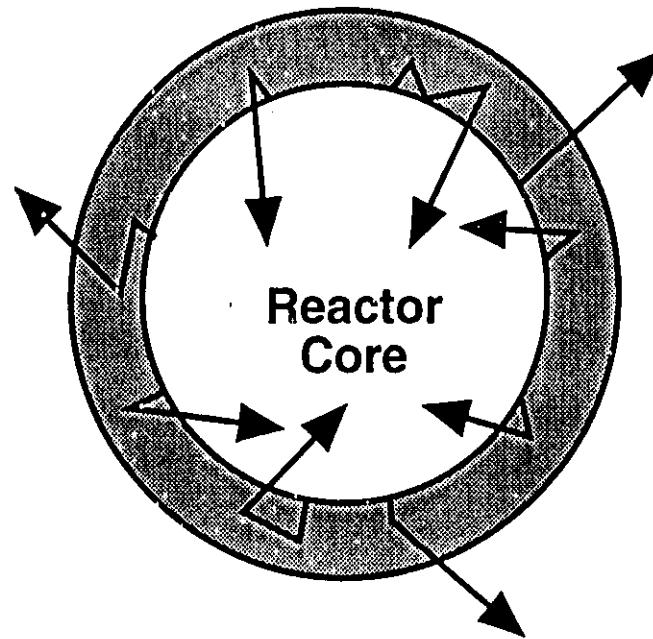
# Depression of the Thermal Neutron Flux in the Interior of Fuel Bundle



# Comparison of Neutron Leakage for Bare and Reflected Cores



(a)



(b)

