HEAT REMOVAL FROM REACTORS

HEAT REMOVAL FROM NUCLEAR REACTORS

OBJECTIVES: DISCUSS THERMAL DESIGN OF NUCLEAR REACTORS

- FISSION: ORIGIN OF THERMAL ENERGY.
- HEAT TRANSFER MECHANISMS:
 - ► CONDUCTION THROUGH FUEL RODS,
 - ► CONVECTION TO THE COOLANT.
- THE COOLANT TRANSPORTS THE THERMAL ENERGY TO **BOILERS** WHERE STEAM IS GENERATED.
 - ► HIGH COOLANT TEMPERATURE FOR HIGH STEAM CYCLES EFFICIENCY.
 - CONSEQUENCE: HIGH FUEL AND CLADDING TEMPERATURES
 METALLURGICAL LIMITATIONS.
- HIGH POWER GENERATION HIGH TEMPERATURE IN THE FUEL & CLADDING TEMPERATURE.
 - ► METALLURGICAL LIMITATIONS .
- COOLANT IS CIRCULATED BY A PUMP.
 - W_{P} / Q_{R} MINIMUM.
- PRACTICALLY, NO LIMIT TO THE THERMAL POWER RELEASED IN THE FUEL - REACTOR CORE.

QUESTION: HOW TO EXTRACT IT WHILE RESPECT-ING TEMPERATURE LIMITATIONS?

HEAT REMOVAL FROM REACTORS

THIS CAN BE ACHIEVED BY:
INCREASING THE COOLANT FLOW RATE. PROBLEMS: HIGH PUMPING POWER, VIBRATIONS.
INCREASING THE FLOW SECTION. PROBLEM: NEUTRON MULTIPLICATION FACTOR.
BY USING DIFFERENT COOLANT. REPLACE GAS COOLANTS BY LIQUID COOLANTS - LIGHT OR HEAVY WATER, OR BY LIQUID METALS.
USING HIGH FUEL-COOLANT CONTACT AREA. ROD BUNDLE DESIGN.
USING BOILING PHENOMENON.
A COMPROMISE BETWEEN NUCLEAR AND THERMAL DESIGN IS REQUIRED.

PAGE 7.2



THERMAL ENERGY RELEASE DURING FISSION IS DUE:

- FISSION PROCESS MAINLY.
- NON-FISSION CAPTURE IN THE FUEL, MODERATOR, COOLANT MATERIAL & STRUCTURAL MATERIAL.
- EMITTED ENERGY DURING FISSION: 207 MeV.
- DISTRIBUTION OF EMITTED ENERGY AMONG DIFFER-ENT FISSION COMPONENTS - TABLE 7.1.
- ENERGY CONVERTED INTO HEAT- RECOVERABLE ENERGY : 200 MeV - TABLE 7.1.
 - ► NEUTRINOS NO ENERGY DEPOSIT.
 - CAPTURE γ-RAYS AN AVERAGE OF 5 MeV ENERGY DEPOSIT.
- DISTRIBUTION OF HEAT RELEASE AMONG DIFFERENT REACTOR COMPONENTS - TABLE 7.2.

HEAT REMOVAL FROM REACTORS - HEAT GENERATION

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Components	Emitted energy	Energy converted to hea or recovered energy	
	Mev	Mev	% of total
Fission fragments	168	168	84
Neutrons	5	5	2.5
Prompt γ rays	7	7	3.5
Delayed radiations:	8	8	4
β-rays γ-rays	7	7	3.5
neutrinos	12 ·	-	-
Capture γ-rays	-	5	2.5 100
TOTAL	207	200	100

Table 7.1 Emitte	d and recoverabl	e energies for	fission of ²⁵ U

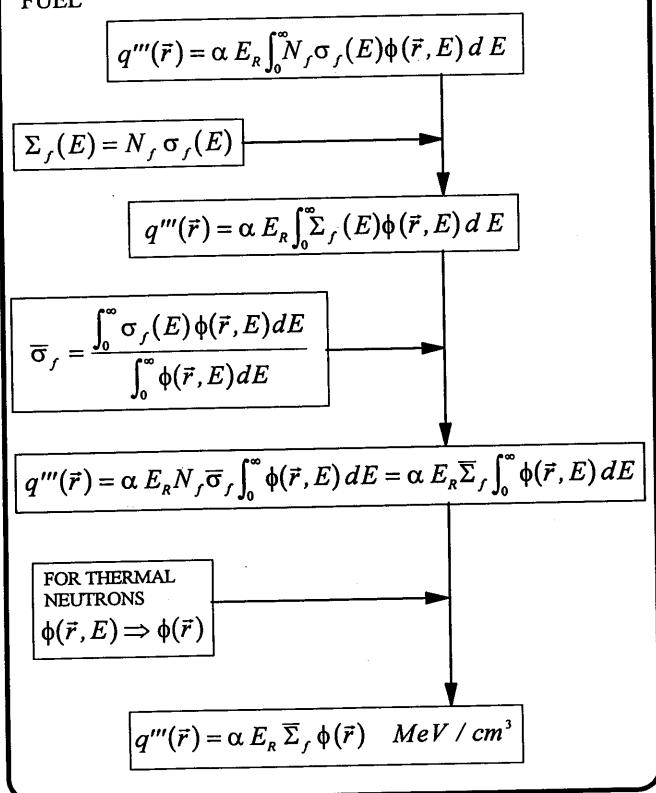
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Table 7.2 Distribution of heat release among different components of CANDU reactors

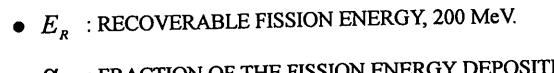
Components		Released thermal energy, %
Energy released in the fuel		93.9
Energy released in the pressure tubes		0.3
Energy released in the calandria		0.1
Energy released in the coolant		0.5
Energy released in the moderator		5.0
Energy released in the shieldings		0.2
	TOTAL	100.0

HEAT REMOVAL FROM REACTORS - HEAT GENERATION

VOLUMETRIC HEAT GENERATION RATE IN REACTOR FUEL







- α : FRACTION OF THE FISSION ENERGY DEPOSITED IN THE FUEL.
- $\overline{\Sigma}_{f}$: MACROSCOPIC FISSION CROSS-SECTION OF THERMAL NEUTRONS.
- $\phi(\vec{r})$: THERMAL NEUTRONS FLUX.
- TO EXPRESS q''' IN

 W / cm^3 multiply by $1.602 \cdot 10^{-13}$ kW / m^3 multiply by $1.602 \cdot 10^{-10}$

USEFUL DEFINITIONS:

• POWER DENSITY OF THE CORE: $kW/l \text{ or } kW/m^3$

- SPECIFIC POWER OF THE FUEL: *kW / kg or MW / ton*
- POWER DENSITY OF THE FUEL: $kW/l \text{ or } MW/m^3$

FOR CANDU REACTORS:

- AVERAGE POWER DENSITY OF THE CORE: 12 MW / m^3
- AVERAGE POWER DENSITY OF THE FUEL: 115 MW/m^3
- MAXIMUM POWER DENSITY OF THE FUEL: 190 MW / m^3

TABLE 拜 | 7.3

Table 7.3 Power density	of popular reactors in MW/m ³
14010 7.5 1 01101 401011	

Reactor type	Average power density of the core	Average power density of the fuel*	Maximum power density of the fuel*
CANDU	12	110	190
Boiling water reactors	56	56 ·	180
Pressurized water reactors	95-105	95-105	190-210

•



SPATIAL VOLUMETRIC HEAT GENERATION DISTRI-BUTION IN THE REACTOR CORE

• WE HAVE SEEN THAT:

$q^{\prime\prime\prime}(\vec{r}) = \alpha E_{R} \overline{\Sigma}_{f} \phi(\vec{r}) \sim \phi(\vec{r})$

- $\phi(\vec{r})$ is determined by solving:
 - ► MULTI-GROUP NEUTRON DIFFUSION EQUATION, OR
 - NEUTRON TRANSPORT EQUATION. (WHICH ARE BEYOND THE SCOPE OF THIS COURSE.)
- TO SIMPLIFY THE DISCUSSION, THE FOLLOWING ASSUMPTIONS ARE MADE.
 - CYLINDRICAL REACTOR CORE WITH AXIAL AND RADIAL REFLECTORS.
 - ► CONSTANT FUEL ENRICHMENT.
 - UNIFORMLY DISTRIBUTED FUEL THROUGHOUT THE CORE, I.E., HOMOGENEOUS REACTOR.

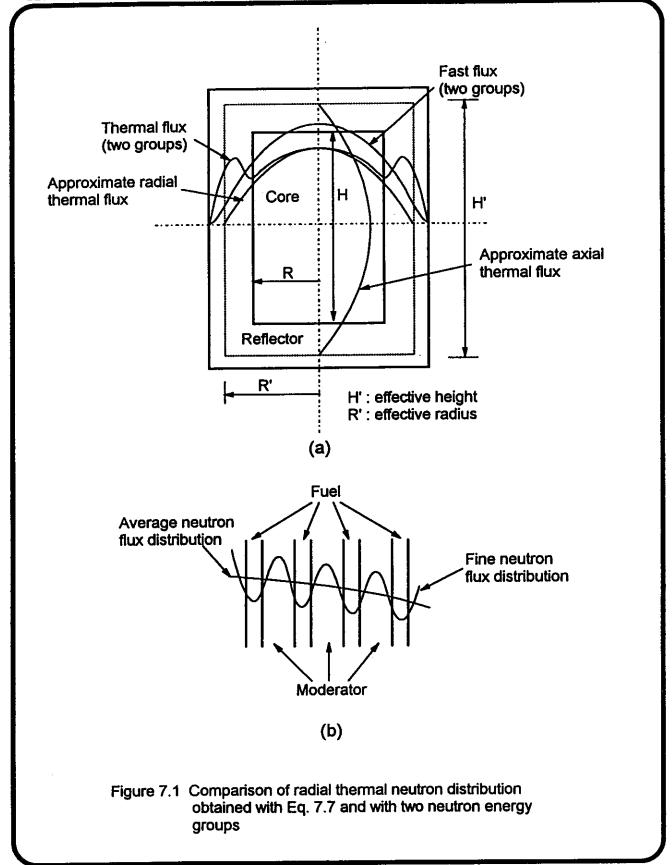
DISCUSS THE SITUATION FOR PWR AND CANDU REACTORS.

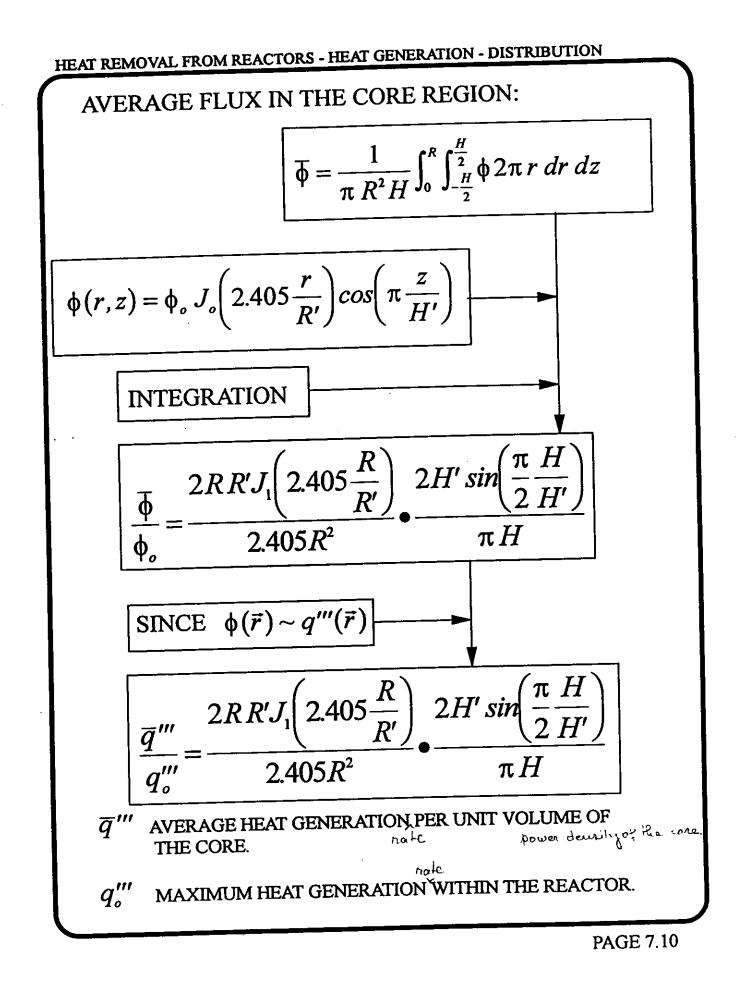
• UNDER ABOVE CONDITIONS, THE DISTRIBUTION OF THE THERMAL NEUTRONS IN THE REACTOR CORE IS APPROXIMATE BY:

$$\phi(r,z) = \phi_o J_o\left(2.405 \frac{r}{R'}\right) \cos\left(\pi \frac{z}{H'}\right)$$

• DISCUSS FIGURE 7.1 TO SHOW THAT THE APPROXIMA-TION IS REASONABLE.

HEAT REMOVAL FROM REACTORS - HEAT GENERATION - DISTRIBUTION





HEAT REMOVAL FROM REACTORS - HEAT GENERATION - DISTRIBUTION

$$\frac{\overline{q}'''}{q_{0}'''} = \frac{2RR'J_{1}\left(2.405\frac{R}{R'}\right)}{2.405R^{2}} \cdot \frac{2H'\sin\left(\frac{\pi}{2}\frac{H}{H'}\right)}{\pi H}$$

• FOR A BARE REACTOR WHERE R = R' and H = H'THE INVERSE OF THE ABOVE RATIO IS:

$$\frac{q_o'''}{\overline{q}'''} = \frac{2.405}{2J_1(2.405)}\frac{\pi}{2} = 3.64$$

• FOR

$$\frac{R}{R'} = \frac{H}{H'} = 0.83$$

THIS RATIO IS:

$$\frac{q_o'''}{\overline{q}'''} = 2.35$$

• FOR A UNIFORM RADIAL NEUTRON FLUX:

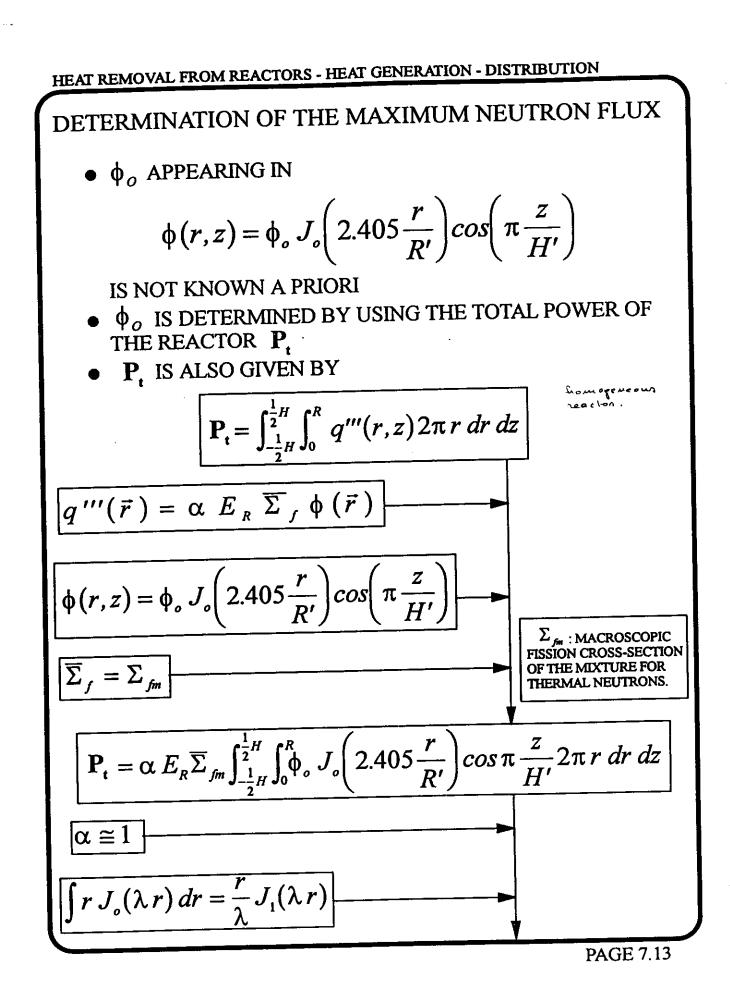
$$\frac{q_o'''}{\overline{q}'''} = 1.57$$

CONCLUSION: THE MAXIMUM HEAT GENERATION RATE IN THE CORE MAY BE SUBSTANTIALLY HIGHER THAN THE AVERAGE HEAT GENERATION RATE.

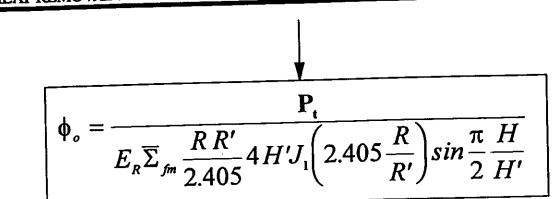
HEAT REMOVAL FROM REACTORS - HEAT GENERATION - DISTRIBUTION

NEUTRON FLUX FLATTENING

- HIGH $q_o''' \overline{q}'''$ IS NOT DESIRABLE.
- REACTOR POWER OUTPUT CAN BE INCREASED BY DE-CREASING THIS RATIO - I.E., MORE UNIFORM HEAT GE-NERATION RATE.
- THIS IS KNOWN AS: "FLATTENING OF THE HEAT GENE-RATION DISTRIBUTION OR OF THE NEUTRON DISTRI-BUTION.
- NEUTRON FLUX FLATTENING IS ACHIEVED BY:
 - ► ADDING REFLECTORS AROUND A BARE REACTOR.
 - ► VARYING RADIAL FUEL ENRICHMENT.
 - ► VARYING THE RATIO OF FUEL-TO-MODERATOR.
 - ► VARYING THE EXTEND OF INSERTION OF CONTROL RODS.
 - ► USING A NEUTRON POISON IN CERTAIN PARTS OF THE CORE.
- ADVANTAGES OF NEUTRON FLATTENING:
 - ► REACTOR POWER OUTPUT INCREASES.
 - ► IN CANDU REACTORS THE COOLANT DISTRIBUTION AMONG THE FUEL CHANNELS IS EASILY ACHIEVED.



