

CHEMICAL ANALYSIS

A SERIES OF MONOGRAPHS ON
ANALYTICAL CHEMISTRY AND ITS APPLICATIONS

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PHYSICAL CONSTANTS

<i>Symbol</i>	<i>Denomination</i>	<i>Magnitude</i>
a.m.u.	atomic mass unit	931.48 MeV (^{12}C scale) 931.16 MeV (^{16}O scale)
<i>c</i>	light velocity in vacuum	$2.99793 \cdot 10^{10} \text{ cm s}^{-1}$
<i>e</i>	electron charge	$4.803 \cdot 10^{-10} \text{ esu}$
<i>h</i>	Planck's constant	$6.625 \cdot 10^{-27} \text{ erg s}$
\hbar	$= h/2\pi$	$1.0544 \cdot 10^{-27} \text{ erg s}$
<i>k</i>	Boltzmann's constant	$1.38047 \cdot 10^{-16} \text{ erg deg}^{-1}$
m_n	neutron mass	1.008665 a.m.u. (^{12}C scale) $1.6757 \cdot 10^{-24} \text{ g}$
m_e	electron rest mass	$5.486 \cdot 10^{-4} \text{ a.m.u. (^{12}\text{C} scale)}$ $9.107 \cdot 10^{-28} \text{ g}$
$m_e c^2$	electron rest energy	0.5110 MeV
m_p	proton rest mass	1.007273 (^{12}C scale) $1.6724 \cdot 10^{-24} \text{ g}$
N_A	Avogadro's number	$6.023 \cdot 10^{23} \text{ atoms mole}^{-1}$ (^{12}C scale)

LIST OF SYMBOLS

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LIST OF SYMBOLS

<i>Symbol</i>	<i>Denomination</i>	<i>Symbol</i>	<i>Denomination</i>
α	-alpha particle -conversion coefficient -quotient of distribution coefficients -correction factor in the internal standard method	α_x	-number of disintegrations -distance energy needed for a hole-electron pair creation (eV)
<i>A</i>	-mass number -atomic weight -activity (rate or number of disintegrations, - counts)	E_x	excitation energy of nucleus x (MeV) energy (MeV, keV, eV, erg, ...)
\AA	\AAngstrom (10^{-8} cm)	E_{C}	Coulomb barrier energy (MeV)
β	beta particle	E_{eff}	cadmium cut-off energy (eV)
β^-	negatron	E_{max}	effective threshold energy (MeV)
β^+	positron		maximum energy in beta spectrum (MeV)
<i>B</i>	background		energy corresponding to neutron velocity v_n (0.025 eV)
<i>b</i>	barn = unit of cross section (cm^2)	E_n	energy at the maximum of a resonance peak (eV)
<i>c</i>	number of counts	E_r	threshold energy (MeV)
<i>cm</i>	centimeter (10^{-2} m)		recoil energy of nucleus x (MeV)
<i>C</i>	-signal + background -capacity (Farad)	E_r	electron volt ($1.60 \cdot 10^{-12}$ erg)
<i>Ci</i>	Curie ($3.7 \cdot 10^{10}$ dps)	E_r	neutron flux (beam or multidirectional) ($n \text{ cm}^{-2} \text{ s}^{-1}$)
<i>Ci</i>	convolution integer	eV	equivalent fission flux ($n \text{ cm}^{-2} \text{ s}^{-1}$)
<i>CR</i>	cadmium ratio		φ at neutron energy E ($n \text{ cm}^{-2} \text{ s}^{-1}$)
<i>CR_x</i>	cadmium ratio of element (<i>isotope</i>) x		epicadmium neutron flux per unit of lethargy = conventional epicadmium flux ($n \text{ cm}^{-2} \text{ s}^{-1}$)
<i>CT</i>	clock time		φ_n at neutron energy E ($n \text{ cm}^{-2} \text{ s}^{-1}$)
δ	-density (g cm^{-3}) -residual standard deviation	$\varphi(E)$	
<i>D</i>	disintegration rate (dps, ...)		
<i>D_A</i>	distribution coefficient for species <i>A</i>		
<i>DT</i>	total dead time		
<i>d</i>	-absorption thickness (mg cm^{-2})	$\varphi_n(E)$	