# Effect of Reflector on Shape of Radial Flux

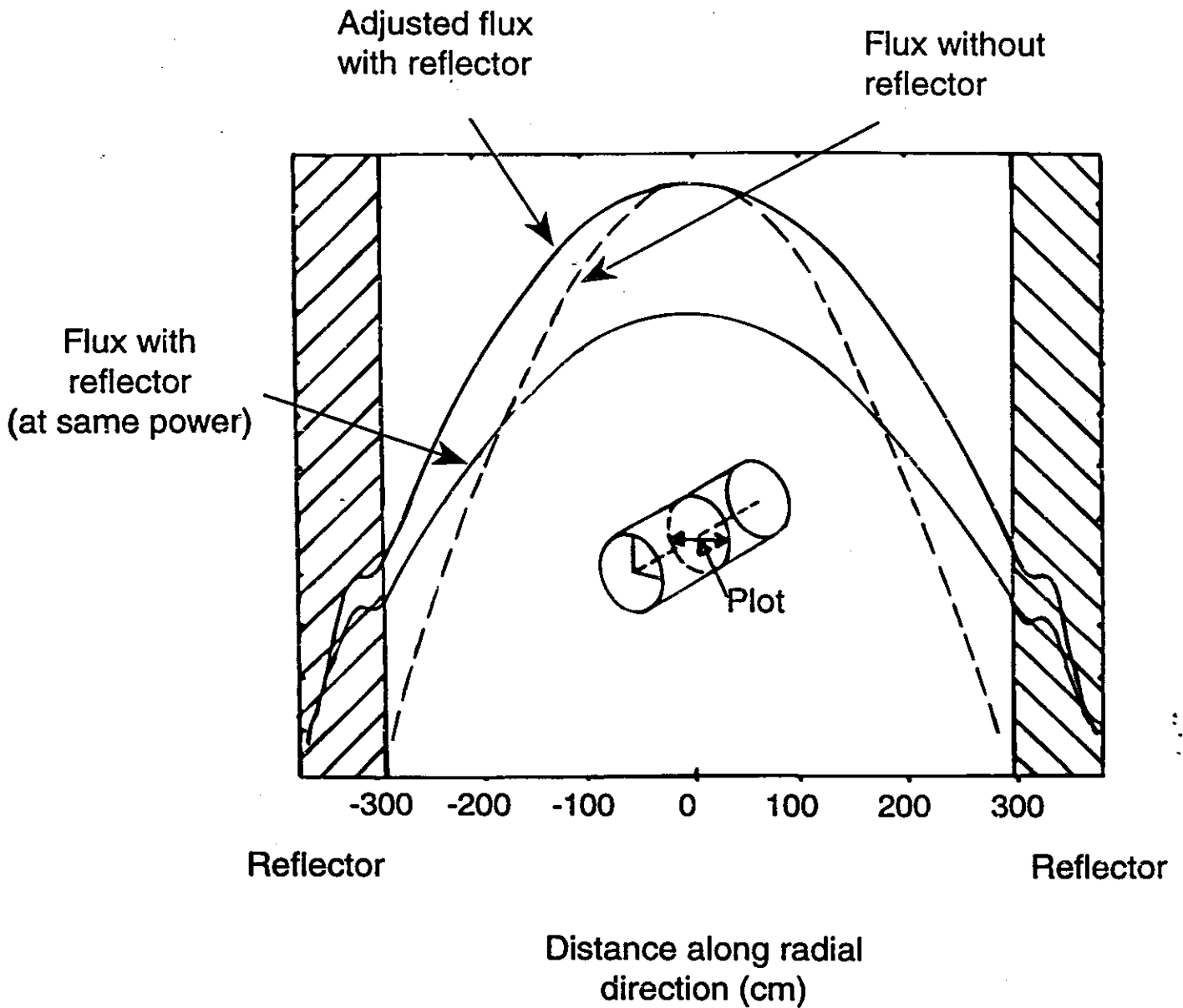
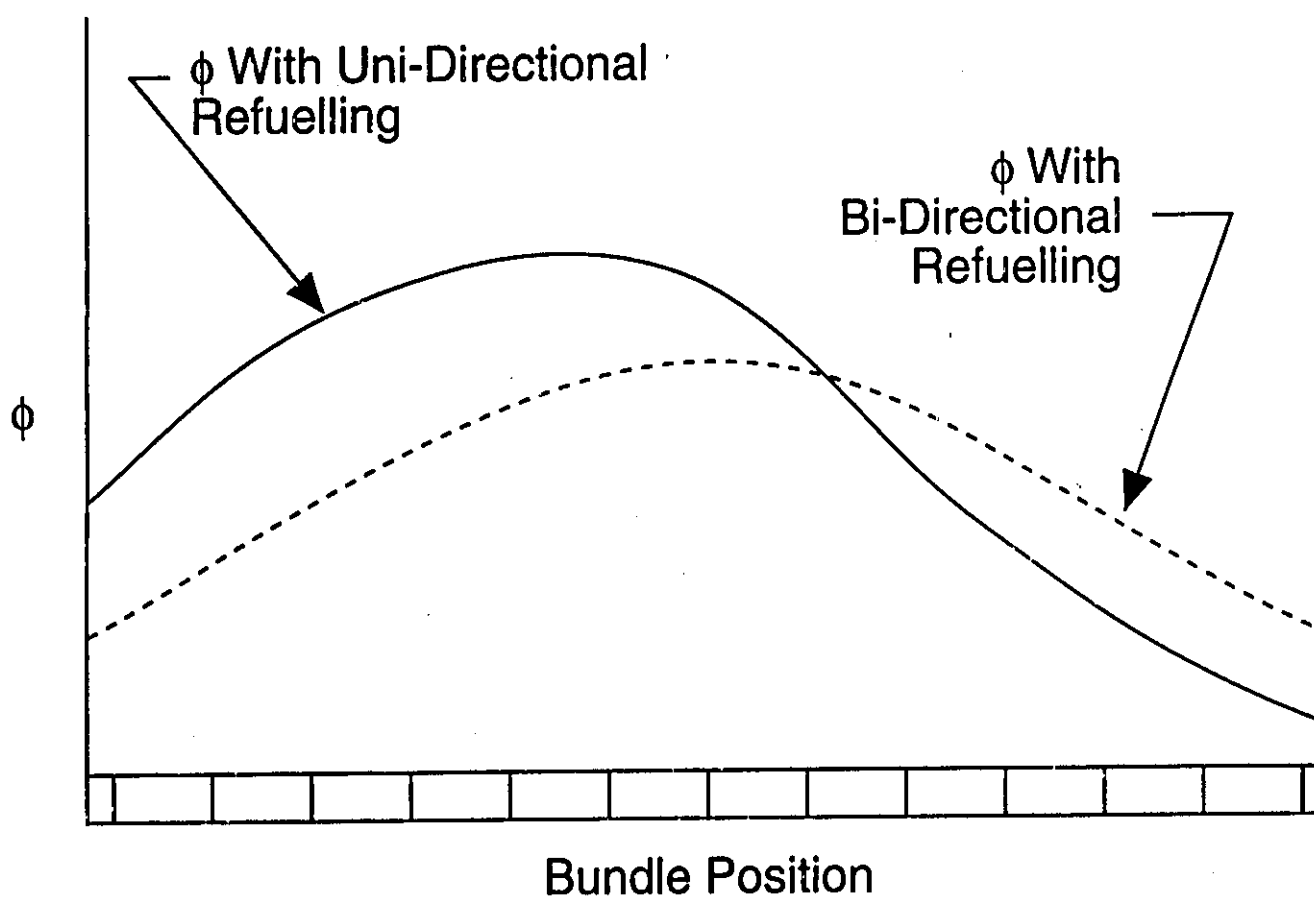


Fig. 6.