HEAT REMOVAL FROM REACTORS - HEAT GENERATION - DISTRIBUTION



WHERE



 $\overline{\Sigma}_{fm}$ IS THE MACROSCOPIC FISSION CROSS-SECTION FOR THERMAL NEUTRONS

 E_{R} RECOVERED ENERGY

IF

$$\frac{R}{R'} = \frac{H}{H'} = 0.83$$

 ϕ_o BECOMES:

$$\phi_o = 2.35 \frac{\mathbf{P}_t}{E_R \overline{\Sigma}_{fm} V}$$

THE DISTRIBUTION OF THE THERMAL NEUTRON FLUX IS THEN GIVEN BY:

$$\phi = \frac{2.35 \mathbf{P}_{t}}{E_{R} \overline{\Sigma}_{fm} V} J_{o} \left(2.405 \frac{r}{R'} \right) \cos \pi \frac{z}{H'}$$

HETEROGENEOUS REACTORS

 CONSIDER A HETEROGENEOUS REACTOR CONSISTING OF "N" FUEL ASSEMBLIES OF "n" RODS:

 r_o IS THE FUEL RADIUS,

- H LENGTH OF THE FUEL,
- Σ_{fr} MACROSCOPIC CROSS SECTION OF THE FUEL. Σ_{fr} to track and

• TOTAL FISSION CROSS SECTION OF THE ENTIRE CORE:

$$\overline{\Sigma}_{fr} Nn\pi r_o^2 H$$

• AVERAGE VALUE OF $\overline{\Sigma}_{fm}$ IN THE CORE IS GIVEN BY

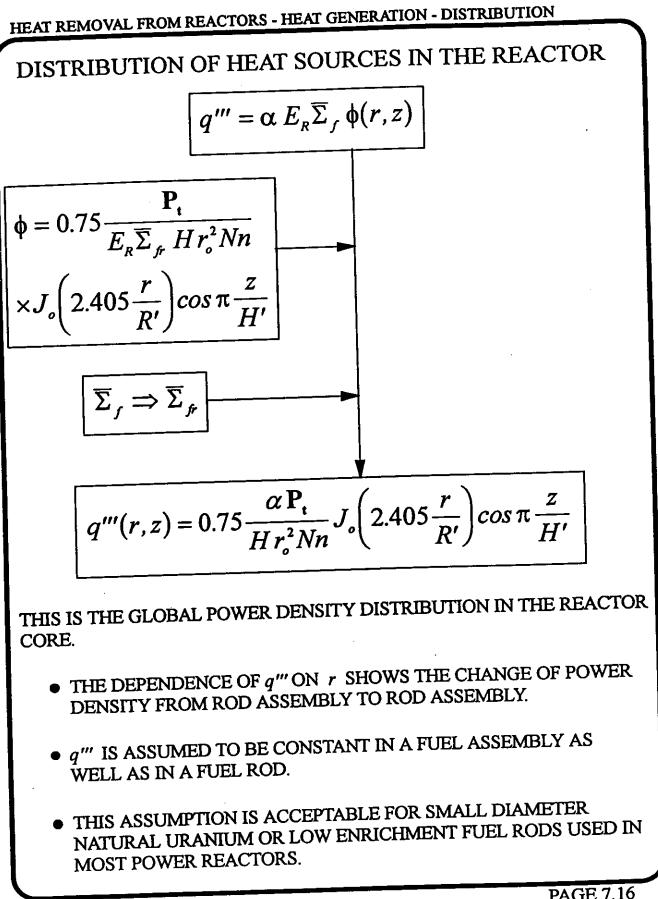
$$\overline{\Sigma}_{fm} = \frac{\overline{\Sigma}_{fr} Nn\pi r_o^2 H}{\pi R^2 H} = \frac{\overline{\Sigma}_{fr} Nnr_o^2}{R^2}$$

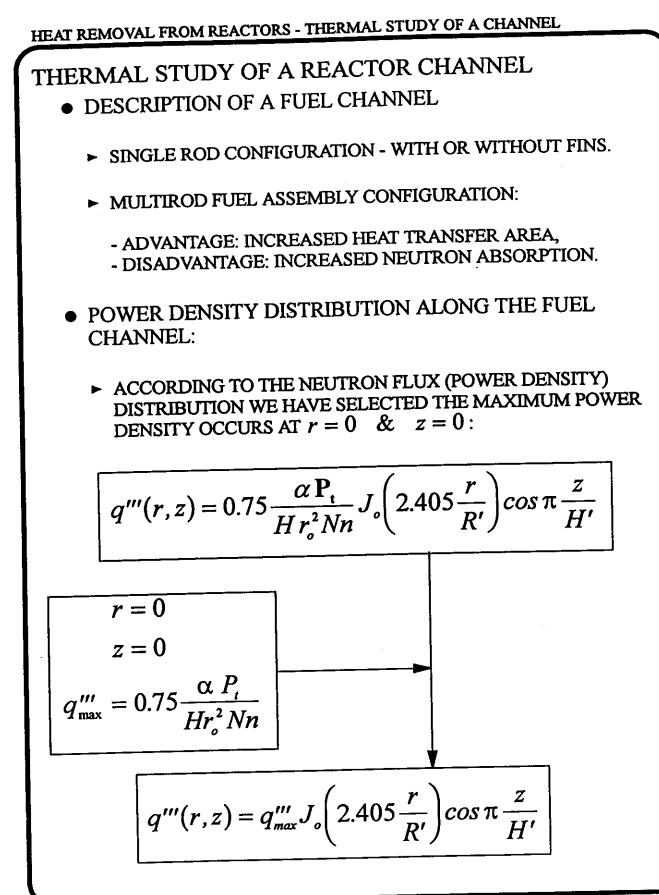
• COMBINING $\overline{\Sigma}_{fm}$ WITH

$$\phi = \frac{2.35 \mathbf{P}_{t}}{E_{R} \,\overline{\Sigma}_{fm} \,V} J_{o} \left(2.405 \frac{r}{R'} \right) \cos \pi \frac{z}{H'}$$

WE OBTAIN:

$$\phi = 0.75 \frac{\mathbf{P}_{t}}{E_{R} \overline{\Sigma}_{fr} H r_{o}^{2} Nn} J_{o} \left(2.405 \frac{r}{R'} \right) \cos \pi \frac{z}{H'}$$





 POWER DENSITY DISTRIBUTION ALONG A CHANNEL (AXIAL DISTRIBUTION) SITUATED AT A GIVEN RADIAL DISTANCE IS:

$$q''' = q_o''' \cos \pi \frac{z}{H'}$$

WHERE:

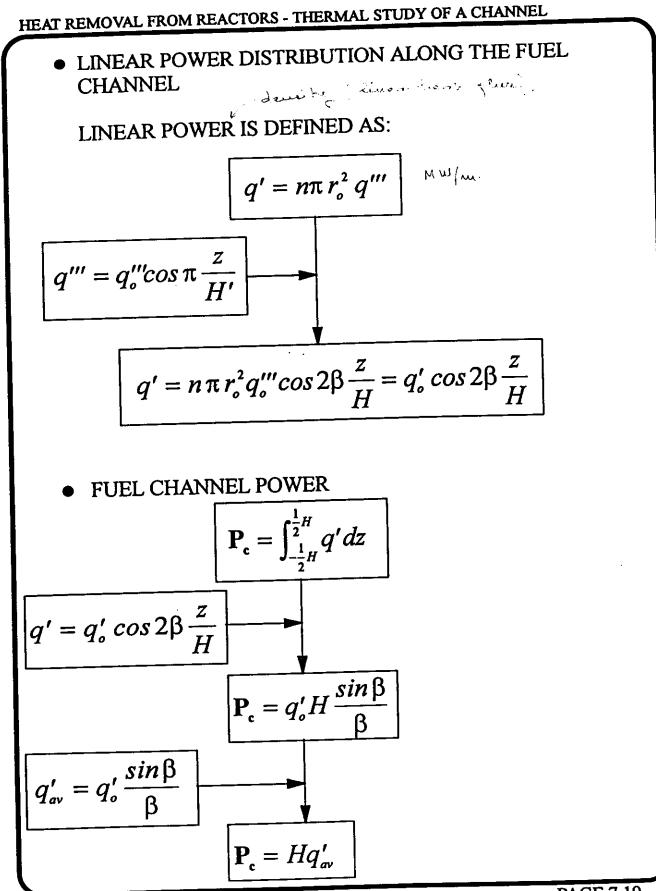
$$q_{o}'''=q_{max}'''J_{o}\left(2.405\frac{r}{R'}\right)$$

IT IS MORE CONVENIENT TO WRITE THE AXIAL DISTRIBU-TION AS:

$$q''' = q_o'''\cos 2\frac{\pi H}{2H'}\frac{z}{H} = q_o'''\cos 2\beta \frac{z}{H}$$

► AVERAGE POWER DENSITY IN A FUEL CHANNEL:

$$q_{av}^{'''} = \frac{\int_{-\frac{1}{2}H}^{\frac{1}{2}H} q_{o}^{'''} \cos 2\beta \frac{z}{H} dz}{\int_{-\frac{1}{2}H}^{\frac{1}{2}H} dz} = q_{o}^{'''} \frac{\sin \beta}{\beta}$$



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BASIC EQUATIONS FOR THE THERMAL STUDY OF A FUEL CHANNEL

THESE EQUATIONS ARE:

- 1. MASS CONSERVATION EQUATION FOR THE COOLANT.
- 2. MOMENTUM CONSERVATION EQUATION FOR THE COOLANT.
- 3. ENERGY CONSERVATION EQUATION FOR THE COOLANT.
- 5. ENERGY CONSERVATION EQUATION FOR THE FUEL (HEAT CONDUCTION EQUATION).
- 6. ENERGY CONSERVATION EQUATION FOR THE CLAD-DING (HEAT CONDUCTION EQUATION).

PLUS APPROPRIATE INITIAL AND BOUNDARY CONDITIONS.

IN THE FOLLOWING DISCUSSION, IT WILL BE ASSUMED THAT:

- THE PRESSURE IS CONSTANT ALONG THE FUEL CHANNEL, AND
- THE COOLANT FLUID IS INCOMPRESSIBLE.

THEREFORE,

- MOMENTUM EQUATION FOR THE COOLANT WILL BE IGNORED, AND
- THE MASS CONSERVATION EQUATION IS GIVEN BY:

G = const

COOLANT ENERGY CONSERVATION EQUATION

REFER TO FIGURE 7.2

ENERGY CONSERVATION PRINCIPLE APPLIED TO THE CON-TROL VOLUME SELECTED IN THE COOLANT:

 $\left(h + \frac{\partial h}{\partial z} dz\right) GA d\tau + \frac{\partial u}{\partial \tau} A dz \rho d\tau = h GA d\tau + q_c'' s dz d\tau$

0R

$$\rho \frac{\partial u}{\partial \tau} + G \frac{\partial h}{\partial z} = \frac{q_c''s}{A}$$

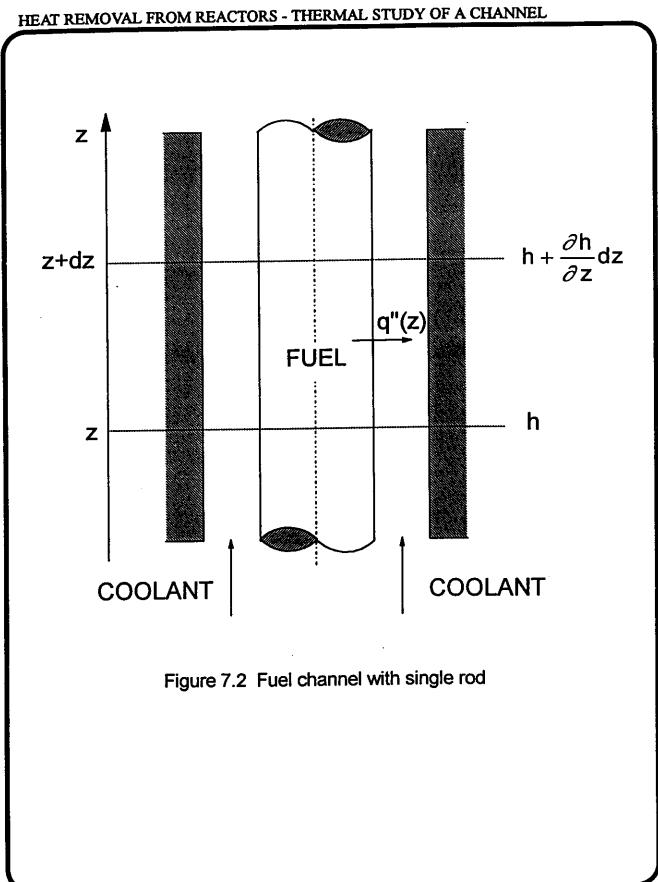
HEAT CONDUCTION EQUATION FOR FUEL:

$$\frac{1}{r}\frac{\partial}{\partial r}\left(k_{f}r\frac{\partial t}{\partial r}\right) + q''' = \frac{\partial}{\partial \tau}\left(\rho_{f}c_{f}t\right) \qquad 0 \le r \le r_{o}$$

HEAT CONDUCTION EQUATION FOR CLADDING:

$$\frac{1}{r}k_{c}\frac{\partial}{\partial r}\left(r\frac{\partial t}{\partial r}\right) = \frac{\partial}{\partial \tau}(\rho_{c}c_{c}t) \qquad r_{o} \leq r \leq r_{c}$$

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BOUNDARY CONDITIONS:

- INLET MASS FLOW RATE.
- INLET TEMPERATURE.
- INLET PRESSURE.
- HEAT CONVECTION AT THE FUEL ELEMENT SURFACE:

$$q_{c}^{\prime\prime} = -k_{c} \left(\frac{\partial t_{c}(r)}{\partial r} \right)_{r=r_{c}} = h_{c} \left(t_{c}(r_{c}) - t \right)$$

• HEAT TRANSFER AT THE FUEL-CLADDING INTERFACE:

$$q_{r=r_{e}}^{\prime\prime} = h_{g} \left(t_{f}(r_{o}) - t_{c}(r_{o}) \right)$$

 h_g : GAP CONDUCTANCE

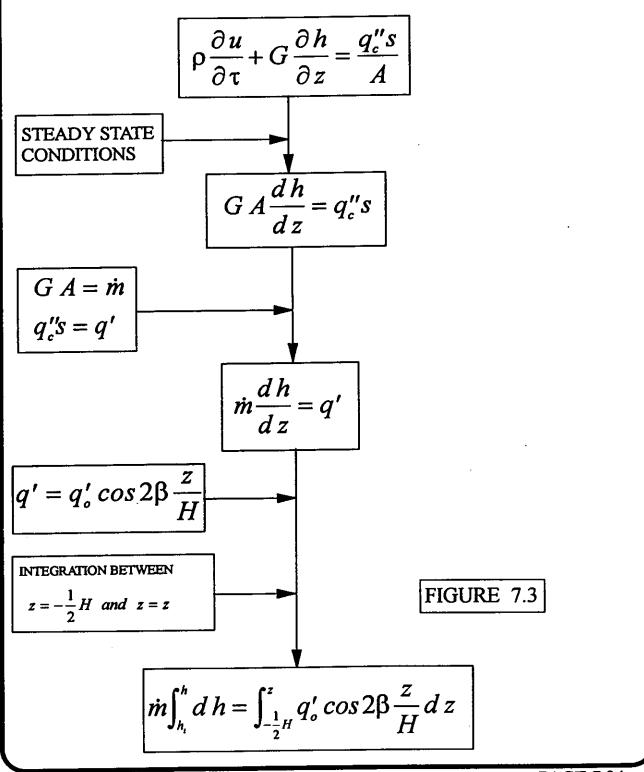
• CONTINUITY OF HEAT FLUXES AT THE FUEL- CLAD-DING INTERFACE:

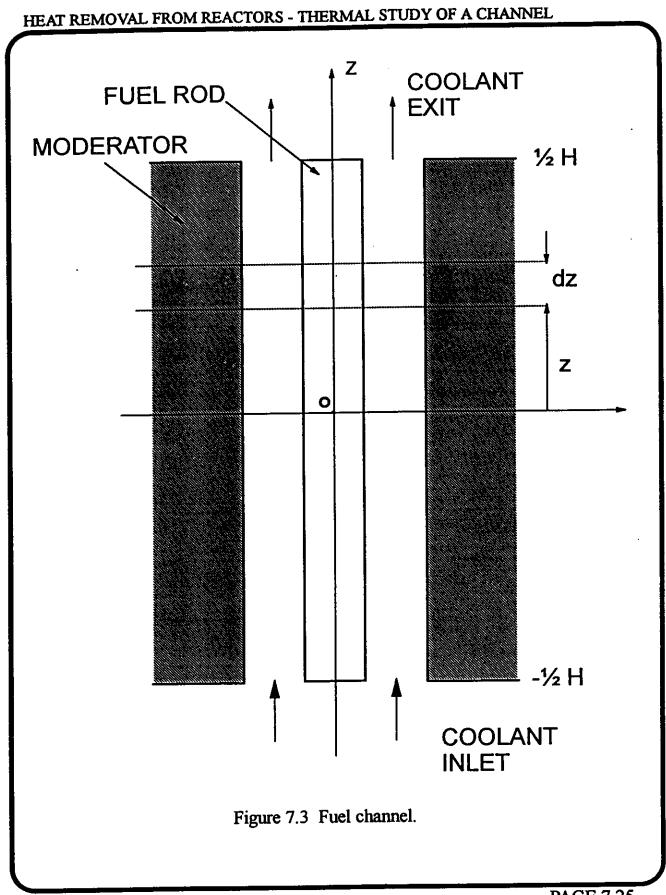
$$k_f\left(\frac{\partial t_f(r)}{\partial r}\right)_{r=r_{\bullet}} = k_c\left(\frac{\partial t_c(r)}{\partial r}\right)_{r=r_{\bullet}}$$

THE NUMERICAL SOLUTION OF THE ENERGY EQUA-TIONS WITH ABOVE BOUNDARY CONDITIONS AND APPROPRIATE INITIAL CONDITIONS YIELDS:

- AXIAL DISTRIBUTION OF THE COOLANT TEMPERA-TURE, AND
- TEMPERATURE DISTRIBUTION IN THE FUEL AND THE CLADDING.

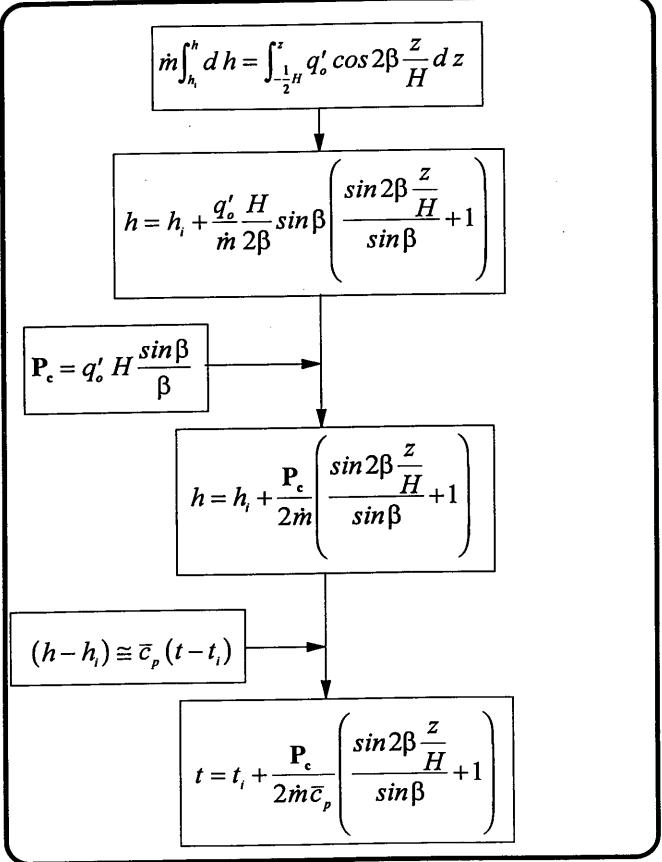
COOLANT TEMPERATURE VARIATION ALONG THE FUEL CHANNEL:

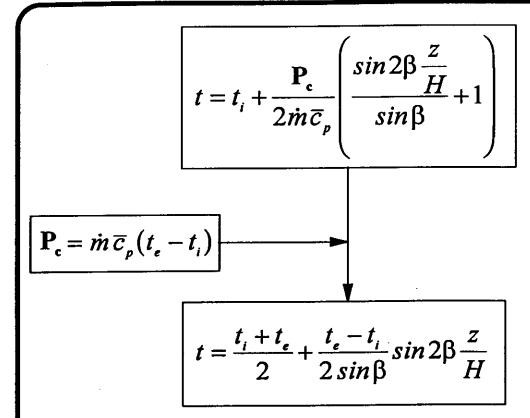




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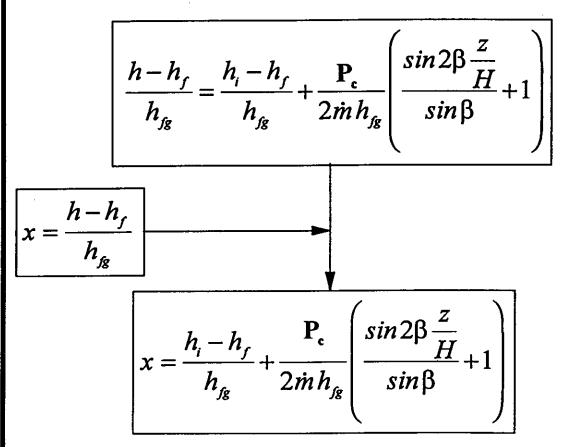
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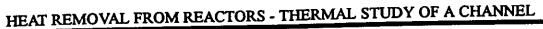
$$h = h_i + \frac{\mathbf{P_c}}{2\dot{m}} \left(\frac{\sin 2\beta \frac{z}{H}}{\sin \beta} + 1 \right)$$

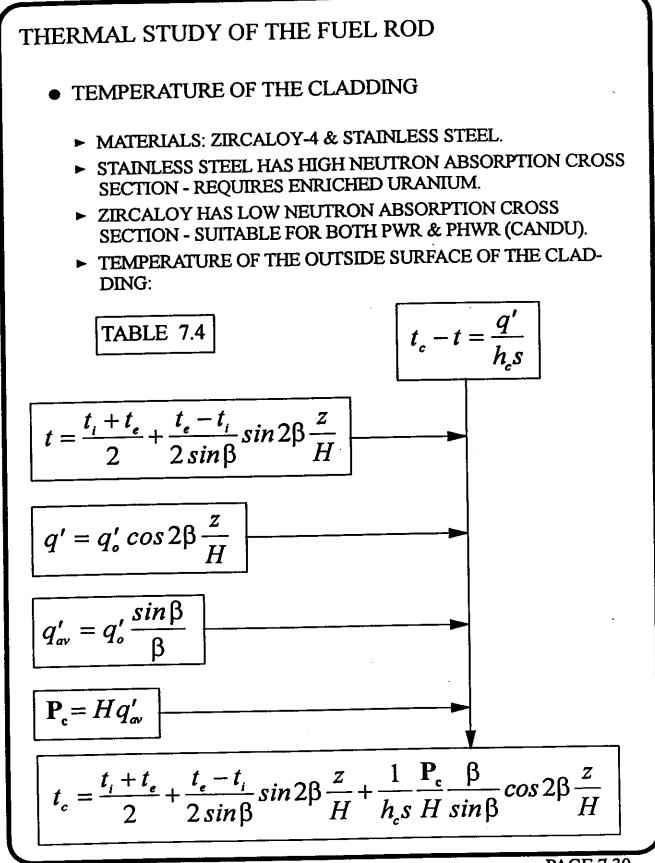
- SUBTRACT FROM BOTH SIDES THE SATURATION ENTHALPY, h_f .
- DIVIDE BOTH SIDES BY THE LATENT HEAT OF VAPORIZATION, h_{fg} .