<i>Symbol</i>	<i>Denomination</i>	<i>Symbol</i>	<i>Denomination</i>
φ^{**}	φ , corrected for resonance absorption at finite dilution ($n \text{ cm}^{-2} \text{ s}^{-1}$)	f_s	self-absorption coefficient for beta rays
φ_0	conventional thermal neutron flux = $n v_n$ ($n \text{ cm}^{-2} \text{ s}^{-1}$)	f_{th}	comparative half-life of beta decay
φ_{reactor}	conventional reactor neutron flux ($n \text{ cm}^{-2} \text{ s}^{-1}$)	Γ	thermal neutron absorption factor in solids
φ_{th}	conventional thermal neutron flux below E_{C} = $n_{th} v_n$ ($n \text{ cm}^{-2} \text{ s}^{-1}$)	Γ_s	nuclear level width (eV)
$\varphi_{th}(E)$	thermal neutron flux at energy E ($n \text{ cm}^{-2} \text{ s}^{-1}$)	γ	partial Γ (eV)
<i>F</i>	-14 MeV neutron flux ($n \text{ cm}^{-2} \text{ s}^{-1}$)	g	gram
	-Fano factor	h	-photopeak height (cm, activity)
	-decay correction factor for measurement of short lived activities (starting point of measuring interval)	I	-height
<i>FDT</i>	fractional dead time	I'	-hour
F_n	fraction of the disintegration of the nuclides of the n^{th} step, producing nuclides of the $(n+1)^{\text{th}}$ step in a disintegration chain	I_{abs}	resonance integral at infinite dilution (barn)
		I_{act}	I corrected for $1/v$ contribution (barn)
		IDT	absorption resonance integral at infinite dilution (barn)
		I^{**}	instantaneous dead time
<i>FWHM</i>	full width at half maximum of a (photo)peak (eV, keV, ...)		effective resonance integral = I corrected for resonance absorption = I at finite dilution (barn)
<i>f</i>	-total neutron absorption factor in solids	I_n	I for the n^{th} resonance peak (barn)
	-decay correction factor for the measurement of short lived activities (exact time within the measuring interval)	I_{tot}	= $\sum I_n$ (barn)
	-fission	I_s	I for the nuclear reaction of type s (barn)
	-fraction	I_s'	I' for the nuclear reaction of type s (barn)
<i>f'</i>	total neutron absorption factor in solution		resonance integral at infinite dilution obtained by integration of $\sigma_{1/v}$ (barn)
$f(E)$	fission neutron flux at energy E ($n \text{ cm}^{-2} \text{ s}^{-1}$)	κ	-linear absorption coefficient for pair production (cm^{-1})
f_n	epicadmium neutron absorption factor in solids		-dielectric constant

LIST OF SYMBOLS

Symbol	Denomination	Symbol	Denomination
K_r	distribution constant	mCi	milli-Curie (10^{-3} Curie)
k	-reactor reproduction factor	mg	milligram (10^{-3} gram)
	-constant	ml	milliliter = 10^{-3} liter
keV	kilo electron volt (10^3 eV)	$m\mu$	milli micron = 10^{-7} cm (10^{-8} micron)
kg	kilogram (10^3 g)	mm	millimeter (10^{-3} m)
λ	-radioactive decay constant (s^{-1})	ms	milli second (10^{-3} second)
	-wave length ($m\mu$, Å)	mV	-milli electron volt (10^{-3} eV)
l	mean free path (cm)		-millivolt (10^{-3} volt)
L	-liter	v	-frequency (s^{-1})
	-ligand		-neutrino
L_c	critical limit	N	-number of neutrons liberated per fission
L_d	detection limit		-number of neutrons in the nucleus
L_q	quantitative determination limit		-number of target nuclei per cm^3
LT	live time		-normality (g eq. L^{-1})
μ	-total mass absorption coefficient ($cm^2 mg^{-1}$)	n	-thermal neutron density from energy 0 to ∞ ($n cm^{-3}$)
	-micron (10^{-4} cm)		-neutron
μ'	total linear absorption coefficient (cm^{-1})		neutron density at energy E ($n cm^{-3}$)
μA	micro ampere (10^{-6} A)		nano gram (10^{-9} gram)
μb	micro barn (10^{-4} barn)	ng	nano second (10^{-9} second)
μCi	micro Curie (10^{-6} Curie)	n(E)	thermal neutron density below E_{th} ($n cm^{-3}$)
μg	micro gram (10^{-6} gram)		average n_{th} in the sample at finite dilution ($n cm^{-3}$)
μl	micro liter (10^{-6} liter)	ng	neutron density at velocity v ($n cm^{-3}$)
μ_n	mobility of electrons in n-type semiconductor material ($cm^2 V^{-1} s^{-1}$)	ns	-probability
	mobility of holes in p-type semiconductor material ($cm^2 V^{-1} s^{-1}$)	n_{th}	-peak to total ratio
μ_p	micro second (10^{-6} second)	\bar{n}_{th}	proton
μ_s	-molarity (mole L^{-1})	n(v)	-reaction energy (MeV, a.m.u., ...)
M	-factor of merit of a counter = $S/2\sqrt{E}$	P	-quality criterion of a counter
MeV	million electron volt (10^6 eV)	p	branching factor
m	-minute	Q	resistivity ($ohm cm^{-1}$)
	-mass	q	-reaction rate (s^{-1})
	-meter	p	count rate (cps, cpm, ...)
mA	milli ampere	R	
meq	milli equivalent		
mb	millibarn (10^{-8} barn)		