# Asymmetry Produced by Uni-Directional Refuelling



# Effect of Bi-Directional Refuelling in Flattening Axial Flux Shape

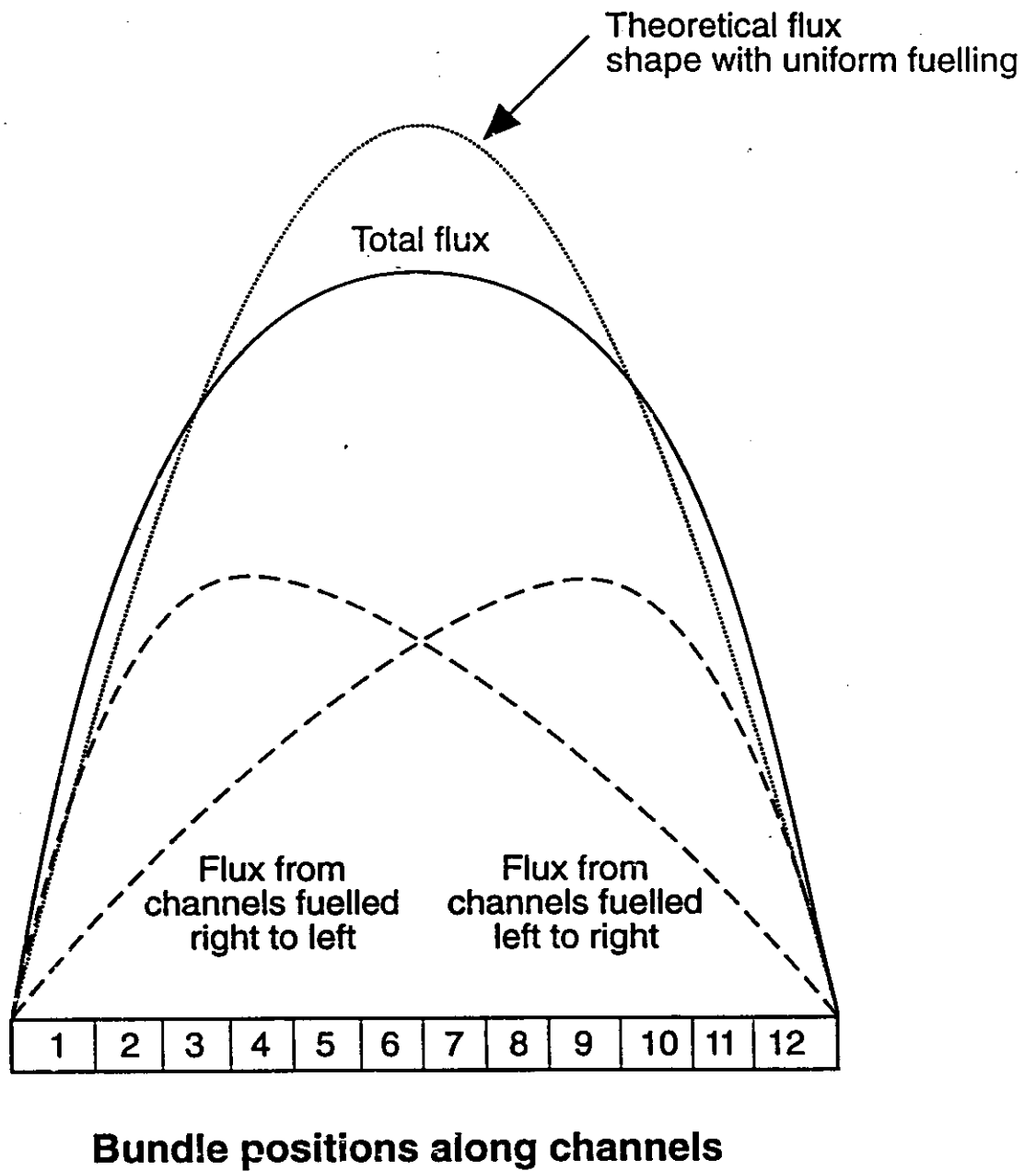


Fig. 6.