THIS IS THE VARIATION OF THE THERMODYNAMIC QUALITY, x, ALONG THE CHANNEL.

- FOR OUR APPLICATION, THE THERMODYNAMIC QUALITY MAY HAVE POSITIVE OR NEGATIVE VALUES.
- DIFFERENT VALUES OF *x* ARE INTERPRETED AS FOLLOWS:
 - x < 0 : SUBCOOLED LIQUID
 - x = 0 : SATURATED LIQUID
 - 0 < x < 1 : SATURATED STEAM-WATER MIXTURE
 - x = 1 : SATURATED STEAM
 - x > 1 : SUPERHEATED STEAM





$$\begin{aligned} t_{c} &= \frac{t_{i} + t_{e}}{2} + \frac{t_{e} - t_{i}}{2 \sin\beta} \sin 2\beta \frac{z}{H} + \frac{1}{h_{c}s} \frac{P_{c}}{H} \frac{\beta}{\sin\beta} \cos 2\beta \frac{z}{H} \\ \hline \mathbf{P}_{c} &= \dot{m} \, \overline{c}_{p} \left(t_{e} - t_{i} \right) \\ \hline \mathbf{DEFINING:} \\ \gamma &= \frac{h_{c} \, s \, H}{2\beta \, \dot{m} \, \overline{c}_{p}} \\ \hline t_{c} &= \frac{t_{i} + t_{e}}{2} + \frac{t_{e} - t_{i}}{2 \sin\beta} \left(\sin 2\beta \frac{z}{H} + \frac{1}{\gamma} \cos 2\beta \frac{z}{H} \right) \end{aligned}$$

THIS EQUATION GIVES THE VARIATION OF THE OUTSIDE TEMPERA-TURE OF THE CLADDING ALONG THE FUEL CHANNEL.

Table 7.4 Thermal properties of Zircaloy-4

Density	Conductivity	Specific heat	Melting point	Limiting temperature
kg/m ³	W/mK (at °C)	J/kgK (at °C)	°C	°C
6570		328 (300)	1850	40
	13.1 (400)	357 (650)		

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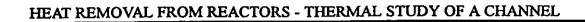
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MAXIMUM CLADDING TEMPERATURE:

$$t_{c} = \frac{t_{i} + t_{e}}{2} + \frac{t_{e} - t_{i}}{2 \sin \beta} \left(\sin 2\beta \frac{z}{H} + \frac{1}{\gamma} \cos 2\beta \frac{z}{H} \right)$$
DERIVATION
$$\frac{d t_{c}}{d z} = \cos 2\beta \frac{z}{H} - \frac{1}{\gamma} \sin 2\beta \frac{z}{H} = 0$$
or
$$\gamma = \tan 2\beta \frac{z}{H}$$
THE MAXIMUM
TEMPERATURE
$$z_{m} = \frac{H}{2\beta} \arctan \gamma$$
THE VALUE OF THE MAXIMUM TEMPERATURE
$$t_{c} = \frac{t_{i} + t_{e}}{2} + \frac{t_{e} - t_{i}}{2 \sin \beta} \left(\sin 2\beta \frac{z}{H} + \frac{1}{\gamma} \cos 2\beta \frac{z}{H} \right)$$

$$t_{max} = \frac{H}{2\beta} \arctan \gamma$$

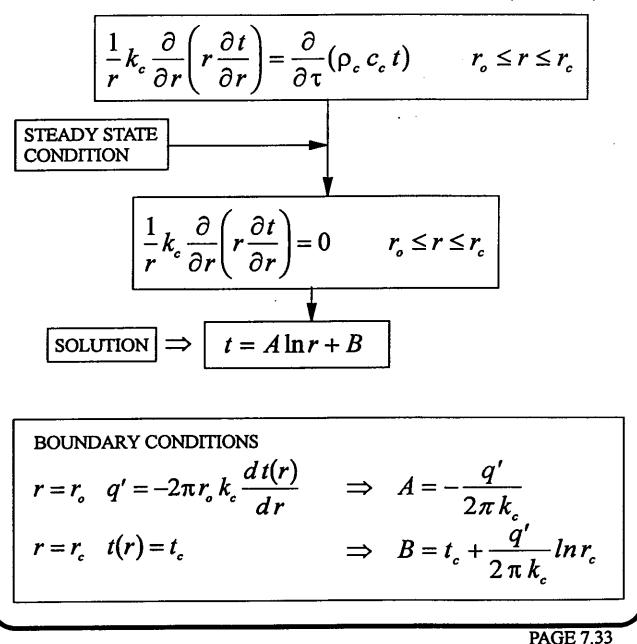
$$t_{cmax} = \frac{t_{i} + t_{e}}{2} + \frac{t_{e} - t_{i}}{2 \sin \beta} \left[\sin(\arctan \gamma) + \frac{1}{\gamma} \cos(\arctan \gamma) \right]$$



MAXIMUM CLADDING TEMPERATURE SHOULD BE LESS THEN 380 - 400 °C.

NORMAL OPERATING TEMPERATURE OF THE CLADDING IS ABOUT 320 °C.

► TEMPERATURE DISTRIBUTION IN THE CLADDING IN THE RADIAL DIRECTION AT A GIVEN AXIAL LOCATION $(k_c = const.)$.



VARIATION OF THE TEMPERATURE THROUGH THE CLADDING :

$$t = t_c + \frac{q'}{2\pi k_c} ln \frac{r_c}{r} \quad with \quad r_o \le r \le r_c$$

TEMPERATURE OF THE INNER SURFACE OF THE CLADDING $(r = r_o)$:

$$t_c' = t_c + \frac{q'}{2\pi k_c} \ln \frac{r_c}{r_c}$$

- GAP CONDUCTANCE BETWEEN FUEL AND CLADDING
 BECAUSE THE LOW HEAT CONDUCTANCE, A LARGE TEMPERATURE DROP OCCURS IN THE GAP REGION (AT THE INTERFACE) BETWEEN THE FUEL AND CLADDING.
 THIS DROP (~ 150 °C) IS SECOND TO THAT IN THE CERAMIC FUEL (URANIUM DIOXIDE).
 DURING THE MANUFACTURING OF THE FUEL RODS, A GAP OF ABOUT 0.08mm IS REQUIRED TO INSERT FUEL PALLETS INTO CLADDING TUBES.
 GRAPHITE POWDER IS ALSO USED (CANDU REACTORS) TO EASE THE INSERTION OF THE PALLETS.
 - FUEL PALLETS ARE LOADED IN AN ATMOSPHERE OF AN INERT GAS (e.g. HELIUM).
 - 1. TO AVOID THE CORROSION, AND
 - 2. TO ASSURE A REASONABLE INITIAL HEAT TRANSFER COEFFICIENT.

GAP CONDUCTANCE BETWEEN FUEL AND CLADDING
THE GAP REGION IS SO NARROW THAT THERE IS NO CON- VECTION CURRENTS IN THE GAS.
 CONSEQUENTLY, AT THE EARLY STAGE, HEAT TRANSFER IN THE GAP REGION IS, ESSENTIALLY, BY CONDUCTION THROUGH THE FILLING GAS (SOME RADIATION HEAT TRANSFER IS ALSO PRESENT)
LATTER, BECAUSE OF THE SWELLING AND THERMAL EX- PANSION OF THE FUEL WHICH IS MORE IMPORTANT TO THAT OF THE CLADDING, THE GAP REGION CLOSES.
 CONSEQUENTLY, DIRECT CONTACT TAKES PLACE BET- WEEN SURFACES AT SEVERAL DISCRETE POINTS.
► THE HEAT TRANSFER IS THEN:
1. BY CONDUCTION AT THESE SOLID-TO-SOLID CONTACT POINTS, AND ALSO
2. BY CONDUCTION THROUGH THE FILLING GAS.

► THE GAP HEAT TRANSFER IS USUALLY EXPRESSED AS:

$$q' = 2\pi r_o h_g \left(t_f - t_c' \right)$$

WHERE h_g is the gap conductance.

► BASED ON THE ABOVE DISCUSSION, THE GAP BETWEEN THE FUEL AND CLADDING IS CLASSIFIED AS:

1. OPEN GAP 2. CLOSED GAP

1. OPEN GAP

- THE FUEL AND CLADDING ARE NOT IN PHYSICAL CONTACT.
 TRUE FOR FRESH FUEL.
- ► THE FUEL STANDS FREELY WITHIN THE CLADDING.
- ► HEAT TRANSFER MECHANISMS ARE:

1. CONDUCTION THROUGH THE FILLING GAS, AND 2. RADIATION.

- ► INITIALLY THE FILLING GAS IS PURE HELIUM.
- LATTER ON FISSION GASES (KRYPTON & XENON) FILL THE GAP REGION AND MIX WITH HELIUM.
- ► THIS ACCUMULATION INCREASES THE PRESSURE IN THE GAP. I.E., THE PRESSURE IN THE FUEL ELEMENT:
- ► TOWARD THE END OF FUEL LIFE

- THE PRESSURE IS ~ 7.5 MPa

- THE COMPOSITION OF THE FILLING GAS: HELIUM, KRYPTON (~15%), XENON (~85%)

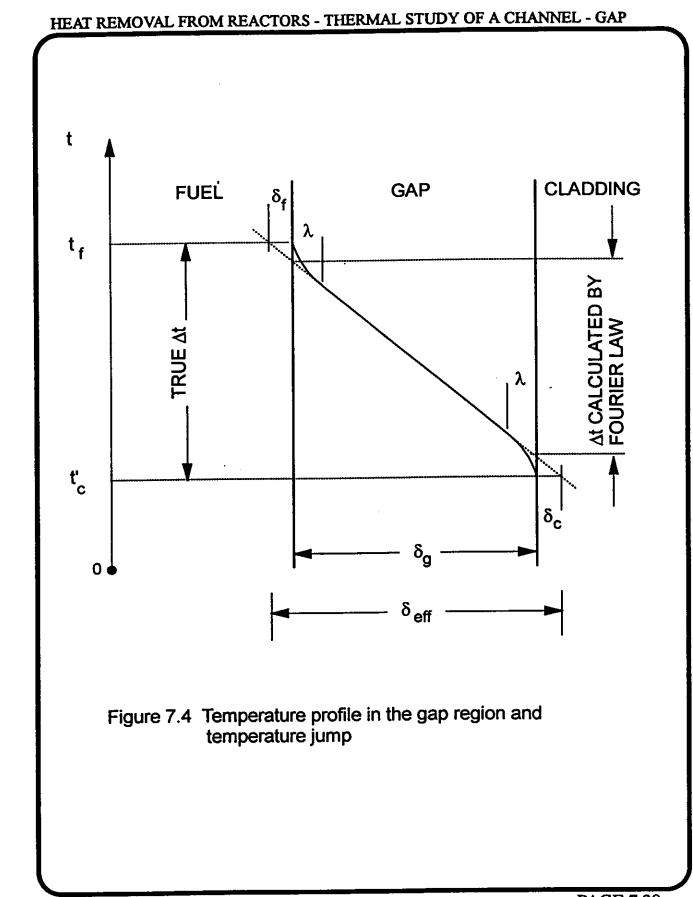
► IF THE GAP CLEARANCE IS MUCH LARGER THEN THE MEAN FREE PATH OF THE ATOMS, THE GAP CONDUCTANCE IS GIVEN BY:

$$h_g = \frac{k_g}{\delta_g} + \frac{\sigma}{\frac{1}{\varepsilon_f} + \frac{1}{\varepsilon_c} - 1} \frac{T_f^4 - T_c'^4}{T_f - T_c'}$$

THE VARIATION OF THE GAS TEMPERATURE IN THE GAP REGION IS SHOWN IN:

FIGURE 7.4

- A STEEP CHANGE IN TEMPERATURES TAKES PLACE IN THE REGIONS CLOSE TO THE SOLID SURFACES.
- ► THE EXTEND OF THE REGION IS ABOUT A MEAN FREE PATH.
- ► THIS STEEP CHANGE IS CALLED "TEMPERATURE JUMP."
- ► TO APPLY PROPERLY THE HEAT CONDUCTION LAW, THE LINEAR PORTION OF THE TEMPERATURE PROFILE SHOULD BE EXTRAPOLATED UNTIL IT CROSSES THE FUEL AND CLADDING TEMPERATURES AT δ_f and δ_c .
- δ_f and δ_c are called "TEMPERATURE JUMP DIS-TANCES"
- THESE DISTANCES SHOULD BE ADDED TO THE ACTUAL GAP THICKNESS TO PREDICT THE CORRECT FUEL-CLADDING TEMPERATURE DIFFERENCE BY USING THE FOURIER CONDUCTION LAW.



HEAT REMOVAL FROM REACTORS - THERMAL STUDY OF A CHANNEL - GAP

THE CONDUCTANCE OF A NARROW GAP (FEW MEAN FREE PATH) IS GIVEN BY:

$$h_g = \frac{k_g}{\delta_g + \delta_f + \delta_c} + \frac{\sigma}{\frac{1}{\varepsilon_f} + \frac{1}{\varepsilon_c} - 1} \frac{T_f^4 - T_c'^4}{T_f - T_c'}$$

KENNARD GIVES THE TEMPERATURE JUMP DISTANCE AS:

$$\delta = 2 \left(\frac{2 - \alpha}{\alpha} \right) \left(\frac{\Gamma}{1 - \Gamma} \right) \left(\frac{k}{\mu c_p} \right) \lambda$$

 λ : MEAN FREE PATH,

 Γ : RATIO OF c_p / c_v for the gases,

 C_p : SPECIFIC HEAT AT CONSTANT PRESSURE,

 C_{v} : SPECIFIC HEAT AT CONSTANT VOLUME,

 μ : VISCOSITY OF THE GAS,

k : CONDUCTIVITY OF THE! POEL

- α is the accommodation coefficient of the Gas IN contact with a solid.
- IT TAKES INTO ACCOUNT THE INCOMPLETE ENERGY IN-TERCHANGE BETWEEN THE GAS MOLECULES AND THE SOLID SURFACE.

► THE ACCOMMODATION COEFFICIENT IS GIVEN BY:

$$\alpha = \frac{T_r - T_i}{T_s - T_i}$$

- T_i :TEMPERATURE OF THE MOLECULES THAT STRIKE THE SOLID,
- T_{\star} : TEMPERATURE OF THE SOLID,
- T_r : TEMPERATURE OF THE REFLECTED MOLECULES.
- α is less than 1.
- $\alpha = 1$, reflected molecules are in Equilibrium with solid.
- SURFACE ROUGHNESS INCREASES THE VALUE OF THE THERMAL ACCOMMODATION COEFFICIENT BY MAKING MULTIPLE COLLISIONS POSSIBLE BETWEEN THE MOLE-CULES AND THE SOLID SURFACE.
- ► THE MEAN FREE PATH, λ , IS GIVEN BY:

$$\lambda = \frac{\lambda_o}{p} \frac{T}{273}$$

T: Absolute temperature (K),

p : PRESSURE (BAR),

 λ_{a} : PROPERTY OF THE GAS.

helium $\lambda_o = 1.74 \times 10^{-5} bar - cm$

xenon $\lambda_a = 3.60 \times 10^{-6} bar - cm$

- MEAN FREE PATH FOR HELIUM AT 1 BAR AND 293 K:

 $\lambda = 0.2 \ \mu m$

- MEAN FREE PATH FOR XENON AT 10 BARS AND 1000 K:

 $\lambda = 0.01 \,\mu m$

THE RADIATION COMPONENT OF THE GAP CONDUCTANCE IS USUALLY SMALL UNDER NORMAL OPERATING CONDI-TIONS, THEREFORE:

$$h_g = \frac{k_g}{\delta_g + \delta_f + \delta_c}$$

- THE GAP WIDTH IS TYPICALLY 80 µm.

- δ_f , δ_c are in the order of magnitude of mean free path; therefore they can be neglected.

- THIS IS TRUE UNTIL THE GAP CLOSES AND THE SOLIDS

CONDUCTIVITY OF THE FILLING GAS IS GIVEN BY:

$$k_g = A \cdot 10^{-6} T^{0.79} W / cm K$$

A IS A CONSTANT.

MAKE CONTACT.

 CONDUCTIVITY FOR A MIXTURE OF TWO GASES IS GIVEN BY:

$$k_{g} = (k_{1})^{x_{1}} (k_{2})^{x_{1}}$$

 k_1 , k_2 : conductivity of the gases

 x_1, x_2 : MOLE FRACTIONS

2. CLOSED GAP

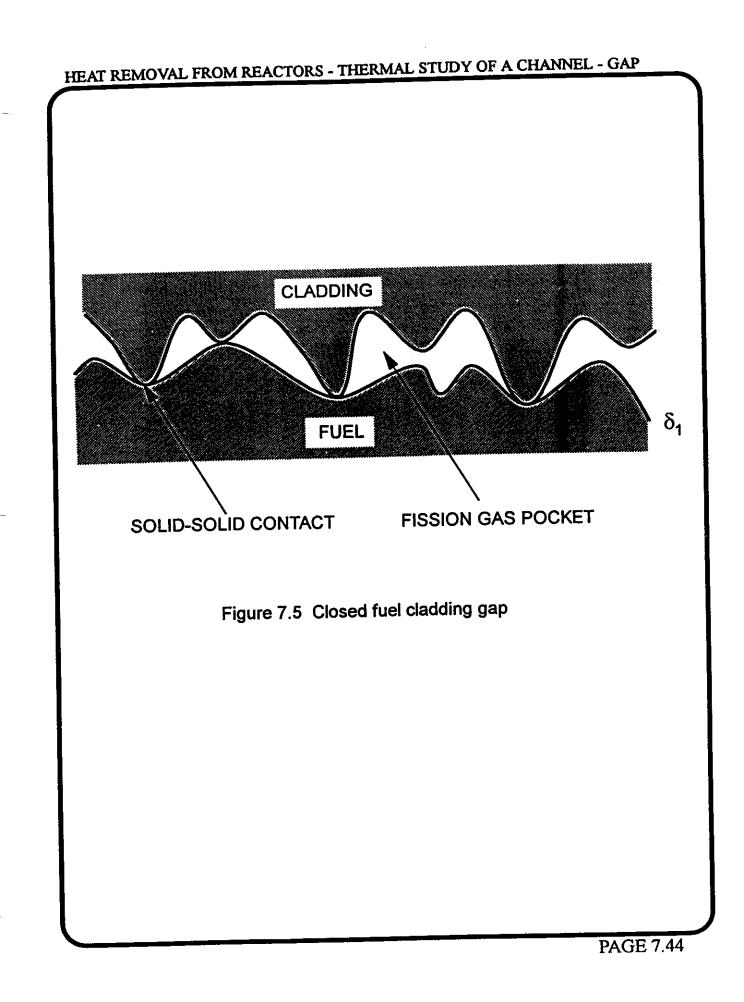
- ► BECAUSE OF:
 - THE FUEL SWELLING,
 - THE DIFFERENTIAL EXPANSION OF THE FUEL, AND
 - PRESSURE EXERTED BY THE COOLANT ON THE OUTSIDE SURFACE OF THE CLADDING THE GAP TENDS TO CLOSE
- ► IN TURN
 - PRESSURE BUILD-UP IN THE GAP REGION DUE TO THE ACCUMULATION OF THE FISSION GASES, AND
 - FUEL DIAMETER REDUCTION DUE TO THE FUEL DENSIFICATION

THE GAP TENDS TO OPEN.

- THE EFFECTS THAT CLOSE THE GAP ARE MORE IMPORTANT THAN THOSE THAT OPEN THE GAP.
- CONSEQUENTLY THE GAP THICKNESS IS CONSIDERABLY REDUCED.
- BECAUSE OF THE ROUGHNESS OF THE SURFACES, SOLID-TO-SOLID CONTACT BETWEEN THE FUEL AND CLADDING IS ESTABLISHED AT HIGH POINTS.
- UNDER THIS CONDITION, HEAT TRANSFER IN THE GAP REGION OCCURS:
 - 1. THROUGH THE POINTS OF SOLID CONTACT,
 - 2. ACROSS THE NOW DISCONTINUOUS GAS GAP BETWEEN THESE POINTS OF CONTACT.