Symbol	Denomination	Symbol	Denomination
	-particle range	σ_a	cross section for compound nucleus formation (= σ_{ab}) (barn)
	-resolution	σ_{coh}	coherent scatter cross section (barn)
	-radius	σ_{col}	collision cross section (barn)
	-distance	$\sigma(D)$	standard deviation for a signal equal to the detection limit
	-resistance (ohm)	$\sigma(E)$	cross section at neutron energy E (barn)
R_A	-nuclear radius (Fermi unit = 10^{-18} cm)	σ_{eff}	effective cross section (barn)
	-recovery factor of species A	Σ	macroscopic cross section = σN (cm^{-1})
		Σ_x	macroscopic removal cross section of sample for 14 MeV neutrons (cm^{-1})
		$\Sigma_{(i)}$	macroscopic removal cross section of element i for 14 MeV neutrons (cm^{-1})
		σ	-effective microscopic target area (cm^2)
			-cross section (barn)
			-linear absorption coefficient for Compton effect (cm^{-1})
			-standard deviation for an infinite population
		σ_0	average cross section in a fission neutron spectrum (barn)
		$\sigma_{\%}$	percentage standard deviation (= percentage coefficient of variation)
		σ_{abs}	absorption cross section (= σ_c) (barn)
		σ_{act}	isotopic activation cross section (barn)
		$\bar{\sigma}_{act}$	average elemental activation cross section (barn)
		σ_r	resonance cross section (barn)

Symbol	Denomination	Symbol	Denomination
$\sigma_r(E)$	resonance cross section at neutron energy E (barn)	$T_{1/2}$	-total time = $\Delta t_a + \Delta t_p$. half-life = $\ln 2/\lambda$ (y, h, m, s, ...)
σ_{reactor}	cross section for a reactor neutron spectrum (barn)	T_m	Maxwellian temperature (°K)
$\sigma_{\text{reactor}}^{\text{eff}}$	effective $\sigma_{\text{reactor}} = \sigma_{\text{reactor}}$ corrected for absorption at finite dilution (barn)	T_0	293.6 °K
$\sigma_{E(1)}$	microscopic elemental removal cross section for 14 MeV neutrons (cm^{-2})	T_R	reactor period
$\bar{\sigma}_s$	average scatter cross section (barn)	t	-decay time (h, m, s, ...) -thickness (cm)
σ_t	total cross section (barn)	$t_{1/2}$	-temperature (°C)
σ_{th}	average cross section for neutron energies up to E_{ca} (barn)	t_b	time necessary to establish half of the equilibrium distribution in isotopic exchange
$\sigma(v)$	cross section at neutron velocity v (barn)	t_{eff}	irradiation time (h, m, s, ...)
$\sigma(\bar{v})$	cross section at neutron velocity \bar{v} (barn)	u	effective thickness for resonance neutron absorption (cm)
$\sigma_{1/v}$	cross section in the epicadmium region, disregarding resonance peaks (barn)	v	number of standard deviations
S	-saturation factor	$V(d)$	-volume (L, ml, μl , ...)
	-surface, area	v	-tension (volt)
	-signal		-volt
$S_{B/A}$	separation factor of species B from A = enrichment factor of A	v_1	electrical field
	= depletion factor for B	v_0	-neutron velocity (cm s^{-1})
s	-standard deviation for a finite population		average neutron velocity in a Maxwell-Boltzmann distribution (cm s^{-1})
	-second		neutron velocity at E_{ca} (cm s^{-1})
θ	-isotopic abundance		most probable neutron velocity in a Maxwell- Boltzmann distribution (2200 m/s at 20°C = 0.025 eV)
τ	-angle (degree, radian)	W_i	statistical weight
	-mean life (s, ...)	w	weight (g, mg, ...)
	-dead time (μs , ...)	y	-year
	-resolving time (μs , ...)	ζ	-fission yield
	-linear absorption co- efficient for photoelectric effect (cm^{-1})	Z	Fermi potential in a semiconductor (eV)
T	-absolute temperature (°K)	z	-atomic number
			-residual
			counting efficiency

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