# Flux Flattening Produced by Adjuster Rods

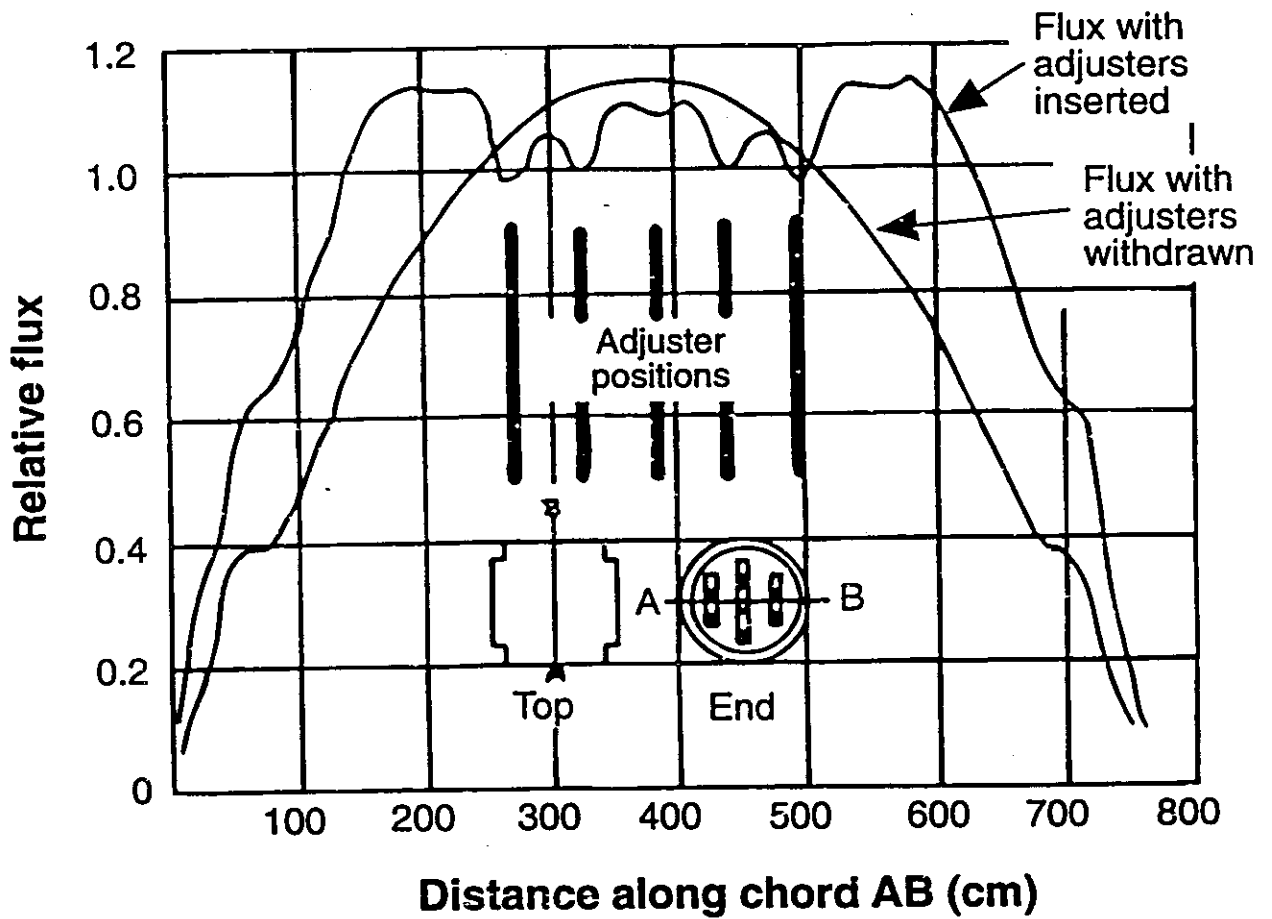


Fig. 6.