REFER TO FIGURE 7.5

iens as





- FOR A CLOSED GAP, DIFFERENT COMPONENTS OF THE CONDUCTANCE ARE:
 - 1. GAS CONDUCTANCE THROUGH DISCONTINUOUS GAP,
 - 2. CONDUCTION THROUGH THE SOLID-TO-SOLID CONTACT POINTS,
 - 3. RADIATION THROUGH THE DISCONTINUOUS GAP.
- CONDUCTANCE DUE TO SOLID-TO-SOLID CONTACT IS GIVEN BY:

$$h_s = A \frac{2k_f k_c}{k_f + k_c} \frac{p_i}{H \delta^{1/2}}$$

A : DIMENSIONAL CONSTANT, $m^{1/2} (= 10 m^{1/2})$

- k_f : CONDUCTIVITY OF THE FUEL, $W/m^{\circ}C$
- k_c : Conductivity of the cladding, $W/m \ ^{\circ}C$

 p_i : SURFACE CONTACT PRESSURE, N/m^2

- H : MEYER HARDNESS NUMBER OF THE SOFTER MATERIAL, N / m^2
- $\delta\,$: RMS of contact material surface roughness and given by:

$$\delta = \left[\left(\delta_1^2 + \delta_2^2 \right) / 2 \right]^{1/2} \quad m$$

 δ_1, δ_2 : SURFACE ROUGHNESS OF THE INTERFACE MATERIAL, *m*.

GAP CONDUCTANCE THROUGH DISCONTINUOUS GAP WAS GIVEN BY:

$$h_g = \frac{k_g}{\delta_g + \delta_f + \delta_c}$$

- THE THICKNESS OF A CLOSED GAP IS RELATED TO THE SURFACE THICKNESS AS: ROUGHNESS

$$\delta_g = C(\delta_1 + \delta_2)$$

C IS A CONSTANT GIVEN BY:

$$C = 2.75 - 2.55 \times 10^{-8} p_i$$

 p_i is the pressure at the interface in N/m^2 .

- TAKING INTO CONSIDERATION THE VALUE OF δ_g THE GAP CONDUCTANCE BECOMES:

$$h_g = \frac{k_g}{C(\delta_1 + \delta_2) + \delta_f + \delta_c}$$

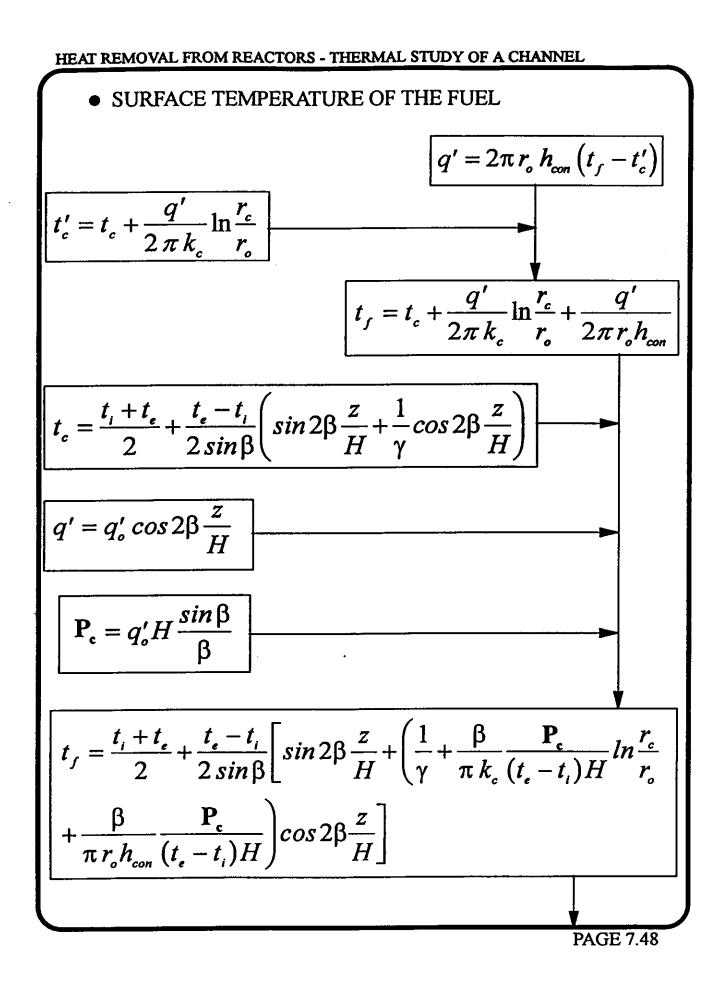
TEMPERATURE JUMP DISTANCES FOR VARIOUS GASES

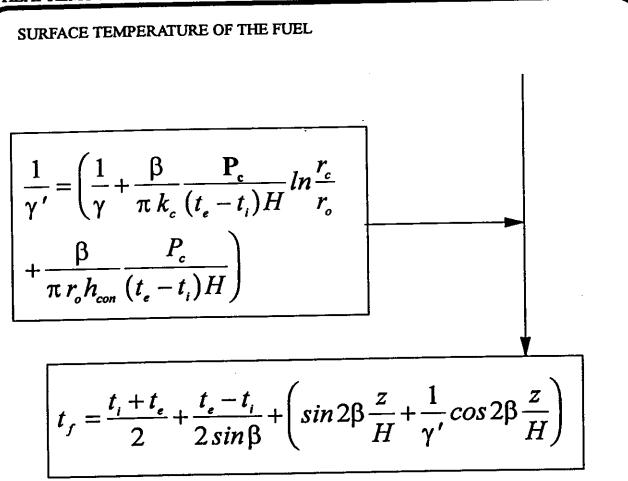
Gas	$\delta_f + \delta_c$, m	Temperature range, °C		
Helium	10×10 ⁻⁶	150-250		
Argon	5×10^{-6}	180-320		
Krypton	1×10^{-6}	180-330		
Xenon	1×10^{-6}	180-330		

HEAT REMOVAL FROM REACTORS - THERMAL STUDY OF A CHANNEL - GAP

THE TOTAL CONDUCTANCE OF A CLOSED GAP IS GIVEN BY:

$$\begin{aligned} h_{con} &= h_s + h_g + h_r \\ &= A \frac{2k_f k_c}{k_f + k_c} \times \frac{p_i}{H\delta^{1/2}} + \frac{k_g}{C(\delta_1 + \delta_2) + \delta_f + \delta_c} \\ &+ \frac{\sigma}{\frac{1}{\epsilon_f} + \frac{1}{\epsilon_c} - 1} \times \frac{T_f^4 - T_c'^4}{T_f - T_c'} \end{aligned}$$





► THE MAXIMUM TEMPERATURE OCCURS AT:

$$z_m = \frac{H}{2\beta} \arctan \gamma'$$

THE VALUE OF THE MAXIMUM TEMPERATURE OF THE FUEL SURFACE IS:

$$t_{fmax} = \frac{t_i + t_e}{2} + \frac{t_e - t_i}{2\sin\beta} \sqrt{1 + \left(\frac{1}{\gamma'}\right)^2}$$

• TEMPERATURE DISTRIBUTION IN THE FUEL

NOW WE WILL DISCUSS:

- 1. THE DISTRIBUTION OF RADIAL TEMPERATURES IN THE FUEL, AND
- 2. THE VARIATION OF THE FUEL CENTERLINE TEMPERATURE ALONG THE CHANNEL.

IN THE DETERMINATION OF THE RADIAL TEMPERATURE DIS-TRIBUTION THE FOLLOWING ASSUMPTIONS WILL BE MADE:

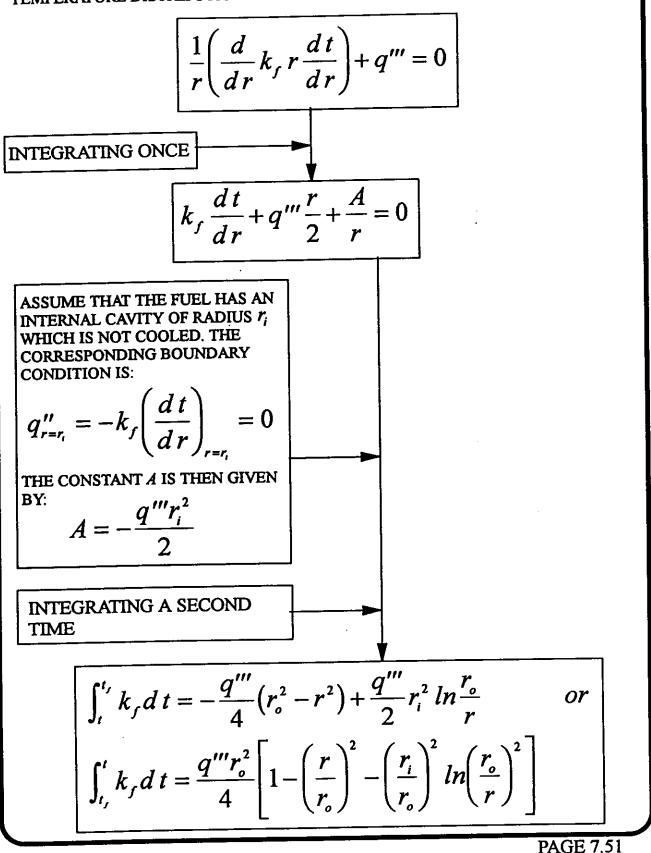
- 1. UNIFORM NEUTRON FLUX (POWER DENSITY) WITHIN THE FUEL.
- 2. NO ANGULAR VARIATION IN THE CONVECTIVE HEAT TRANSFER COEFFICIENT AND GAP CONDUCTANCE, I.E., NO ANGULAR TEMPERATURE GRADIENT.
- 3. AXIAL HEAT CONDUCTION IS SMALL COMPARED TO THAT IN THE RADIAL DIRECTION.
- 4. STEADY STATE CONDITIONS PREVAIL.
- UNDER ABOVE CONDITIONS, HEAT CONDUCTION EQUA-TION:

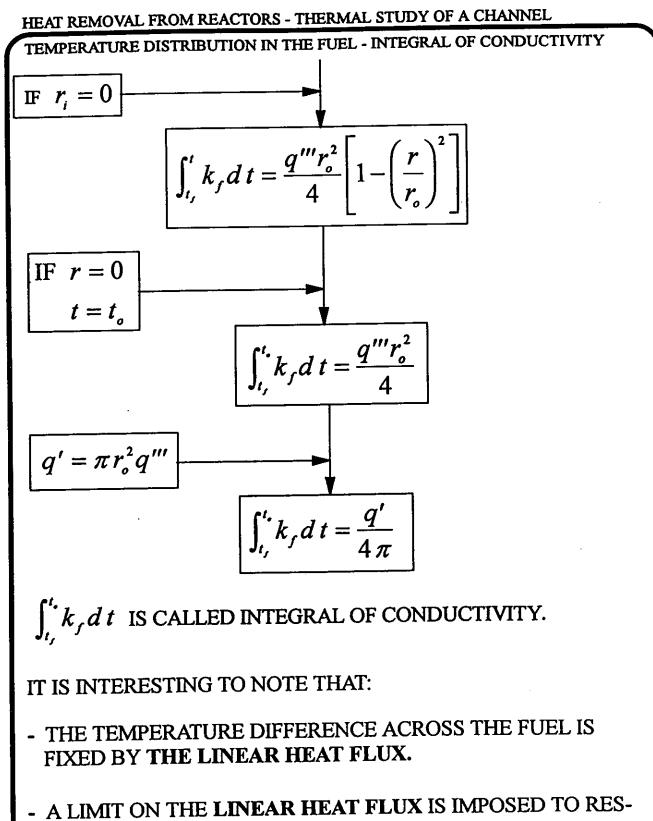
$$\frac{1}{r}\frac{\partial}{\partial r}\left(k_{f}r\frac{\partial t}{\partial r}\right)+q^{\prime\prime\prime}=\frac{\partial}{\partial \tau}\left(\rho_{f}c_{f}t\right)\qquad 0\leq r\leq r_{o}$$

BECOMES:

$$\frac{1}{r}\left(\frac{d}{dr}k_{f}r\frac{dt}{dr}\right) + q^{\prime\prime\prime} = 0$$

TEMPERATURE DISTRIBUTION IN THE FUEL





PECT THE MAXIMUM TEMPERATURE.

TEMPERATURE DISTRIBUTION IN THE FUEL - INTEGRAL OF CONDUCTIVITY

$$\int_{t_f}^{t_f} k_f dt = \frac{q'}{4\pi}$$

PROPERTIES OF "THE CONDUCTIVITY INTEGRAL:"

- 1. IT IS DIRECTLY RELATED TO THE LINEAR POWER OF THE FUEL.
- 2. IT CAN BE DETERMINED EXPERIMENTALLY.
- 3. CENTER LINE TEMPERATURE OF THE FUEL t_o IS INDEPENDENT OF THE ROD DIAMETER.
- 4. THE UPPER LIMIT OF THE INTEGRAL CAN BE TAKEN AS A VARIABLE - THE DIFFERENTIATION YIELDS THE THERMAL CONDUCTIVITY.
- 5. THE CONDUCTIVITY INTEGRAL CAN BE WRITTEN AS:

$$\int_{t_{f}}^{t_{*}} k_{f} dt = \int_{0}^{t_{*}} k_{f} dt - \int_{0}^{t_{f}} k_{f} dt$$

I.E., NORMALIZED TO 0 °C.

6. THE CONDUCTIVITY INTEGRAL CAN BE USED TO DETERMINE CENTERLINE TEMPERATURE OF THE FUEL.

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-METALLIC

1. METALLIC FUELS

- URANIUM METAL IS A VERY POOR FUEL.
- SUBSTANTIAL DIMENSIONAL CHANGES UNDER IRRADIATION AND THERMAL CYCLING (UP TO 60% OF THE ORIGINAL LENGTH).
- THIS CHANGE IS DUE TO " α -PHASE" PRESENT UNDER 665 °C.
- " α -PHASE" IS ANISOTROPIC.
- CONSEQUENTLY, FUEL ROD:
 - EXPANDS IN THE AXIAL DIRECTION. CONTRACTS IN THE RADIAL DIRECTION.
- CONSEQUENCE:

CLADDING FAILURE, AND EXPOSITION OF THE FUEL TO THE COOLANT.

- STRONG CHEMICAL REACTION BETWEEN FUEL AND COOLANT.
- AT 290 °C, EXPOSED FUEL IS DESTROYED IN FEW HOURS.
- ALLOYING MATERIALS (Zr, Cr, Mo, Fe, etc.) IMPROVE THE DIMEN-SIONAL STABILITY BUT THEY INCREASE PARASITIC NEUTRON ABSORPTION.

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-METALLIC

- URANIUM METAL IS UNFIT FOR USE IN BWR, PWR, CANDU REACTORS.
- CONDUCTIVITY OF THE URANIUM METAL VARIES MODERATELY WITH TEMPERATURE.
- THE CONDUCTIVITY OF A PURE URANIUM METAL AS A FUNCTION OF TEMPERATURE IS GIVEN BY:

$$k_f = 25.58 + 1.75 \left(\frac{t}{100}\right) + 0.018 \left(\frac{t}{100}\right)^3 \quad W / m \ ^{\circ}C$$

t in $^{\circ}C$

- IN THE DETERMINATION OF THE FUEL CENTERLINE TEMPERA-TURE, THE CONDUCTIVITY OF THE URANIUM METAL CAN BE TAKEN AS CONSTANT.

SEE

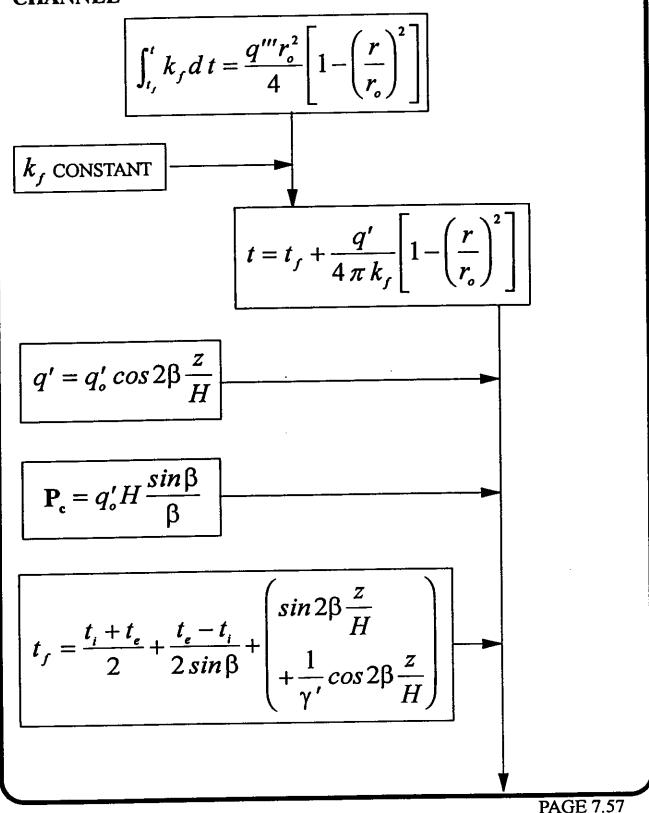
Table 7.6 Conductivity of fuel materials

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS

Table 7.6 Conductivity of fuel materials

Température	Uranium	U02	Thorium	Th02	UC
°F	к _с =	K _c = Btu/hr pd ^o F			•
200	15.80	4.5	21.75	7.29	14.77
300	16.40	-	22.18	6.25	14.07
· 400	17.00	3.5	22.60	5.34	13.48
500	17.50	-	23.00	4.61	13.02
600	18.10	2.8	23.45	4.03	12.67
700	18.62	-	23.90	3.59	12.39
. 800	19.20	2.5	: 24.30	3.21	12.19
900	19.70	-	24.65	2.91	12.02
1 000	20.25	2.2	25.75	2.68	11.91
1 100	20.75	- ·	25.60	2.47	• •
1 200	21,20	2.0	26.13	2.30	11.82
1 300	21.60	-	-	2.17	
1 400	22.00	1.6	· _	2.07	11.76
1 600		1.5	-	1.90	11.70
1 800	_	1.4	-	1.80	11.67
2 000	_	1.3	-	1.70	11.57
	_	1.2	• ••	1.69	-
2 200 2 400	_	1.1	_	1.68	-
	_	1.1	-	-	_ '
2 600 3 200	 -	1.1	-	-	-
3 200	-				

CENTERLINE TEMPERATURE OF THE FUEL ALONG THE CHANNEL



CENTERLINE TEMPERATURE OF THE FUEL ALONG THE CHANNEL

$$t_{o} = \frac{t_{i} + t_{e}}{2} + \frac{t_{e} - t_{i}}{2 \sin\beta} \left(\sin 2\beta \frac{z}{H} + \frac{1}{\gamma''} \cos 2\beta \frac{z}{H} \right)$$

.

WHERE:

$$\frac{1}{\gamma''} = \frac{1}{\gamma'} + \frac{\beta}{2\pi k_f} \frac{\mathbf{P_e}}{(t_e - t_i)H}$$

MAXIMUM CENTERLINE TEMPERATURE IS LOCATED AT:

$$z = \frac{H}{2\beta} \arctan \gamma''$$

MAXIMUM CENTERLINE TEMPERATURE IS:

$$t_{omax} = \frac{t_i + t_e}{2\sin\beta} + \frac{t_e - t_i}{2\sin\beta} \sqrt{1 + \left(\frac{1}{\gamma''}\right)^2}$$

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS - CERAMIC

II. CERAMIC FUELS

- URANIUM DIOXIDE A CERAMIC MATERIAL IS WIDELY USED IN POWER REACTORS.
- ADVANTAGES:
 - ► DIMENSIONAL STABILITY.
 - ► ADEQUATE RESISTANCE TO RADIATION.
 - ► HIGH MELTING POINT: ~ 2800 ° C.
 - ► NO CHEMICAL REACTION WITH HOT LIGHT OR HEAVY WATER (VERY IMPORTANT FUTURE).
 - ► HIGH RETENTION CAPABILITY FOR FISSION GASES FOR FUEL TEMPERATURES LESS THAN 1000 ° C.

- DISADVANTAGES:

- ► LOW THERMAL CONDUCTIVITY, I.E., HIGH TEMPE-RATURE GRADIENT WITHIN FUEL: (10⁶ °C/cm).
- ► HIGH CENTERLINE TEMPERATURE: 2000-2400 ° C.