# Flux Flattening Produced by Differential Fuelling

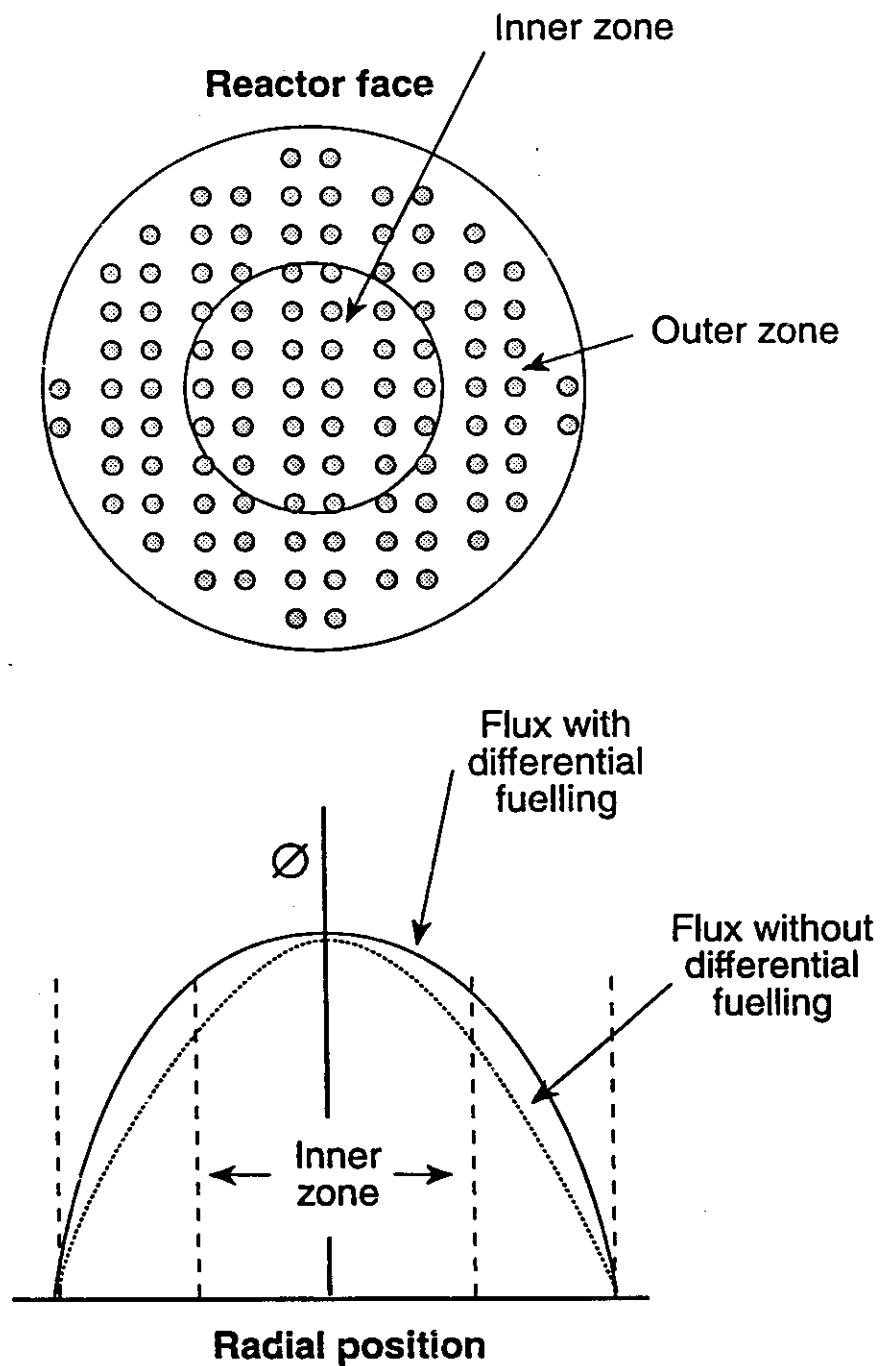
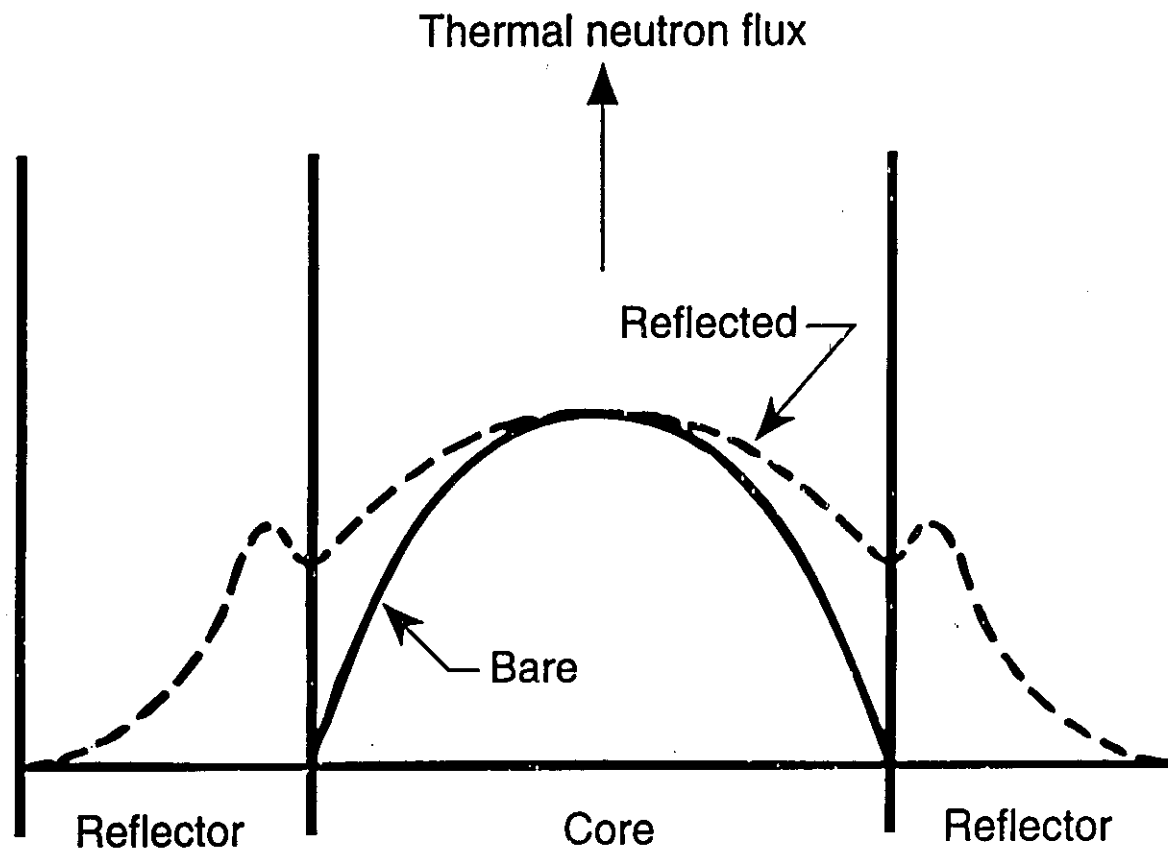


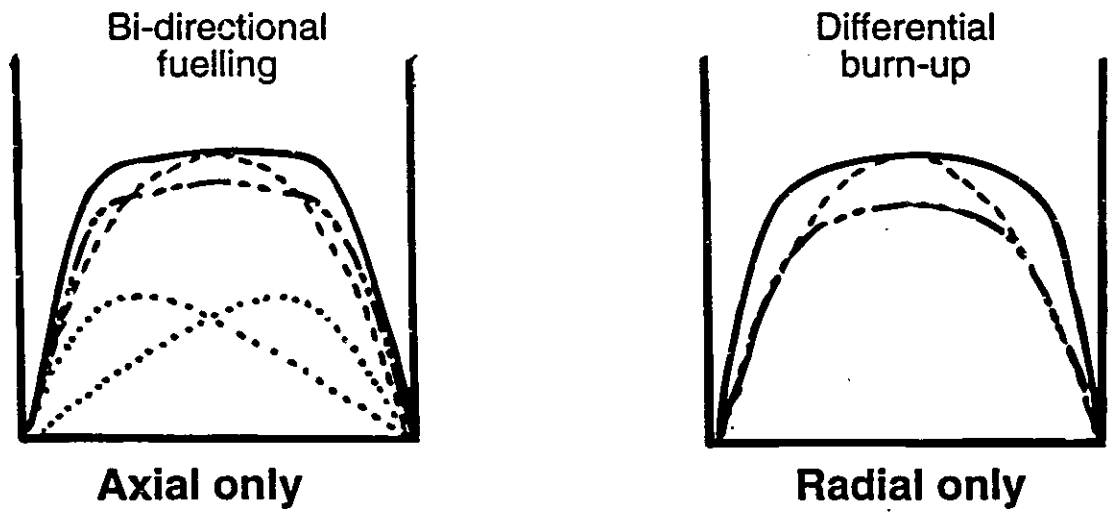
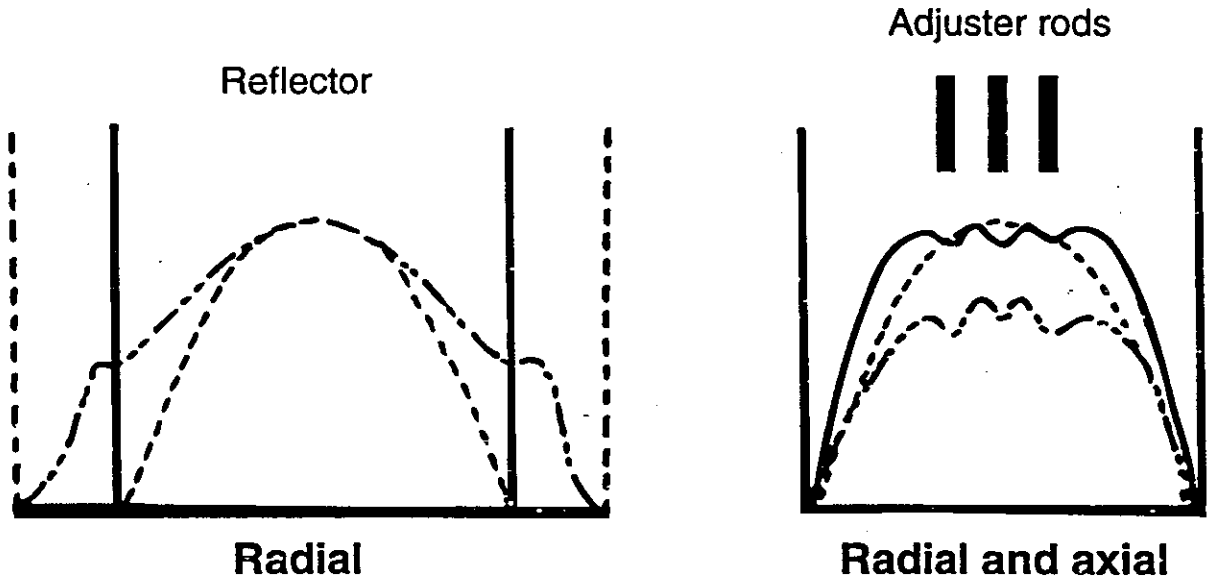
Fig. 6