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

- FABRICATION
 - CYLINDRICAL FUEL PELLETS ARE MANUFACTURED BY COMPACTING UNDER PRESSURE A FINELY GROUND URANIUM DIOXIDE POWDER.
 - PELLETS ARE THEN SINTERED IN A NEUTRAL AT-MOSPHERE AT ABOUT 1700 ° C.
 - ► BY CONTROLLING THE SINTERING CONDITIONS, FUEL OF DENSITY BETWEEN 80% AND 98% OF THE THEORETICAL DENSITY CAN BE PRODUCED.
 - PELLETS ,AFTER GRINDING, ARE INSERTED IN A ZIRCALLOY TUBING AND SEALED BY WELDING THE END CAP.

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

- RESTRUCTURING

- DURING IRRADIATION, UNDER THE EFFECT OF HIGH TEMPERA-TURES AND TEMPERATURE GRADIENTS, UO₂ FUEL PELLETS UNDERGO CHANGES IN THE MORPHOLOGY.
- THESE HIGH TEMPERATURES AND GRADIENTS PRODUCE A RAPID DIFFUSIONS OF THE OXIDES TOWARD THE LOW TEMPE-RATURE REGIONS AND THE VOIDS (PORES) TOWARD THE HIGH TEMPERATURE CENTER REGION.
- THE RESULT IS THE RESTRUCTURING OF THE FUEL PELLET INTO CHARACTERISTIC ZONES:

REFER TO FIGURE 7.6

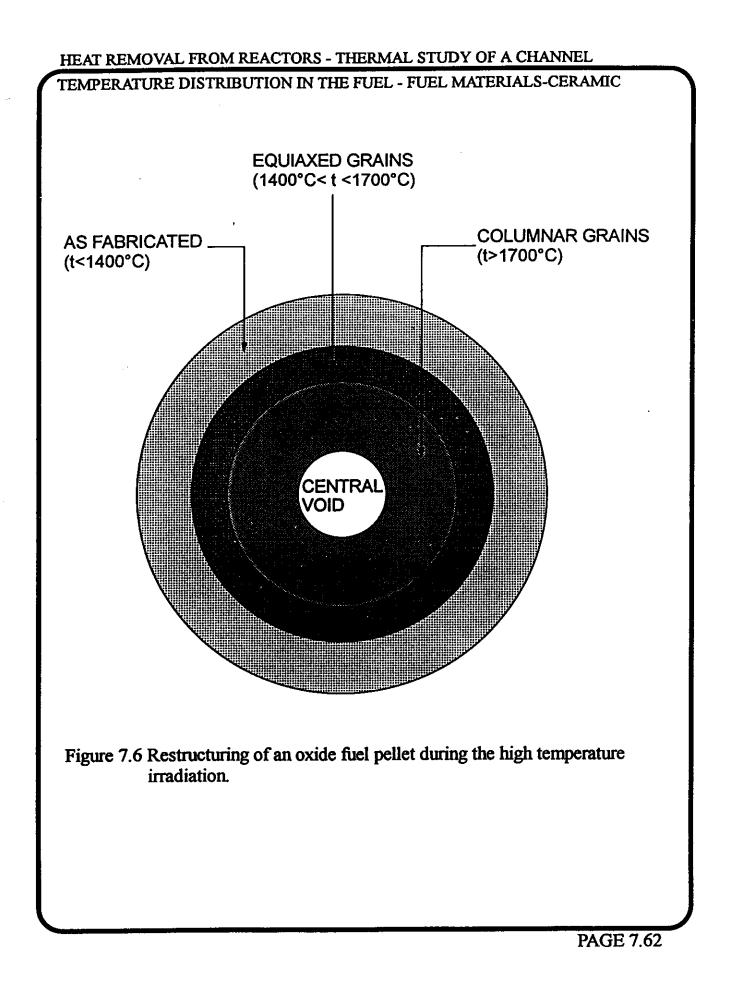
- UNCHANGED REGION WHERE THE TEMPERATURES ARE LOW AND INITIAL FINE GRAIN STRUCTURE IS KEPT.
- EQUIAXED GRAINS REGION WHERE THE INITIAL FINE GRAINS HAVE GROWN MANY TIMES OF THEIR ORIGINAL SIZE.

IN THIS REGION THE TEMPERATURE IS THE SIGNIFICANT PARAMETER.

► COLUMNAR GRAINS REGION WHERE THE BOUNDARIES OF GRAINS THE ARE DELINEATED BY FINE RADIAL STREAKS OF MIGRA-TING PORES OR FISSION GAS BUBBLES.

IN THIS REGION THE TEMPERATURE GRADIEN IS THE SIGNI-FICANT PARAMETER.

 THE FORMATION OF A CENTRAL VOID IS ALSO POSSIBLE TO ACCOMMODATE THE MIGRATING VOIDS (PORES).



TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

• UNDER THE NORMAL OPERATING CONDITIONS OF WATER COOLED REACTORS ONLY UNCHANGED AND EQUIAXED RE-GIONS ARE OBSERVED.

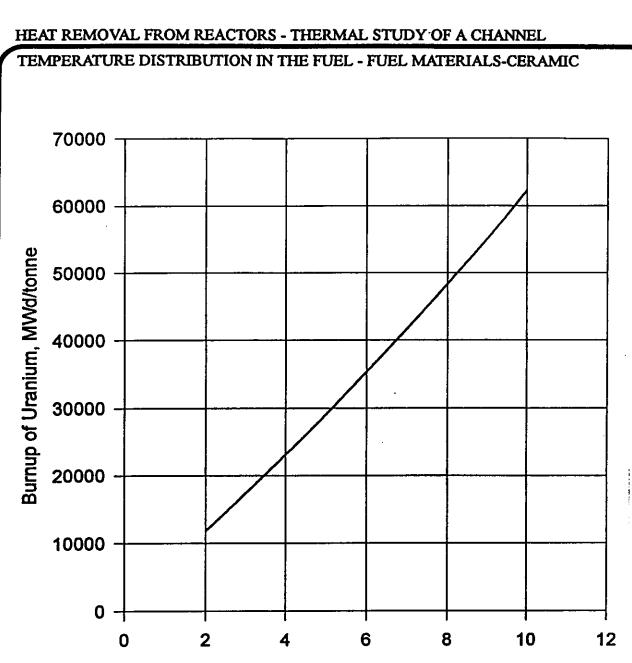
- CRACKING

- ► LARGE THERMAL GRADIENTS IN THE FUEL LEAD TO THER-MAL STRESSES.
- THE CONSEQUENCE IS THE FORMATION OF RADIAL CRACKS.
- ► THESE CRACKS DON'T AFFECT THE PERFORMANCE OF THE FUEL IF THE PELLETS ARE SUITABLY RESTRAINED BY THE CLADDING.

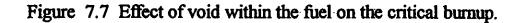
TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

- SWELLING

- CONSTITUTE A MAJOR LIMITATION ON THE PERFORMANCE OF THE URANIUM DIOXIDE FUEL.
- THE SWELLING IS THE CONSEQUENCE OF THE FORMATION OF TWO FISSION PRODUCT ATOMS (MAINLY GASEOUS ONES) FOR EVERY FISSILE ATOM.
- ► AT LOW AND MODERATE BURNUPS SWELLING IS NOT SIGNI-FICANT AND VARIES LINEARLY WITH BURNUP.
- ABOVE A CRITICAL BURNUP, SWELLING BECOMES IMPOR-TANT AND LEADS TO UNACCEPTABLE DIMENSIONAL CHANGES.
- ► CRITICAL BURNUP CAN BE INCREASED BY:
 - 1. DECREASING SLIGHTLY THE DENSITY OF THE URA-NIUM DIOXIDE, I.E., INCREASING THE POROSITY, AND
 - 2. PROVIDING MORE CLADDING RESTRAIN.
- ► **FIGURE 7.7** SHOWS THE EFFECT OF THE VOID (PORES) WITHIN THE FUEL ON THE CRITICAL BURNUP.
- CRITICAL BURNUP ALSO DEPENDS ON THE OPERATING TEMPERATURE OF THE FUEL.



% of Void Volume



TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

THERMAL CONDUCTIVITY OF URANIUM DIOXIDE

- THE PROPERTIES OF URANIUM DIOXIDE IN GENERAL AND ITS CONDUCTIVITY IN PARTICULAR HAVE BEEN EXTEN-SIVELY STUDIED.
- ► HOWEVER, THE CONDUCTIVITY OF *UO*₂ IS NOT KNOWN ACCURATELY.
- ► THE CONDUCTIVITY OF CERAMIC FUEL DEPENDS ON:
 - 1. TEMPERATURE,
 - 2. POROSITY (DENSITY),
 - 3. U/O RATIO, AND
 - 4. FUEL BURNUP.
- ► THE RELATIVE DENSITY OF UO, IS AROUND 95%.
- ► THE RELATIVE DENSITY IS DEFINED AS THE RATIO OF THE TRUE DENSITY TO THE THEORETICAL DENSITY:

$$\rho_{\kappa} = \frac{\rho}{\rho_{TH}}$$

► THEORETICAL DENSITY, ρ_{TH} , IS THE DENSITY OF THE PORLESS SOLID.

► THE THEORETICAL DENSITY OF UO_2 IS 1097 kg / m^3 .

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

(THERMAL CONDUCTIVITY OF URANIUM DIOXIDE)

- ► BY CONTROLLING THE SINTERING CONDITIONS, THE RELA-TIVE DENSITY CAN BE VARIED.
- ► THE CONDUCTIVITY OF POROUS MATERIALS DEPENDS ON THE RELATIVE DENSITY AND INCREASES WITH INCREAS-ING RELATIVE DENSITY (OR DECREASING POROSITY).
- HENCE, HIGH RELATIVE DENSITY (LOW POROSITY) IS DESIRABLE TO MAXIMIZE THE CONDUCTIVITY.
- ► HOWEVER, LOW POROSITY INCREASES THE SWELLING DUE TO THE FISSION GASES AND DEFORMS THE FUEL.
- TO ACCOMMODATE THE FISSION GASES SOME POROSITY (ABOUT 5%) IS REQUIRED.
- ► THE POROSITY IS DEFINED AS:

$$\alpha = \frac{V_p}{V} = \frac{V - V_s}{V}$$

V : TOTAL VOLUME OF THE PELLET

- V_p : VOLUME OF THE PORES
- V_{s} : VOLUME OF THE SOLID

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

(THERMAL CONDUCTIVITY OF URANIUM DIOXIDE)

► DENSITY OF THE OXIDE FUEL:

$$\rho = \rho_s(1-\alpha) + \rho_g \alpha$$

KNOWING THAT:

$$\rho_{g} \alpha << \rho_{s} (1-\alpha)$$

$$\rho_{s} = \rho_{rp}$$

WE CAN ALSO WRITE FOR THE POROSITY:

$$\alpha = 1 - \frac{\rho}{\rho_{TD}} \iff \text{POROSITY}$$

 ρ / ρ_{TD} is the relative density.

THE EFFECT OF THE POROSITY ON THE CONDUCTIVITY IS GIVEN BY THE MAXWELL-EUCKEN FORMULA:

$$k = \frac{1-\alpha}{1+\beta\alpha} k_{TD}$$

k : CONDUCTIVITY OF THE POROUS FUEL.

 $k_{\tau p}$: CONDUCTIVITY AT THEORETICAL DENSITY.

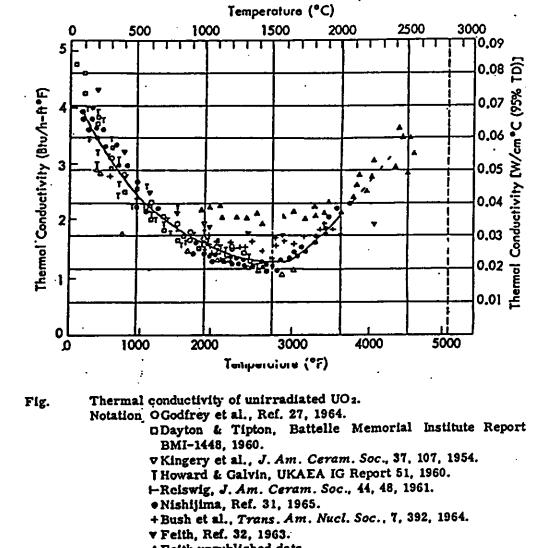
 β : PORE SHAPE FACTOR; $\beta = 0.5$ FOR FUEL OF RELATIVE DENSITY 0.9 AND ABOVE; $\beta = 0.7$ FOR FUEL OF LOW-ER DENSITY.

PAGE 7.68

ويوابد والمربية بالمتعمون والمتعادية والمتعادين والمراج

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC (THERMAL CONDUCTIVITY OF URANIUM DIOXIDE)

- DATA ON THE THERMAL CONDUCTIVITY OF UNIRRADIAT-ED URANIUM DIOXIDE IS A A FUNCTION OF TEMPERATURE IS SHOWN IN THE FIGURE BELOW.
- DATA FROM DIFFERENT SOURCES WERE CORRECTED TO 95% DENSITY.



A Feith unpublished data.

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC (THERMAL CONDUCTIVITY OF URANIUM DIOXIDE)

- ► DESPITE THIS CORRECTION THE DATA IS STILL DISPERSED.
- THIS DISPERSION CAN BE SOMEWHAT REDUCED BY USING THE MAXWELL-EUCKEN FORMULA.
- AN OTHER CAUSE OF THE DISPERSION IS THE O/U RATIO WHICH VARIES BETWEEN 1.8 AND 2.2.
- THE CONDUCTIVITY OF URANIUM DIOXIDE INCREASES WHEN O/U IS REDUCED AND VICE VERSA.
- THE CONDUCTIVITY OF URANIUM DIOXIDE DECREASES WITH BURNUP.
- ► FOR AN UNIRRADIATED URANIUM DIOXIDE OF 95% THEORETICAL DENSITY THE CONDUCTIVITY IS GIVEN BY:

 $k_{95\%} = \frac{38.24}{402.4 + t} + 6.125 \times 10^{-13} (t + 273)^3 \quad W / cm^{\circ}C$

t IS IN ℃.

and the second sec

TO APPLY THIS CORRELATION TO OTHER DENSITY RATIOS THE FOLLOWING CORRECTION SHOULD BE DONE:

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$$\frac{k}{k_{\text{95%}}} = \frac{1.025}{0.95} \frac{1 - \alpha}{1 - \alpha\beta}$$

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

(THERMAL CONDUCTIVITY OF URANIUM DIOXIDE)

 A CORRELATION WHICH TAKES INTO ACCOUNT THE BURNUP EFFECT AS WELL AS THE DENSITY EFFECT IS GIVEN BY:

$$k = \frac{(1-\alpha)}{(1+\alpha\beta)} (0.067 + 1.086 \times 10^{-4} T + \frac{3.6}{T} + \frac{28.8}{T^2} + 11.13 \frac{F}{T})^{-1} W/m^{\circ}C$$

$$T = 1.8t + 491.7 ; t in ^{\circ}C$$

$$F : burnup (fission/cm^3) \times 10^{-20}$$

 ONCE THE DEPENDENCE OF THE URANIUM DIOXIDE CON-DUCTIVITY ON TEMPERATURE IS KNOWN THE FOLLOWING EQUATIONS:

$$\int_{t_f}^t k_f dt = \frac{q^{\prime\prime\prime} r_o^2}{4} \left[1 - \left(\frac{r}{r_o}\right)^2 - \left(\frac{r_i}{r_o}\right)^2 \ln\left(\frac{r_o}{r}\right)^2 \right]$$

OR

$$\int_{t_{f}}^{t} k_{f} dt = \frac{q''' r_{o}^{2}}{4} \left[1 - \left(\frac{r}{r_{o}}\right)^{2} \right]$$

CAN BE EASILY INTEGRATED TO OBTAIN AN EQUATION WHOSE SOLUTION WILL YIELD THE TEMPERATURE PROFILE IN THE FUEL.

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC

DETERMINATION OF THE CONDUCTIVITY OF URANIUM DIOXIDE

- IT IS DIFFICULT TO CONDUCT EXPERIMENTS TO DETER-MINE THE CONDUCTIVITY OF URANIUM DIOXIDE.
- THE CONDUCTIVITY CAN BE DETERMINED BY INSERTING THERMOCOUPLES AT DIFFERENT RADIAL POSITIONS IN THE FUEL.
- THIS IS NOT AN EASY TASK.
- THE MEASUREMENTS ARE SUBJECT TO HIGH DEGREE OF UNCERTAINTY BECAUSE OF:
 - ► THE LOW THERMAL CONDUCTIVITY, AND
 - ► HIGH TEMPERATURE GRADIENTS.
- A MORE CONVENIENT WAY IS TO MEASURE:
 - ► THE CENTER TEMPERATURE, AND
 - ► FUEL SURFACE TEMPERATURE.
 - THE LATTER TEMPERATURE CAN ALSO BE CALCULATED FROM:
 - COOLANT TEMPERATURE,
 - LOCAL HEAT GENERATION RATE , AND
 - ESTIMATED HEAT TRANSFER COEFFICIENT.
 - THE MEASUREMENT IS, THEREFORE, THE INTEGRAL OF CONDUCTIVITY.

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC (DETERMINATION OF THE CONDUCTIVITY OF URANIUM DIOXIDE)

- A THIRD METHOD ID BASED ON THE INDIRECT DETERMI-NATION OF THE OF THE FUEL CENTER TEMPERATURE BY TYING IT :
 - ► TO THE MELTING POINT (2880 °C), OR

TO THE OBSERVABLE CHANGE IN THE URANIUM DIO-XIDE STRUCTURE SUCH AS GRAIN PATTERN MODIFI-CATION:

- EQUIAXED (~1500 °C), OR
- COLUMNAR (~1800 °)
- THE VALUE OF THE INTEGRAL OF CONDUCTIVITY FROM 0 °C TO MELTING POINT FOR A URANIUM DIOXIDE PELLET OF 95% IS:

$$\int_{0}^{2865} k \, dt = 93.5 \quad W / cm$$

TEMPERATURE DISTRIBUTION IN THE FUEL - FUEL MATERIALS-CERAMIC CONDUCTIVITY OF URANIUM DIOXIDE

• THE DEPENDENCE OF THE INTEGRAL OF CONDUCTIVI-TY ON TEMPERATURE IS GIVEN IN:

FIGURE 7.9

• USING FIGURE 7.9 AND THE FOLLOWING EQUATION,

$$\int_{0}^{t} k \, dt - \int_{0}^{t} k \, dt = \frac{q'}{4\pi}$$

THE FUEL CENTER LINE TEMPERATURE IS DETERMINED AS FOLLOWS:

► FROM FIGURE 7.9 AND THE SURFACE TEMPERATURE OF THE FUEL PELLET DETERMINE THE INTEGRAL:

$$\int_0^t k \, dt$$

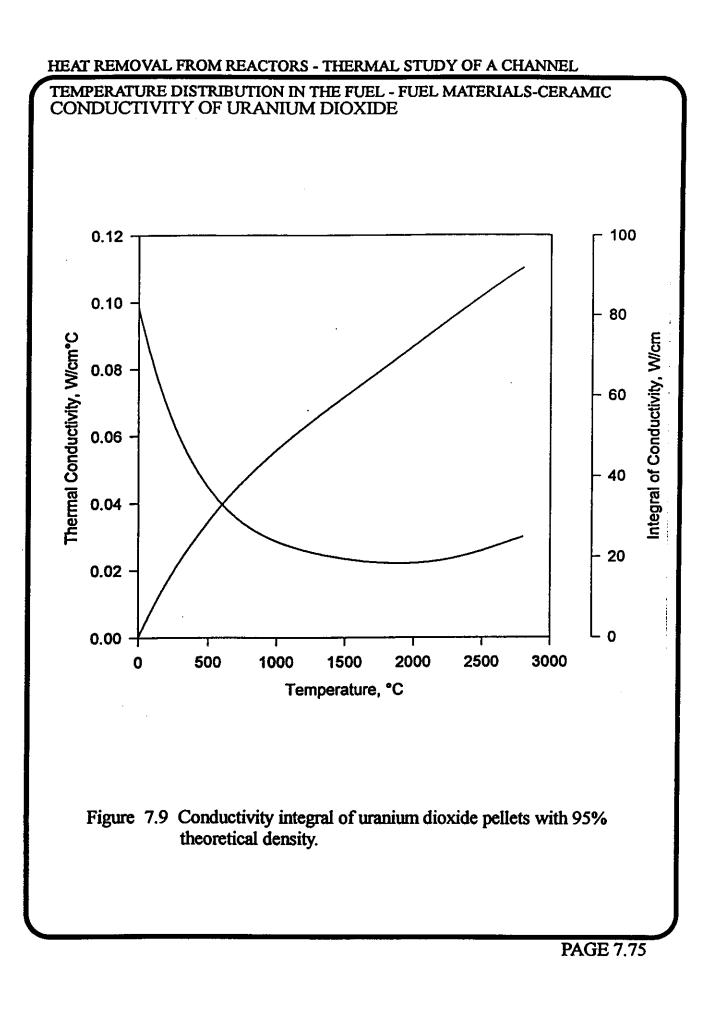
► SINCE q' IS KNOWN, DETERMINE FROM

$$\int_{0}^{t} k \, dt - \int_{0}^{t} k \, dt = \frac{q'}{4\pi}$$

THE INTEGRAL:

$$\int_0^t k \, dt$$

► USING FIGURE 7.9 DETERMINE THE CENTER LINE TEMPE-RATURE OF THE FUEL PELLET.