# Flux Distribution in Reflected Reactor



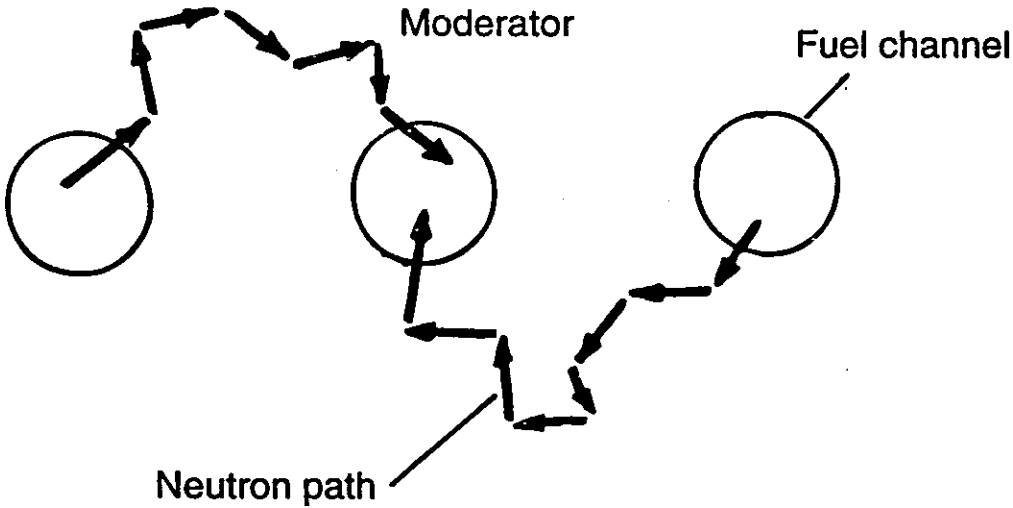
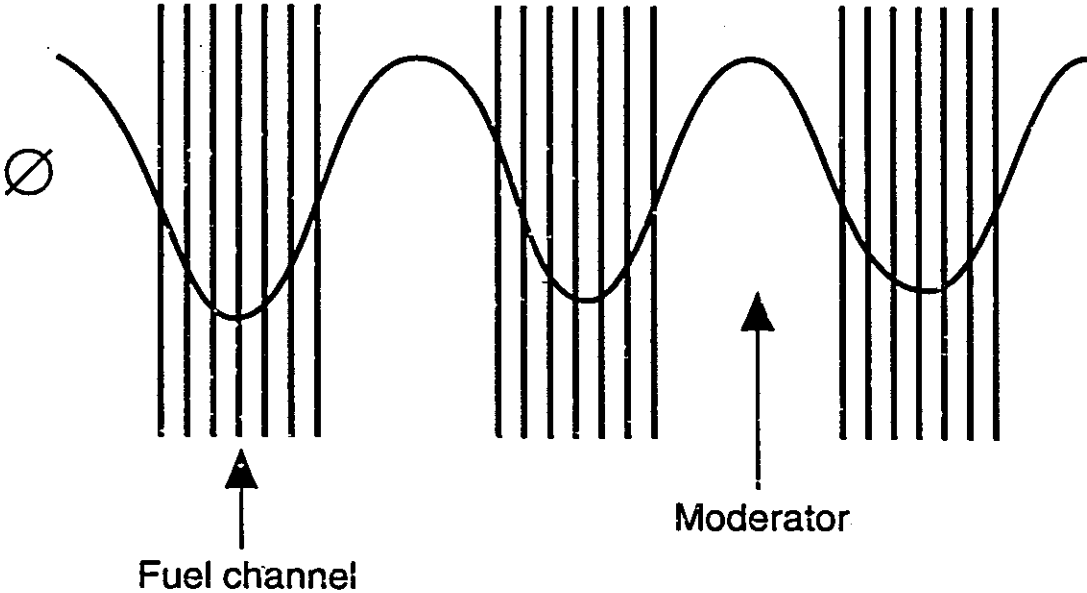


# Flux Flattening

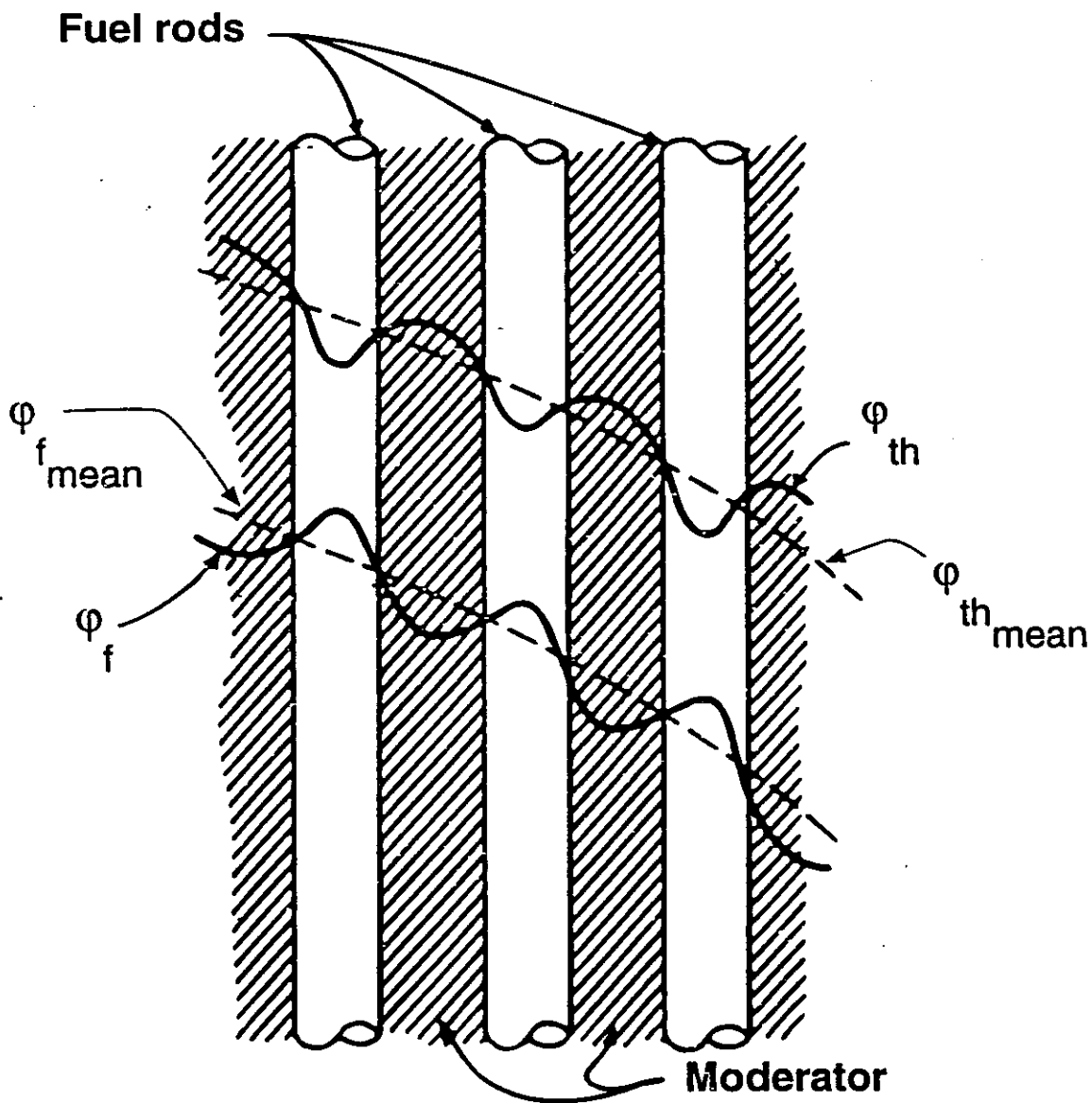


- Without flattening
- .-.-.-.- With flattening
- With flattening and power increase

# Neutron Flux in Core



# Flux Variation in Fuel



## Flux Flattening in CANDU Reactors

|               | Reflector      | Bi-directional<br>fuelling | Adjusters | Differential<br>burnup | $\frac{\phi_{avg}}{\phi_{max}}$ |
|---------------|----------------|----------------------------|-----------|------------------------|---------------------------------|
| NPD           | axial & radial | x                          |           |                        | 42%                             |
| Douglas Point | radial         | x                          |           | x                      | 50%                             |
| Pickering - A | radial         | x                          | x         |                        | 57%                             |
| Pickering - B | radial         | x                          | x         |                        | ~60%                            |
| Bruce - A     | radial         | x                          |           | x                      | ~59%                            |
| Bruce - B     | radial         | x                          | x         |                        | ~60%                            |
| Darlington    | radial         | x                          | x         | x                      | ~60%                            |
| Point Lepreau | radial         | x                          | x         | x                      | ~60%                            |