TEMPERATURE DISTRIBUTION IN THE FUEL WITH NEUTRON DEPRESSION

TEMPERATURE DISTRIBUTION IN A FUEL ROD WITH NEUTRON DEPRESSION

- IN A FUEL ROD THE HEAT GENERATION RATE IS RE-DUCED WHEN PROGRESSED TOWARDS ITS CENTER.
- THIS IS DUE TO THE FACT THAT THE THERMALISATION OF THE FAST NEUTRONS TAKES PLACE IN THE MODE-RATOR.
- THERMAL NEUTRON ENTERING THE FUEL ARE FIRST ABSORBED BY THE OUTER PART OF THE FUEL.
- CONSEQUENTLY, THE NEUTRON FLUX IS LOWER IN THE CENTER.
- THE DISTRIBUTION OF THERMAL NEUTRONS WITHIN THE FUEL IS GIVEN BY:

$$\phi = \phi_o I_o(\kappa r)$$

I. : MODIFIED BESSEL FUNCTION OF THE FIRS KIND AND ZERO ORDER. FIGURE ON PAGE 7,7

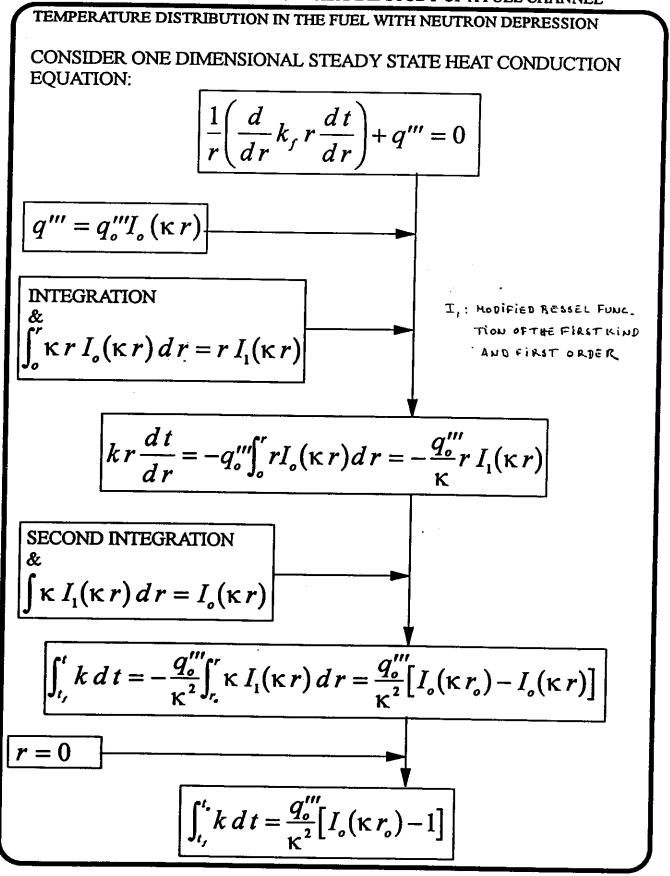
 ϕ_{a} : thermal neutron flux on the center line of the fuel

 I_{a} : zero order modified Bessel function of the first kind

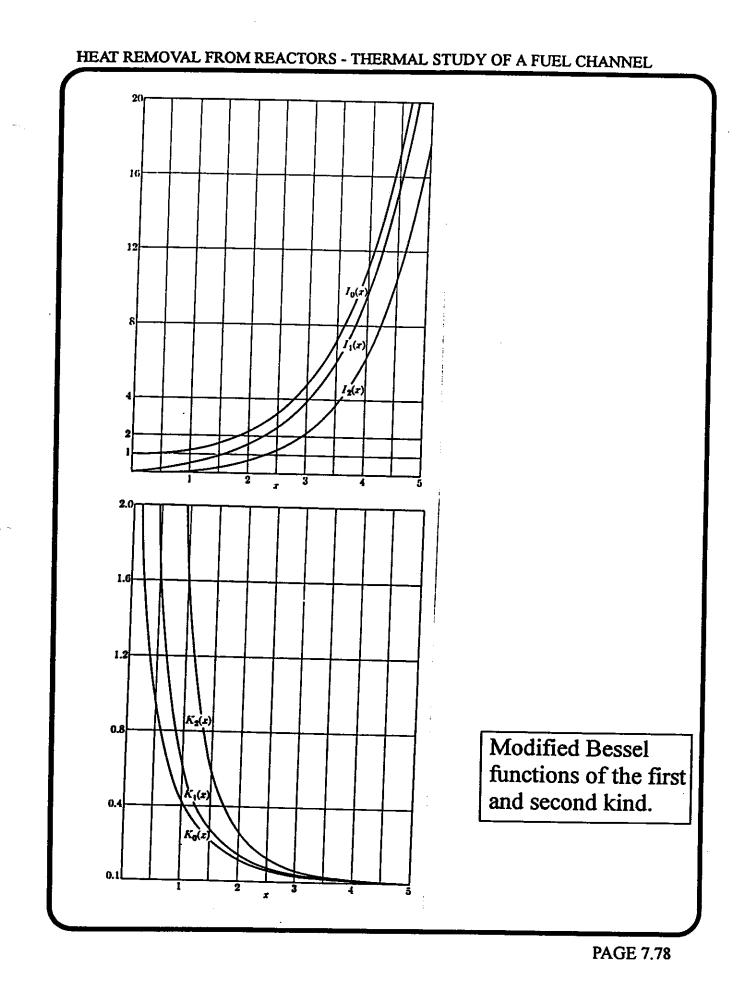
 κ : inverse of the thermal diffusion length in the fuel

• SINCE
$$q''' \sim \phi$$

$$q^{\prime\prime\prime} = q_o^{\prime\prime\prime} I_o(\kappa r)$$

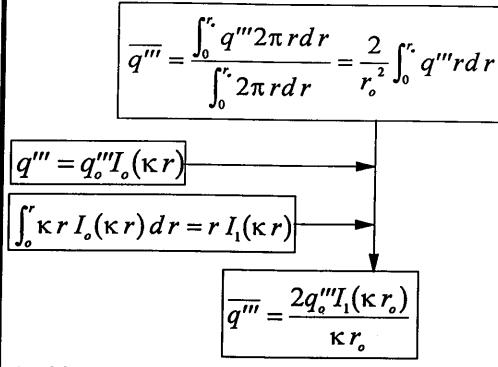






TEMPERATURE DISTRIBUTION IN THE FUEL WITH NEUTRON DEPRESSION

THE AVERAGE HEAT SOURCE (POWER DENSITY) OVER THE CROSS SECTION OF THE FUEL IS DEFINED AS:



RECONSIDER:

$$\boxed{\int_{t_{r}}^{t} k \, dt = \frac{q_{o}^{\prime\prime\prime\prime}}{\kappa^{2}} [I_{o}(\kappa r_{o}) - I_{o}(\kappa r)]}$$

$$\int_{t_{r}}^{t} k \, dt = \frac{q_{o}^{\prime\prime\prime\prime}}{\kappa^{2}} [I_{o}(\kappa r_{o}) - 1]$$

$$\boxed{\overline{q^{\prime\prime\prime\prime}} = \frac{2q_{o}^{\prime\prime\prime}I_{1}(\kappa r_{o})}{\kappa r_{o}}}$$

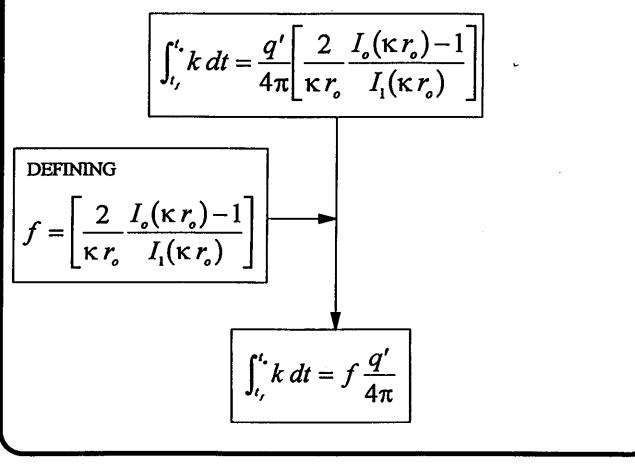
$$\boxed{q^{\prime} = \pi r_{o}^{2} \overline{q^{\prime\prime\prime\prime}}}$$

TEMPERATURE DISTRIBUTION IN THE FUEL WITH NEUTRON DEPRESSION

1

$$\int_{t_{r}}^{t} k \, dt = \frac{q'}{4\pi} \frac{2}{\kappa r_{o}} \frac{1}{I_{1}(\kappa r_{o})} \left[I_{o}(\kappa r_{o}) - I_{o}(\kappa r) \right]$$
$$\int_{t_{r}}^{t} k \, dt = \frac{q'}{4\pi} \left[\frac{2}{\kappa r_{o}} \frac{I_{o}(\kappa r_{o}) - 1}{I_{1}(\kappa r_{o})} \right]$$

CONSIDER AGAIN:



TEMPERATURE DISTRIBUTION IN THE FUEL WITH NEUTRON DEPRESSION

- f IS CALLED "FLUX DEPRESSION FACTOR."
- f IS A FUNCTION OF:
 - THE FUEL ENRICHMENT, AND
 - ► THE FUEL ROD DIAMETER.

· •

- FOR NATURAL URANIUM AND FOR LOW ENRICHED URANIUM (<2.5%), f is slightly less than 1.
- FOR HIGH ENRICHMENT f IS INCREASINGLY SMALL-ER THAN 1.
 - ► f VALUES FOR A URANIUM DIOXIDE PELLET OF 95% THE-ORETICAL DENSITY AND 9.4 mm IN ARE:

ENRICHMENT %	f	
0.	1.	UATURAL URAN'I VM
5	0.94	
10	0.87	
15	0.79	
20	0.72	

$$f = \left[\frac{2}{\kappa r_o} \frac{I_o(\kappa r_o) - 1}{I_1(\kappa r_o)}\right]$$

$$\int_{t_{r}}^{t_{r}} k \, dt = f \frac{q'}{4\pi}$$

PAGE 7.81

TEMPERATURE DISTRIBUTION IN THE FUEL WITH NEUTRON DEPRESSION

EFFECT OF f ON q' (LINEAR POWER DENSITY): • INTEGRAL OF CON-DUCTIVITY FOR UNIFORM HEAT GENERATION. • INTEGRAL OF CON-DUCTIVITY FOR NON-UNIFORM HEAT GENERATION. $\Rightarrow \int_{t_i}^{t_i} k \, dt = f \left[\frac{q'}{4\pi} \right]_{NU}$

• THE COMPARISON OF THE ABOVE INTEGRAL OF CONDUCTIVITY FOR THE SAME t_f and t_o YIELDS:

$$\frac{\left[q'\right]_{NU}}{\left[q'\right]_{U}} = \frac{1}{f}$$

• CONSEQUENTLY:

 $[q']_{\scriptscriptstyle NU} > [q']_{\scriptscriptstyle U}$

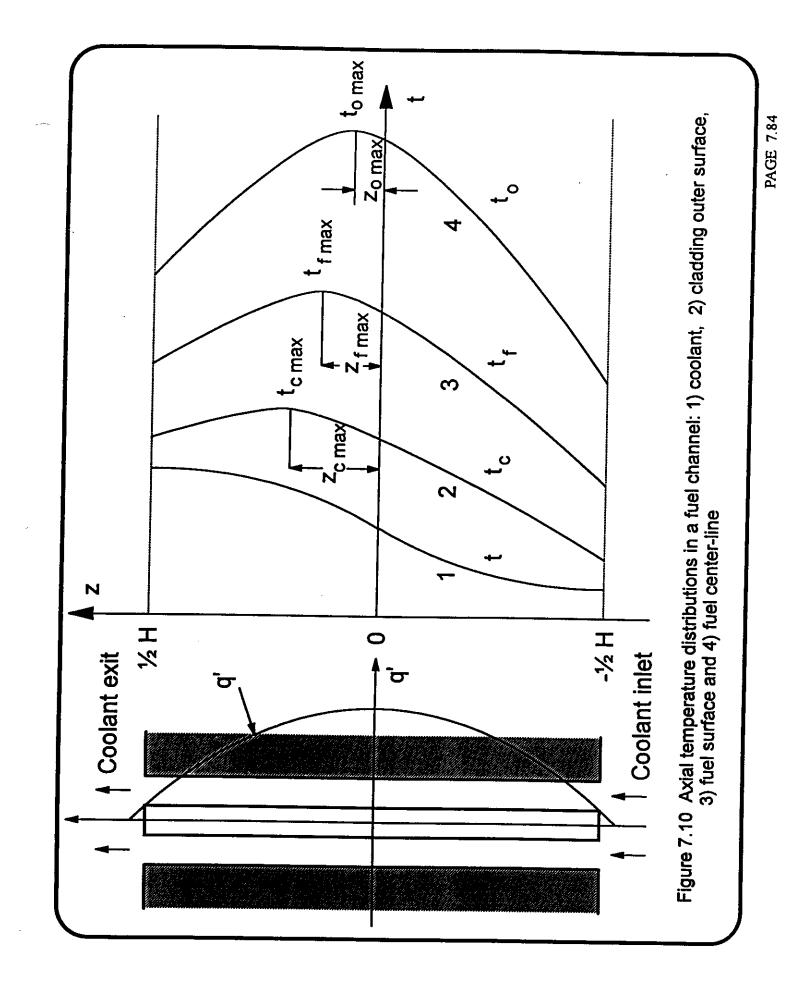
REMARKS ON CHANNEL TEMPERATURES

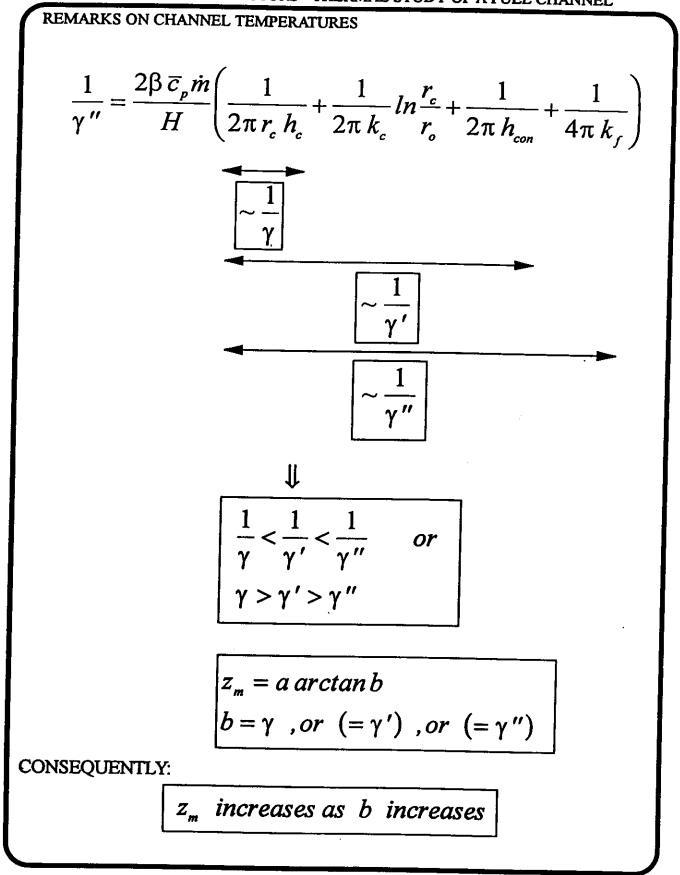
REMARKS ON THE FUEL CHANNEL TEMPERATURE

• VARIATION OF THE TEMPERATURES ALONG THE CHANNEL:

FIGURE 7.10

- COMMENT ON THE COOLANT TEMPERATURE.
- COMMENTS ON THE TEMPERATURE OF:
 - ► THE OUTER SURFACE OF THE CLADDING,
 - ► THE FUEL SURFACE,
 - ► THE FUEL CENTERLINE.
- REASONS OF SUCH A VARIATION:
 - COOLANT TEMPERATURE INCREASES STEADILY PAST THE MID-PLANE OF THE CHANNEL.
 - LINEAR POWER (LINEAR HEAT FLUX) CHANGES VERY SLOWLY IN THE VICINITY OF THE CHANNEL MID-PLANE.
- AS WE MOVE AWAY FROM THE FUEL CENTER, THE MA-XIMUM TEMPERATURES SHIFTS TOWARD THE EXIT OF THE FUEL CHANNEL.





REMARKS ON CHANNEL TEMPERATURES

- IN OTHER WORDS, THE LOCATION OF THE MAXIMUM TEMPERATURE IS RELATED TO THE THERMAL RESIS-TANCE.
- THIS LOCATION SHIFTS FURTHER DOWNSTREAM OF THE FUEL CHANNEL MID-PLANE AS THE THERMAL **RESISTANCE DECREASES.**
- OTHER COMMENTS:
 - ► CLADDING AND FUEL CENTERLINE TEMPERATURES TO-GATHER WITH CHF IMPOSE LIMITATION ON THE MAXI-MUM ALLOWABLE HEAT GENERATION IN THE FUEL ELEMENT.
 - ► THE POWER DENSITY PROFILE ALONG THE CHANNEL IS NOT ALWAYS SYMMETRICAL BECAUSE OF:
 - THE FUEL-MODERATOR DENSITY VARIATIONS,
 - THE FUEL LOADING AND UNLOADING (CANDU),
 - THE MOVEMENT OF THE CONTROL RODS.
 - PHYSICAL PROPERTIES OF THE COOLANT VARY WITH TEM-PERATURE; CONSEQUENTLY h VARIES ALONG THE CHANNEL.
 - A CONSTANT h_{i} BASED ON THE AVERAGE CHANNEL TEM-PERATURES YIELDS:
 - 5 TO 10 % ERROR ON h_c FOR LIQUID COOLANTS, ~3 % ERROR ON h_c FOR GAS COOLANTS.

PRESSURE DROP IN FUEL CHANNELS AND PUMPING POWER

- PRESSURE DROP THROUGH THE FUEL CHANNEL
 - AS THE COOLANT FLOWS THOUGH THE CHANNEL ITS PRES-SURE DROPS DUE TO:
 - 1. THE FRICTION BETWEEN THE COOLANT AND WALL,
 - 2. THE ACCELERATION AS THE SPECIFIC MASS OF THE COOLANT DECREASES WITH INCREASING TEMPERA-TURE, OR VAPOR FORMATION,
 - 3. THE GRAVITY.
 - ACCELERATION PRESSURE DROP IS SMALL IN LIQUID COOLED REACTORS BUT MAY BE SIGNIFICANT IN A GAS COOLED REACTOR OR IN A REACTOR WHERE BOILING TAKES PLACE.
- THE TOTAL PRESSURE DROP GRADIENT IN A FUEL CHANNEL IS GIVEN BY:

$$-\frac{dp}{dz} = \left(\frac{dp}{dz}\right)_{f} + \left(\frac{dp}{dz}\right)_{a} + \left(\frac{dp}{dz}\right)_{g} = \frac{4\tau_{w}}{D} + G\frac{d}{dz}v + \rho g$$

$$p : pressure, N/m^{2}$$

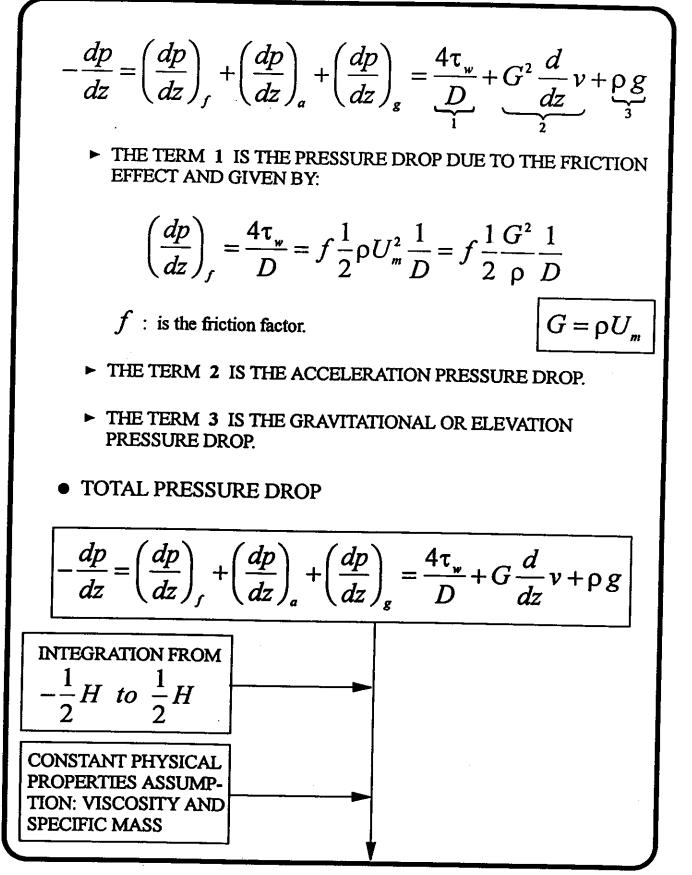
$$\tau_{w} : wall shear stress, N/m^{2}$$

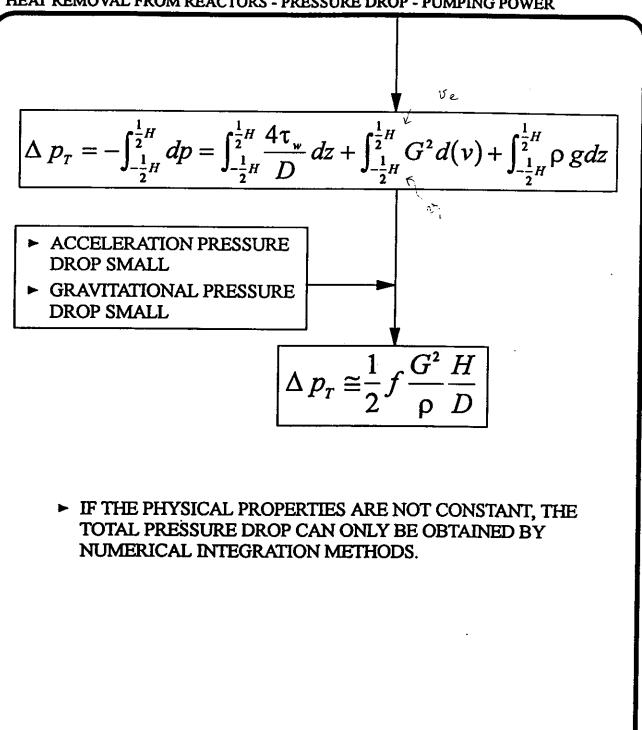
$$D : diameter or hydraulic diameter of the channel, m$$

$$G : mass flux of the coolant, kg/m^{2}s$$

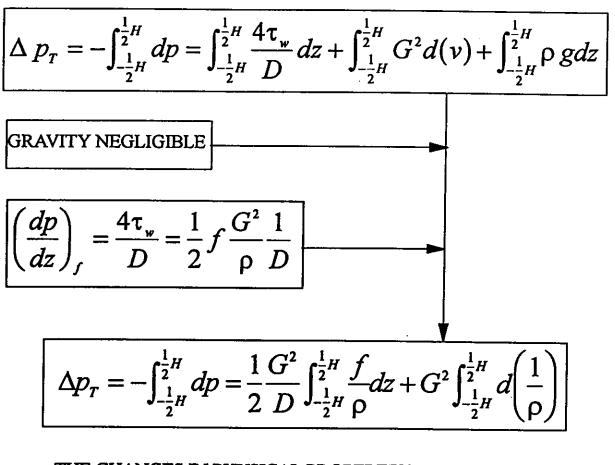
$$v : specific volume of the coolant, m^{3}/kg$$

- ρ : specific mass of the coolant, kg/m³
- g : acceleration of the gravity, m/s^2





• FOR GAS COOLANTS, ACCELERATION TERM CAN NOT BE NEGLECTED.



- THE CHANGES IN PHYSICAL PROPERTIES OF THE GAS COO-LANTS ARE DUE:
 - TO THE CHANGES IN TEMPERATURES
 - RATHER THAN THE CHANGES IN PRESSURES.
- FOR PRACTICAL PURPOSES, THE PRESSURE CAN BE TAKEN CONSTANT AND EQUAL TO:

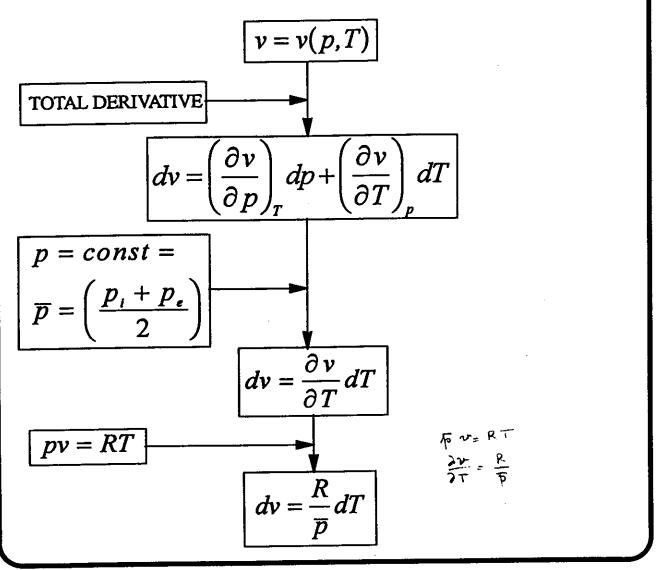
$$\overline{p} = \frac{p_i + p_e}{2}$$

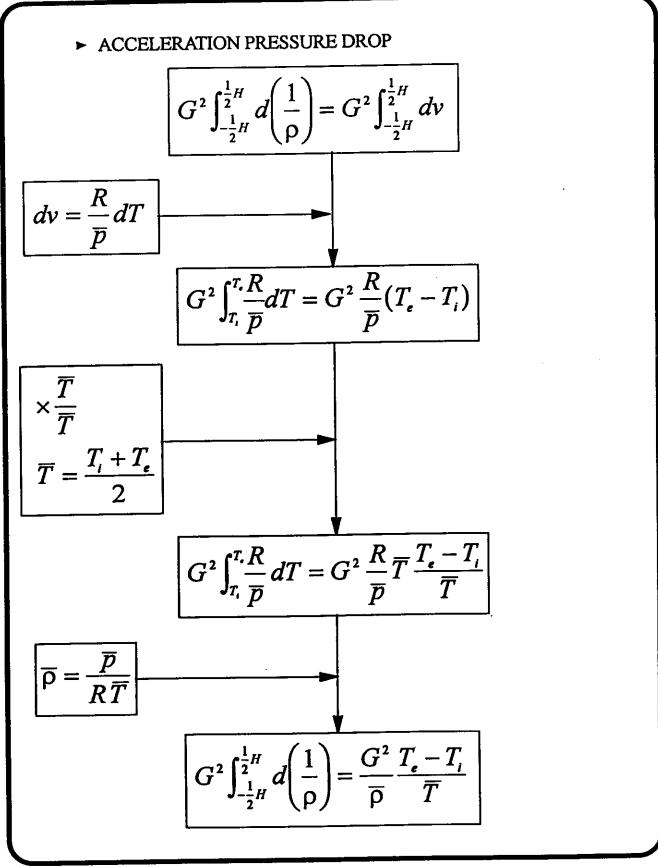
 p_i : inlet pressure, p_i : exit pressure.

THE VARIATION OF THE VISCOSITY OF GASES WITH THE TEMPERATURE IS SLOW.

•
$$f \sim Re^{-0.2} \sim \mu^{0.2}$$
 $\left(Re = \frac{\rho UD}{\mu}\right)$

- THE CHANGES IN f WITH TEMPERATURE IS EVEN SMALLER.
- CONSEQUENTLY, f CAN BE TAKEN AS CONSTANT.
- ► SPECIFIC VOLUME OF THE GAS COOLANT





TOTAL PRESSURE DROP

$$\Delta p_{T} = -\int_{-\frac{1}{2}H}^{\frac{1}{2}H} dp = \frac{1}{2} \frac{G^{2}}{D} \int_{-\frac{1}{2}H}^{\frac{1}{2}H} \frac{f}{\rho} dz + G^{2} \int_{-\frac{1}{2}H}^{\frac{1}{2}H} d\left(\frac{1}{\rho}\right)$$

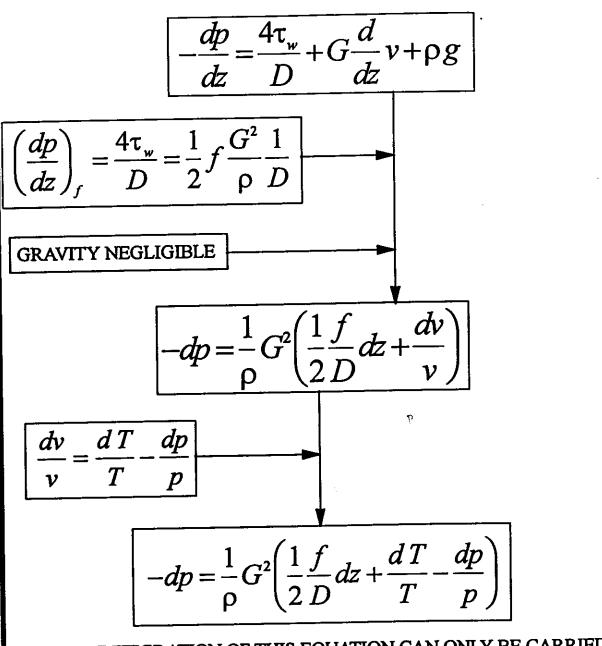
$$f = const.$$

$$\rho = \overline{\rho} = \frac{\overline{p}}{R\overline{T}}$$

$$G^{2} \int_{-\frac{1}{2}H}^{\frac{1}{2}H} d\left(\frac{1}{\rho}\right) = \frac{G^{2}}{\overline{\rho}} \frac{T_{e} - T_{i}}{\overline{T}}$$

$$\Delta p_{T} = p_{i} - p_{e} = \frac{1}{2} f \frac{G^{2}}{\overline{\rho}} \frac{H}{D} + \frac{G^{2}}{\overline{\rho}} \frac{(T_{e} - T_{i})}{\overline{T}}$$

A MORE ACCURATE SOLUTION REQUIRES TO TAKE INTO ACCOUNT THE EFFECT OF PRESSURE CHANGES ON THE SPECIFIC VOLUME OF THE GAS.



THE INTEGRATION OF THIS EQUATION CAN ONLY BE CARRIED OUT NUMERICALLY.

- IN MOST OF THE GAS COOLED REACTORS THE TERM:

 $\frac{G^2}{\rho}\frac{dT}{T}$

ACCOUNTS 10 TO 15% OF THE TOTAL PRESSURE DROP.

- THE TERM:

 $\frac{G^2}{\rho} \frac{dp}{p}$

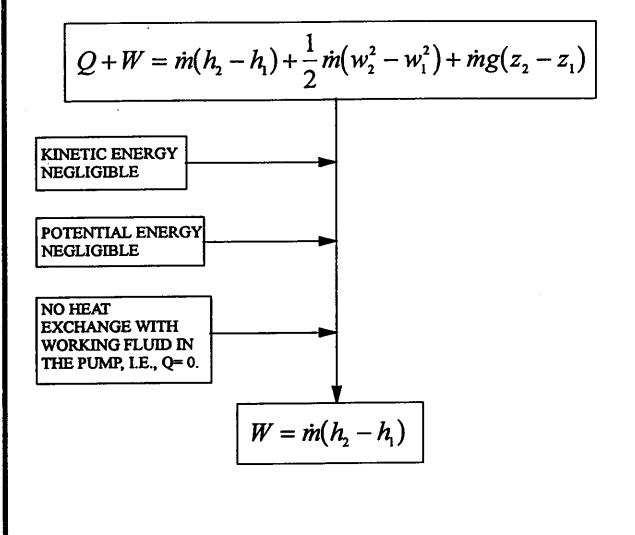
ACCOUNTS FOR 1 TO 2% OF THE TOTAL PRESSURE DROP.

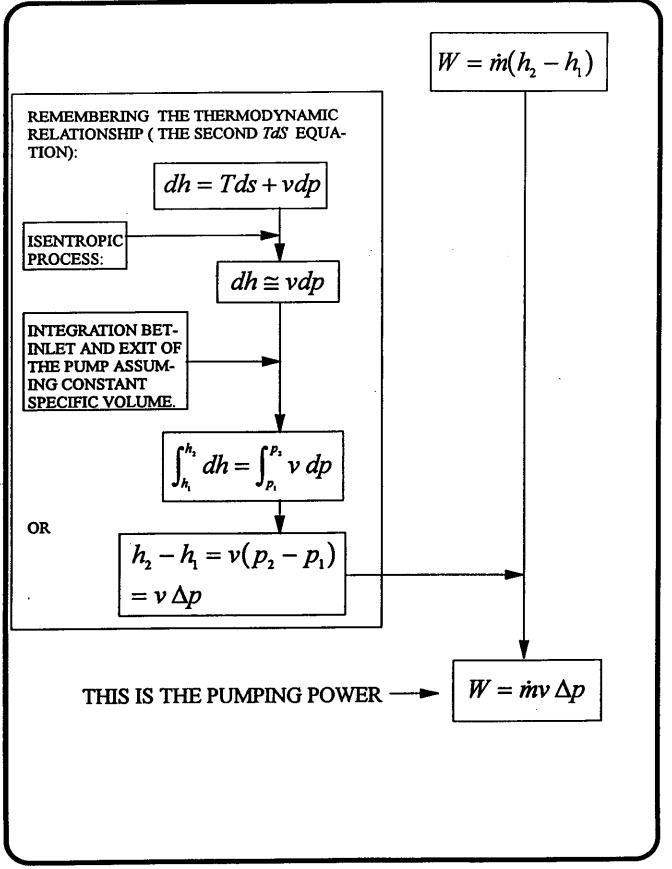
- IN THE PRELIMINARY DESIGN, $-\frac{G^2}{\rho}\frac{dp}{p}$ can be neglected.

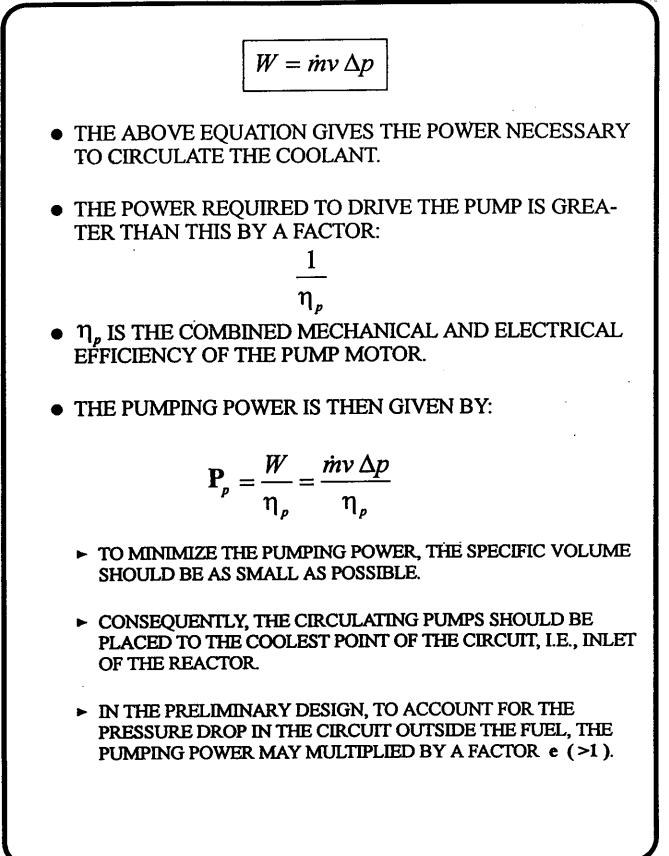
POWER REQUIRED TO CIRCULATE THE COOLANT - PUMPING POWER

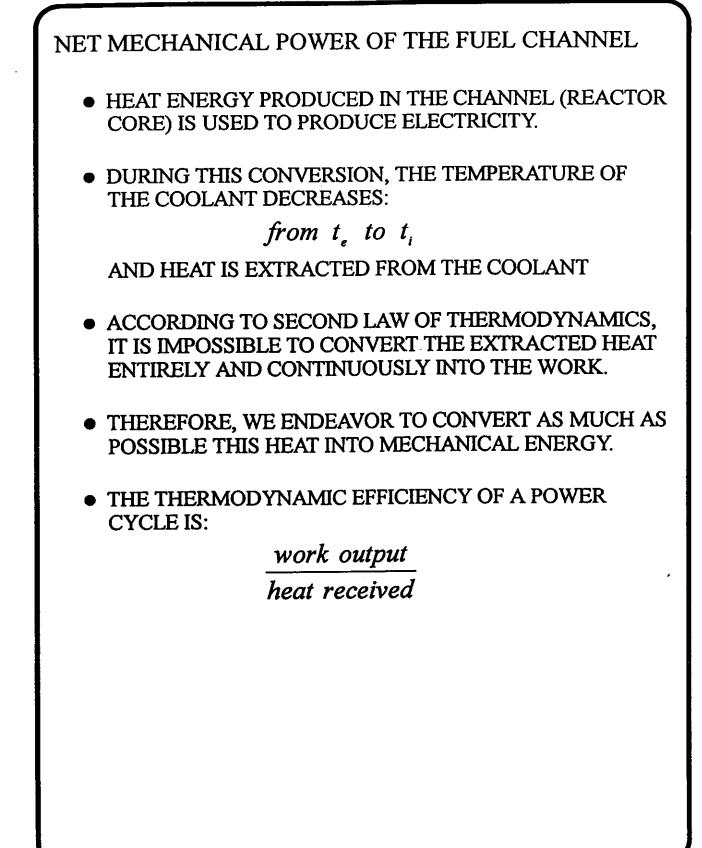
- A PUMP IS USED TO CIRCULATE THE COOLANT THROUGH THE FUEL CHANNEL.
- THE PRESSURE RISE ACROSS THIS PUMP BALANCES THE DROP IN PRESSURE OF THE FLOWING COOLANT IN FUEL CHANNELS.
- TO PRODUCE THE PRESSURE RISE MECHANICAL ENERGY IS ADDED TO THE COOLANT IN THE PUMP.
- SUBSEQUENTLY, THIS MECHANICAL ENERGY IS TRANSFORMED INTO THERMAL ENERGY AND TO-GATHER WITH THE THERMAL ENERGY FROM THE FUEL IS ADDED TO THE COOLANT.
- THE CONVERSION OF THE TOTAL THERMAL ENERGY INTO MECHANICAL (ELECTRICAL) ENERGY IS ACHIEV-ED WITH AN EFFICIENCY OF 30%.
- THE USE OF ELECTRICAL ENERGY TO DRIVE THE PUMPS AND SUBSEQUENT RECONVERSION INTO ELECTRICAL ENERGY WITH AN EFFICIENCY OF 30% REDUCES THE OVERALL EFFICIENCY OF THE POWER PLANT.
- WHEN POWER INPUT TO THE PUMPS INCREASES, THE SIZE AND THE COST ALSO INCREASE.

- IN LIQUID COOLED REACTORS, THE PUMPING POWER CORRESPONDS 3 TO 4% OF THE ELECTRICAL OUTPUT.
- IN GAS COOLED REACTORS, THE PUMPING POWER IS WITHIN 6 TO 15% OF THE ELECTRICAL OUTPUT.
- THE PUMPING POWER IS CALCULATED BY USING THE ENERGY CONSERVATION PRINCIPLE FOR A FLOWING SYSTEM:









- THE BASIC THERMODYNAMIC CYCLE IS THE CARNOT CYCLE. IN THIS CYCLE:
 - ALL HEAT IS RECEIVED ISOTHERMALLY AT A TEMPERA-TURE, T_h .
 - ALL HEAT IS REJECTED ISOTHERMALLY AT A LOWER TEMPERA TURE, T_c .
 - ► ALL THE PROCESSES IN THE CYCLE ARE REVERSIBLE.
 - ► THERMAL EFFICIENCY OF THE CARNOT CYCLE IS GIVEN BY:

$$\eta_c = 1 - \frac{T_c}{T_h}$$

 WHEN THE TEMPERATURE OF THE COOLANT LEAVING THE REACTOR DECREASES

from t to
$$t-dt$$

IT RELEASES PER UNIT OF MASS A HEAT ENERGY EQUAL TO THE

the change of enthalpy, dh.

• THIS HEAT ENERGY CAN BE CONVERTED TO WORK WITH A MAXIMUM EFFICIENCY GIVEN BY:

$$\eta_c = 1 - \frac{T_c}{T}$$

PAGE 7.101

Go tax

• TOTAL HEAT RELEASED BY THE COOLANT WHEN ITS TEMPERATURE DECREASES

from t_e to t_i (or enthalpy from h_e to h_i) IS GIVEN BY:

$$\mathbf{P}_{\mathbf{c}} = \int_{h_{i}}^{h_{i}} dh = \int_{T_{i}}^{T_{i}} \overline{c}_{p} dT$$

WHERE T IS THE ABSOLUTE TEMPERATURE.

 THE MAXIMUM WORK THAT CAN BE RECOVERED FROM THIS HEAT IS:

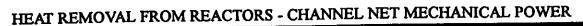
$$W_{\max} = \int_{T_i}^{T_c} \left(1 - \frac{T_c}{T}\right) dh = \int_{T_i}^{T_c} \left(1 - \frac{T_c}{T}\right) \overline{c}_p dT$$

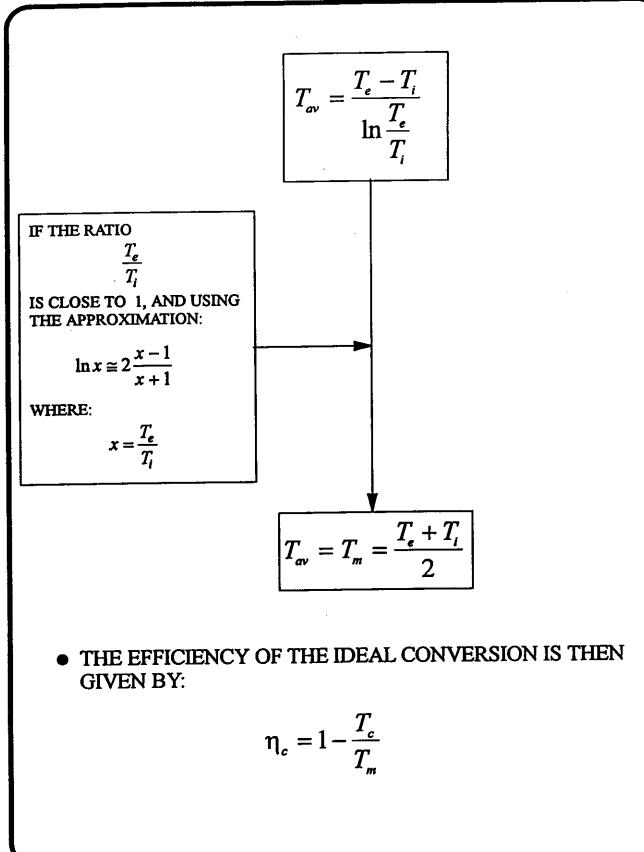
 THE EFFICIENCY OF THIS IDEAL CONVERSION IS GI-VEN BY

$$\eta_{c} = \frac{W_{\text{max}}}{P_{c}} = \frac{\int_{T_{c}}^{T_{c}} \left(1 - \frac{T_{c}}{T}\right) \overline{c}_{p} dT}{\int_{T_{c}}^{T_{c}} \overline{c}_{p} dT} = 1 - \frac{T_{c}}{T_{av}}$$

• T_{av} IS THE LOGARITHMIC MEAN TEMPERATURE OF THE COOLANT DEFINED AS:

$$T_{av} = \frac{T_e - T_i}{\ln \frac{T_e}{T_i}}$$





- ► IN CANDU REACTORS, TYPICAL INLET AND EXIT TEMPERA-TURES OF THE COOLANT ARE 267 °C AND 312 °C, RESPEC-TIVELY.
- ► THE CORRESPONDING LOGARITHMIC MEAN TEMPERA-TURE IS: 289.2 ° C.
- ► THE ARITHMETIC MEAN TEMPERATURE IS: 289.5 °C.
- ► THEREFORE T_{m} CAN BE REPLACED BY T_{m} .
- WE HAVE SEEN THAT FOR A IDEAL ENERGY CONVER-SION SYSTEM, THE HEAT ENERGY CONVERTED INTO MECHANICAL ENERGY IS:

$$\mathbf{W}_{max} = \eta_c \mathbf{P}_c$$

- HOWEVER, REAL ENERGY CONVERSION SYSTEMS ARE NOT PERFECT AND HAVE SEVERAL IRREVERSIBILITIES SUCH AS:
 - ► FRICTION,
 - ► HEAT TRANSFER WITH FINITE TEMPERATURE DIFFERENCE,
 - ► ETC.

- THEREFORE, THE EFFICIENCY OF THE REAL SYSTEMS IS LESS THAN THE EFFICIENCY OF THE IDEAL SYS-TEMS.
- INTRODUCING A FACTOR " $\eta_r < 1$ " TO TAKE INTO AC-COUNT THE IRREVERSIBILITIES, THE RECOVERABLE MECHANICAL ENERGY IS GIVEN BY:

 $W = \eta_r \eta_c P_c = \eta P_c$

- η is the combined thermal efficiency of
 - ► THE STEAM CYCLE, AND
 - ► THE TURBO GENERATORS.
- THE EFFICIENCY OF NUCLEAR POWER PLANTS IS A-BOUT 30%.
- P. SHOWS THE THERMAL OUTPUT OF THE FUEL CHANNEL.
- IN CALCULATING THE TOTAL THERMAL OUTPUT OF THE CHANNEL, P_T , THE POWER TO CIRCULATE THE COOLANT, $\eta_p P_p$, SHOULD BE ADDED TO THE THER-MAL POWER OF THE CHANNEL:

$$\mathbf{P}_{T} = \mathbf{P}_{c} + \eta_{p} \mathbf{P}_{p}$$

• THE GROSS ELECTRICAL POWER IS THEN GIVEN BY:

$$\eta \left(\mathbf{P}_{c} + \eta_{p} \mathbf{P}_{p} \right)$$

• THE NET ELECTRIC POWER IS:

$$\mathbf{W}_{net} = \eta \left(\mathbf{P}_{c} + \eta_{p} \mathbf{P}_{p} \right) - \mathbf{P}_{p} = \eta \mathbf{P}_{c} - \left(1 - \eta \eta_{p} \right) \mathbf{P}_{p}$$

• THE OVERALL EFFICIENCY OF THE FUEL CHANNEL IS:

$$\eta_{net} = \frac{\mathbf{W}_{net}}{\mathbf{P}_c} = \eta - (1 - \eta \eta_p) \frac{\mathbf{P}_p}{\mathbf{P}_c}$$

- THE EFFICIENCY OF THE PUMPS VARIES BETWEEN: 65% AND 95%.
- ► IN PWR AND CANDU REACTORS THE EFFICIENCY OF THE PUMPS IS BETWEEN 90% AND 92%.

OPTIMUM OPERATING POINT OF A CHANNEL

• TO DISCUSS THE OPTIMUM OPERATING POINT OF THE CHANNEL IT WILL BE ASSUMED THAT:

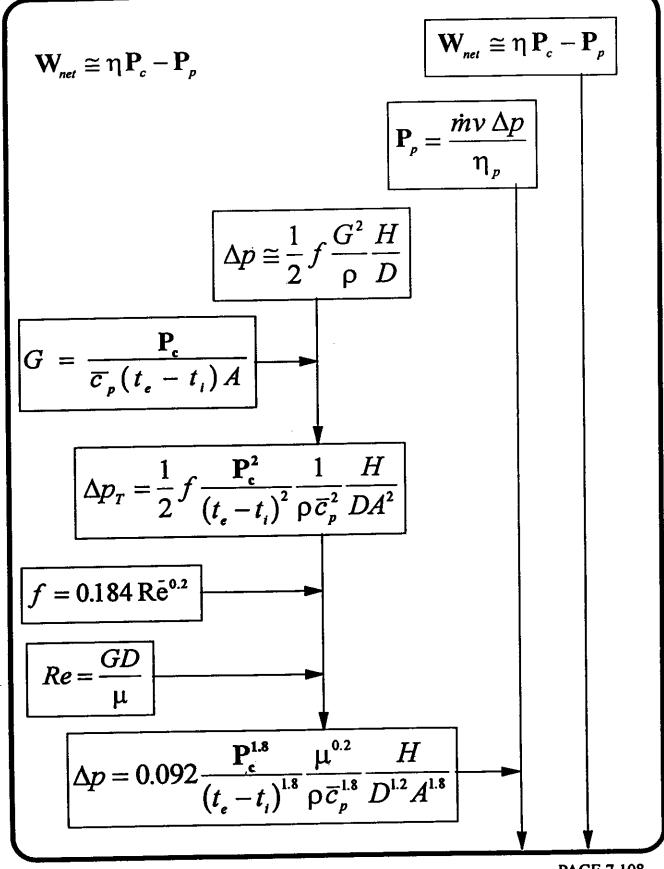
$$\eta_p \mathbf{P}_p < \mathbf{P}_c$$

• THEREFORE WE WRITE:

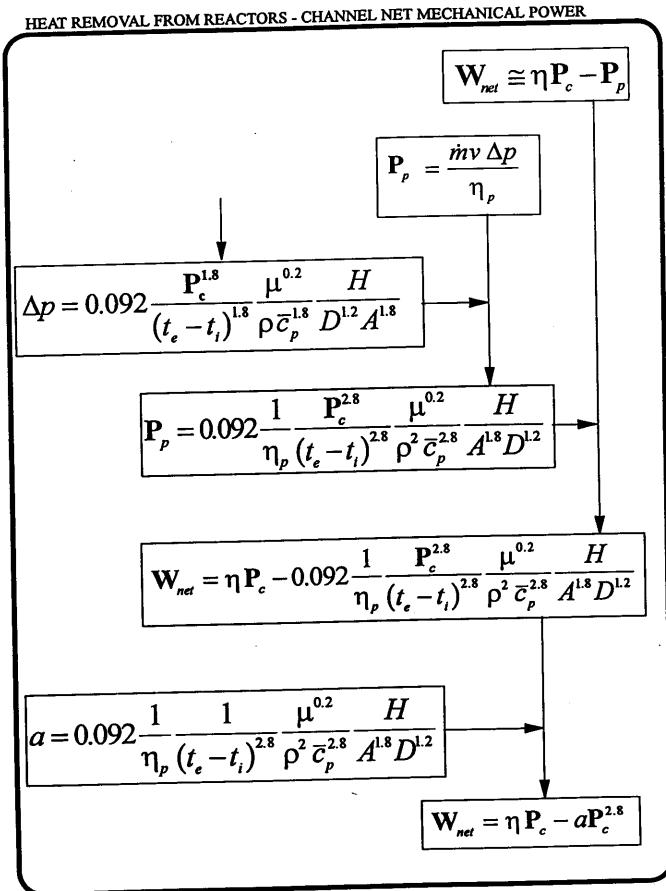
$$\mathbf{P}_{\tau} \cong \mathbf{P}_{c}$$

• THE NET ELECTRICAL POWER OF THE CHANNEL BECOMES:

$$\mathbf{W}_{net} \cong \eta \, \mathbf{P}_c - \mathbf{P}_p$$

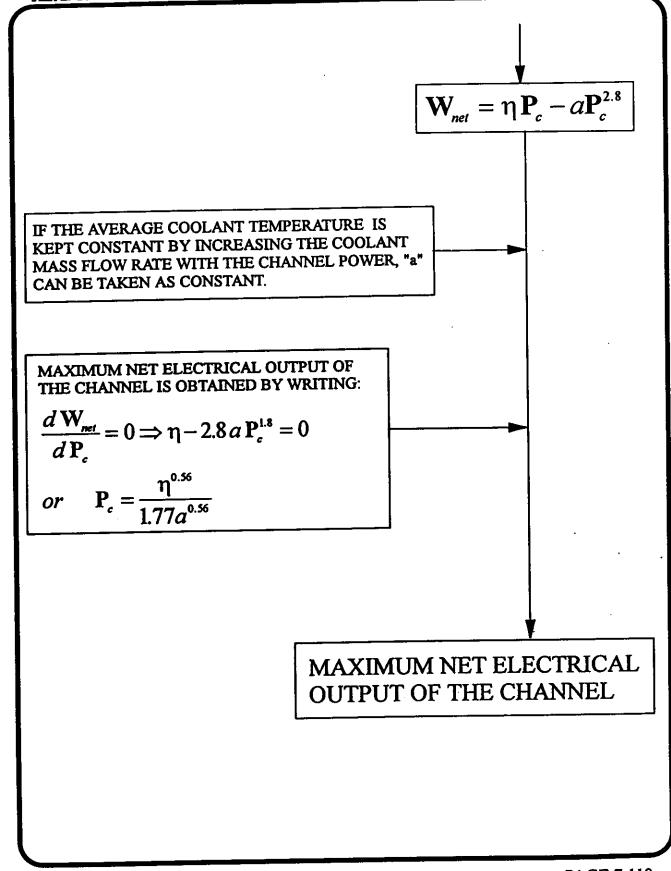


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► BEYOND THE MAXIMUM THERMAL CHANNEL POWER:

$$\mathbf{P}_{c} = \frac{\eta^{0.56}}{1.77a^{0.56}}$$

THE NET ELECTRICAL POWER FROM THE CHANNEL STARTS FALLING BECAUSE OF THE HIGH POWER REQUIRED TO CIRCULATE THE COOLANT.

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THE CHOICE OF COOLANT FOR REACTORS

- THE COOLANT MAY BE A GAS (CARBON DIOXIDE OR HELIUM) OR LIQUID (LIGHT OR HEAVY WATER OR AN EUTECTIC SODIUM-POTAS#SIUM ALLOY).
- COOLANT SELECTION CRITERIA:
 - ► ECONOMICS:

LOW COST, AVAILABILITY, LOW PUMPING POWER, HIGH HEAT TRANSFER COEFFICIENT.

► PHYSICS:

LOW FUSION POINT, HIGH BOILING TEMPERATURE, COMPATIBILITY WITH FUEL, CLADDING, VALVES, PIPING, ETC., GOOD THERMAL STABILITY.

► NEUTRONICS:

LOW NEUTRON CAPTURE CROSS-SECTION, MODERATING POWER COMPATIBLE WITH THE TYPE OF THE REACTOR (THERMAL OR FAST), LOW RADIOACTIVITY, GOOD STABILITY UNDER IR RADIATION.

- HELIUM AND CARBON DIOXIDE ARE VERY SUITABLE GASES
 - ► THE COST OF HELIUM IS HIGH.

- LIGHT AND HEAVY WATER ARE SUITABLE FOR THER-MAL REACTORS:
 - ► PLAY DUAL ROLE: MODERATING AND COOLING.
 - ► HIGH TEMPERATURES IN BOTH FLUIDS REQUIRE HIGH SYS-TEM PRESSURES:
 - THICK PRESSURE VESSELS OR TUBES.
 - THE CAPTURE CROSS-SECTION OF LIGHT WATER IS HIGH:
 ENRICHED URANIUM IS REQUIRED TO ACHIEVE THE CRI-TICALITY.
 - ► HEAVY WATER HAS VERY LOW CAPTURE CROSS-SECTION BUT IT IS EXPENSIVE.
 - ► BOTH WATERS REQUIRE STAINLESS STEEL OR ZIRCALLOY CLADDING.
- LIQUID METALS SODIUM-POTASSIUM ALLOY
 - ► ADVANTAGES:
 - HAVE HIGH SATURATION TEMPERATURE AT ATMOSPHE-RIC PRESSURE - A PRESSURIZED COOLANT SYSTEM IS NOT REQUIRED.
 - DO NOT MODERATE FAST NEUTRONS; SUITABLE FOR FAST REACTORS.
 - ► DISADVANTAGES:
 - RADIATION HAZARD BECAUSE OF ${}^{23}Na(n,\gamma)^{24}Na$ REACTION.
 - VIOLENT CHEMICAL REACTION WITH AIR AND WATER.
 - HIGH NEUTRON CAPTURE CROSS-SECTION FOR THER-MAL NEUTRONS - NOT SUITABLE FOR THERMAL REAC-TORS.

• A GOOD COMPARISON OF THE PERFORMANCE OF DIF-FERENT COOLANTS CAN BE UNDERTAKEN BY EXAM-INING THE RATIO OF:

> pumping power channel thermal power

WHICH HAS THE FOLLOWING FORM:

$$\frac{\mathbf{P}_{p}}{\mathbf{P}_{c}} = \underbrace{\left[0.092 \frac{1}{\eta_{p}} \frac{\mathbf{P}_{c}^{1.8}}{\left(t_{e} - t_{i}\right)^{2.8}} \right] \left[\frac{\mu^{0.2}}{\rho^{2} \, \overline{c}_{p}^{2.8}} \right] \left[\frac{H}{D^{1.2} \, A^{1.8}} \right]}_{2}$$

- ► THE TERM 1 IS RELATED TO THE OPERATING POINT OF THE CHANNEL.
- ► THE TERM 2 IS RELATED TO THE PHYSICAL PROPERTIES OF THE COOLANT.
- THE TERM 3 IS RELATED TO THE GEOMETRY OF THE CHAN-NEL.
- FROM COOLANT POINT OF VIEW, THE TERM 2 SHOULD BE AS SMALL AS POSSIBLE TO ENSURE A MINIMUM:

$$\frac{\mathbf{P}_p}{\mathbf{P}_c}$$

• A BETTER DISCUSSION OF THE COOLANT EFFECT CAN BE CARRIED OUT BY WRITING THAT:

$$\mathbf{P}_{c} = h_{c} S \Delta t_{f}$$

WHERE

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- h_c : heat transfer coefficient between the rod and coolant,
- S : heat transfer surface,
- Δt_f : average temperature difference between the fuel element and coolant.

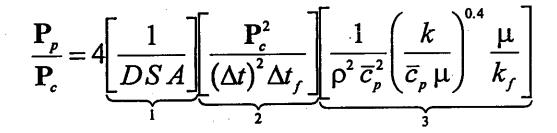
ASSUMING THAT HEAT TRANSFER COEFFICIENT IS GI-VEN BY:

$$h_c = 0.023 \frac{k_f}{D} \left(\frac{GD}{\mu}\right)^{0.8} \left(\frac{\overline{c}_p \mu}{k_f}\right)^{0.4}$$

THE RATIO:

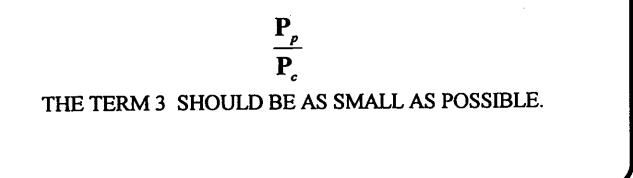
 $\frac{\mathbf{P}_p}{\mathbf{P}_a}$

CAN BE WRITTEN AS:



WHERE $\Delta t = (t_e - t_i)$.

- IN THE ABOVE EQUATION, THE PHYSICAL PROPERTIES OF THE COOLANT APPEAR IN THE TERM 3.
- IN ORDER TO ACHIEVE MINIMUM RATIO OF:



- TABLE 7.7 COMPARES SEVERAL COOLANTS FROM THE POINT OF VIEW OF PHYSICAL PROPERTIES.
- THE PROPERTIES WERE CALCULATED AT:
 - ► 0 °C FOR GASES, AND
 - ► 80 °C FOR LIQUIDS
- IT IS OBSERVED THAT HYDROGEN IS THE BEST GAS COOLANT FOLLOWED BY HELIUM AND STEAM. HOWEVER:
 - ► HYDROGEN IS EXPLOSIVE,
 - ► HELIUM IS EXPENSIVE,
 - ► STEAM IS CORROSIVE.
- CARBON DIOXIDE IS A SUITABLE COOLANT FOR GAS COOLED REACTORS.
- AIR AND NITROGEN HAVE ACTIVATION PROBLEMS.
- AMONG LIQUIDS WATER (LIGHT AND HEAVY) IS THE BEST, FOLLOWED BY LIQUID METALS.

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Table 7.7	Comparison	of the cool	lants
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Gas	$\left[\frac{1}{\rho^2 \overline{c}_p^2} \left(\frac{k}{\overline{c}_p \mu}\right)^{0.4} \frac{\mu}{k}\right]$	$\frac{X}{X_{H_2}}$	Liquids	$\left[\frac{1}{\rho^2 \bar{c}_p^2} \left(\frac{k}{\bar{c}_p \mu}\right)^{0.4} \frac{\mu}{k}\right]$	$\frac{X}{X_{H_1}}$		
H ₂	662	1.0	H ₂ O	0.0004425	1.0		
He	3,315	5.1	*Na	0.0008770	2.0		
H ₂ O	5,040	7.7	*Hg	0.0033500	7.6		
CO ₂	6,560	10.1	*Bi	0.0053000	12.0		
Air	8,150	12.5	Glycol	0.0091900	20.8		
N ₂	8,740	13.4	Freon-12	0.0095700	21.6		

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* A different correlation for heat transfer coefficient has been used.

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